

Modelling X-ray beacons in curved space time

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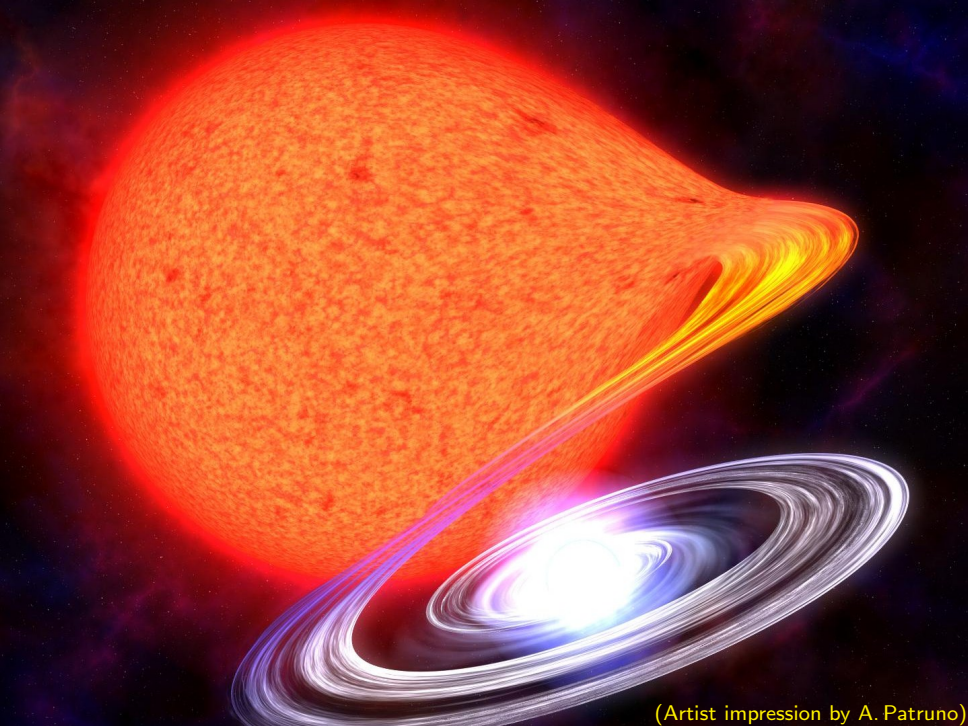
ESAC, 28th July

in collaboration with

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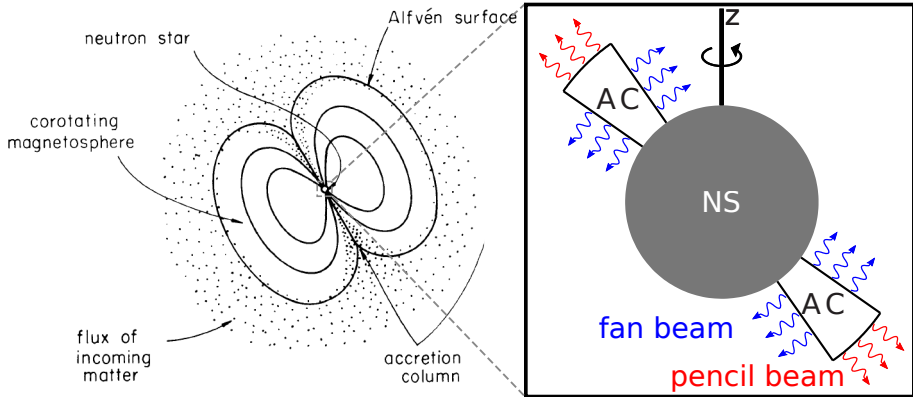
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²AIP, ³IAAT, ⁴ESA/ESAC, ⁵GMU,
⁶NRL SSD, ⁷SAI, ⁸CRESST, ⁹CASS





(Artist impression by A. Patruno)

Accreting neutron stars



(adapted from Lamb et al., 1973)

compact object

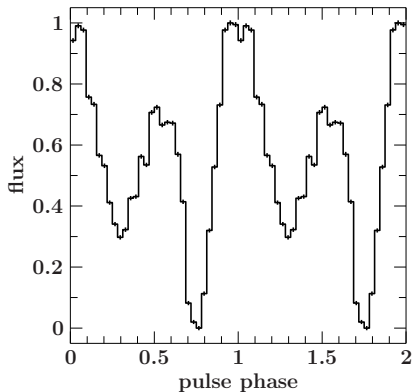
Mass: $1 - 3 M_{\odot}$

Radius: $8 - 20$ km

highly magnetized

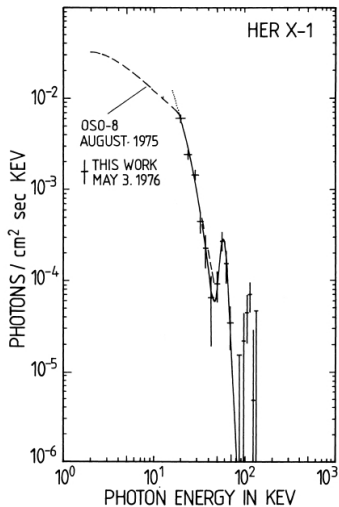
B-field: $B \sim 10^{12}$ G

Observables



(priv. comm M. Kühnel)

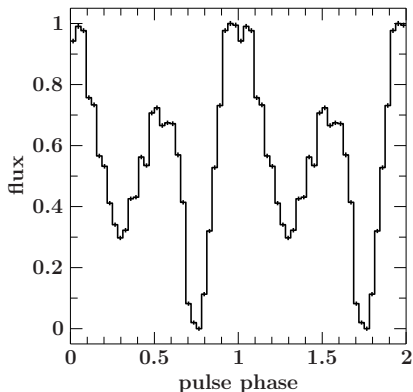
pulse profile



(Trümper et al., 1978)

cyclotron line

Modeling **pulse profiles** of **accreting neutron stars**



Tool needed which accounts for **relativistic effects** while allowing

- arbitrary geometries for the emission regions
- arbitrary emission profiles

light bending

Schwarzschild metric (spherical coordinates)

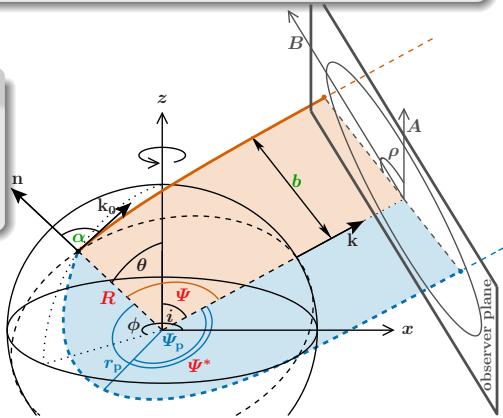
$$ds^2 = - \left(1 - \frac{2M}{r}\right) dt^2 + \left(1 - \frac{2M}{r}\right)^{-1} dr^2 + r^2 (d\theta^2 + \sin^2 \theta d\phi^2)$$

Photon trajectory to observer

$$\Psi(R) = \int_R^\infty dr \frac{1}{r^2} \left[\frac{1}{b^2} - \frac{1}{r^2} \left(1 - \frac{2M}{r}\right) \right]^{-\frac{1}{2}}$$

observed flux

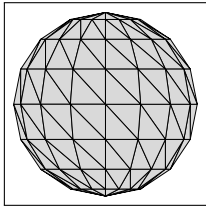
$$dF = I \cdot d\Omega(\Psi, b)$$



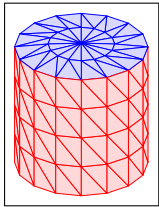
light bending

geometry

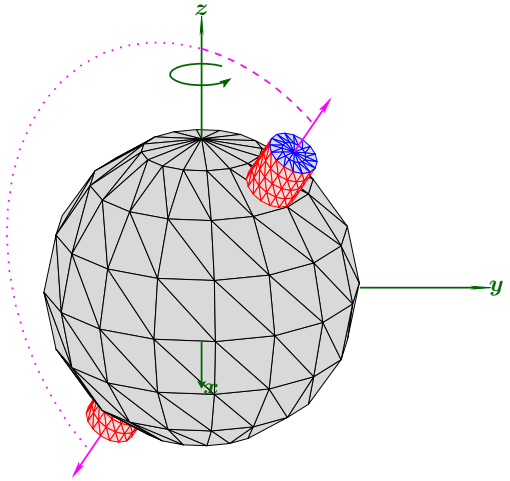
Sample geometry of the emitting surface with small surface elements



+

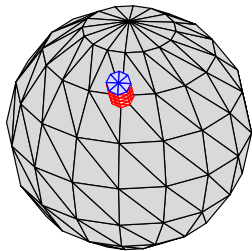


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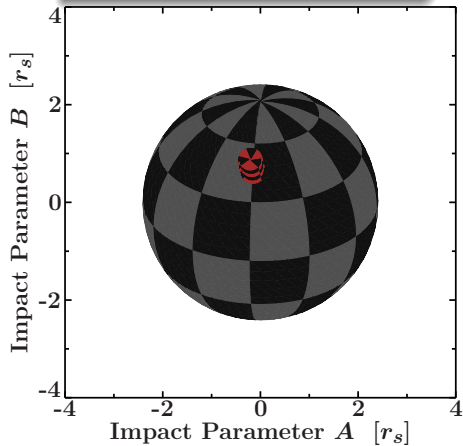


light bending

geometry



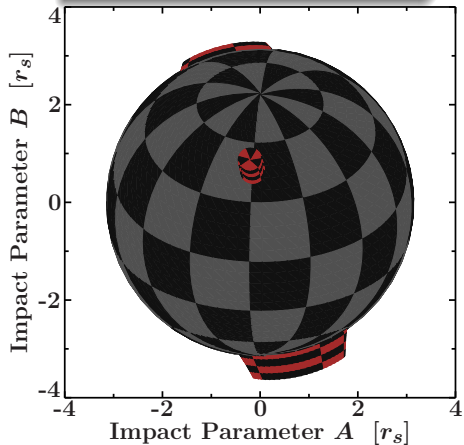
geometrical projection



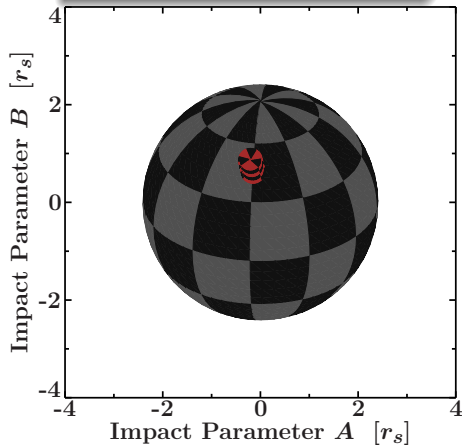
light bending

geometry

relativistic projection



geometrical projection



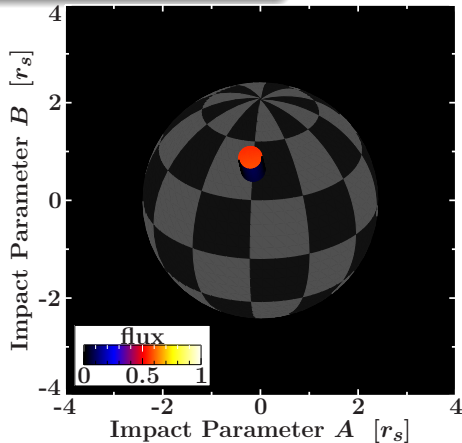
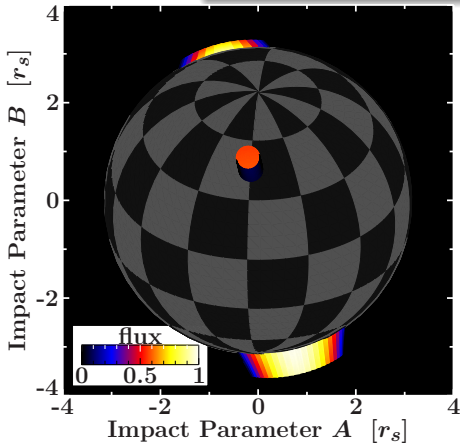
light bending

geometry



emission profile

emission profile: $I \propto 1 + 2 \cdot \cos(\gamma)$



light bending

geometry

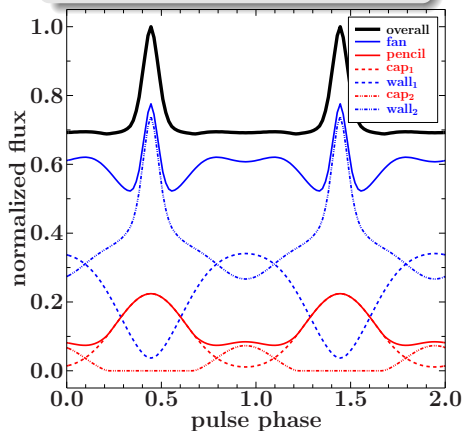


emission profile

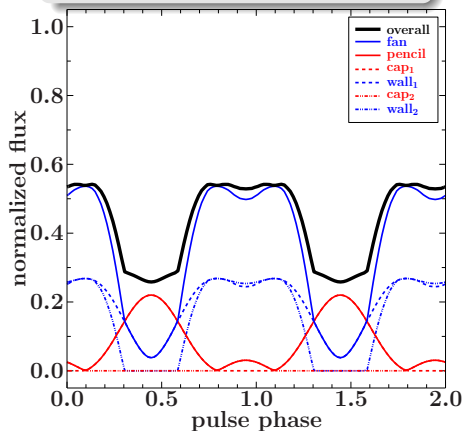


observed
flux

relativistic/geometrical case ?



relativistic/geometrical case ?



light bending

geometry

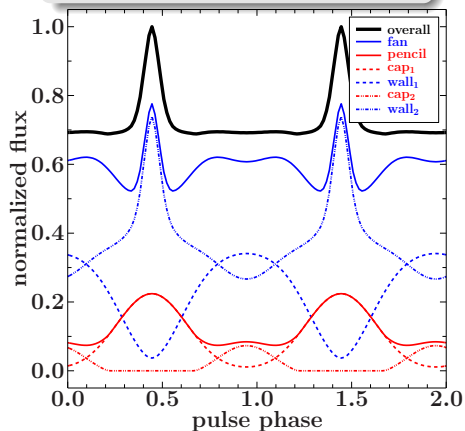


emission profile

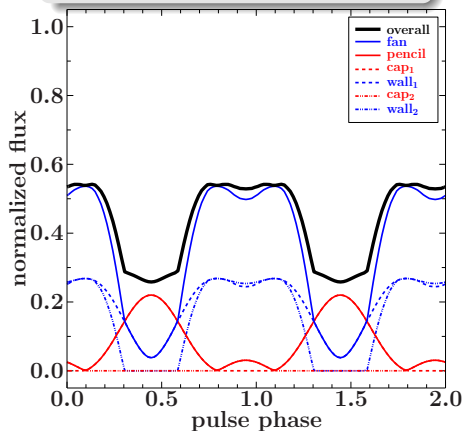


observed flux

relativistic/geometrical case !



relativistic/geometrical case !



light bending

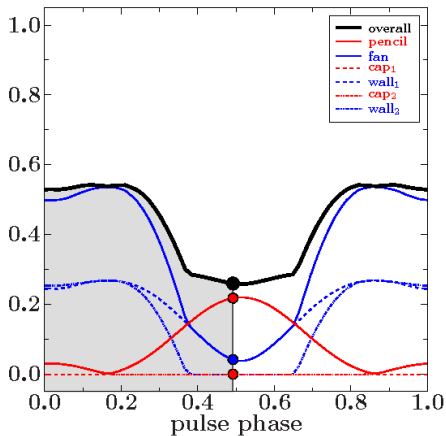
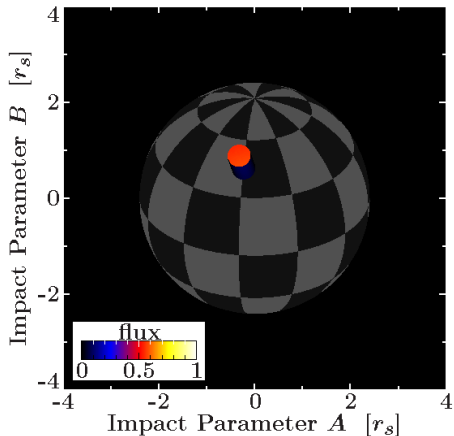
geometry



emission profile



observed
flux



light bending

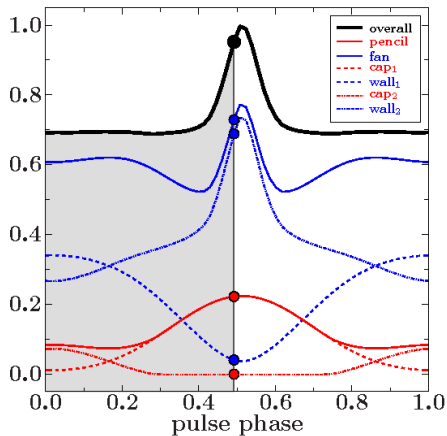
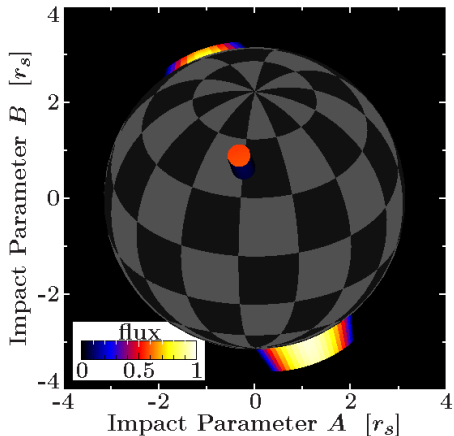
geometry



emission profile



observed
flux



light bending model

We now have a modular model to obtain the observed flux of an accreting neutron star accounting for

- relativistic effects
- arbitrary geometries for the emission regions
- arbitrary emission profile

model parameters

neutron star:

$$M_{\text{NS}}, R_{\text{NS}}, f$$

emission region, e.g.,

accretion column:

$$i_{\text{AC}_1}, \phi_{\text{AC}_1}; R_{\text{AC}_1}, H_{\text{AC}_1}$$

$$i_{\text{AC}_2}, \phi_{\text{AC}_2}; R_{\text{AC}_2}, H_{\text{AC}_2}$$

...

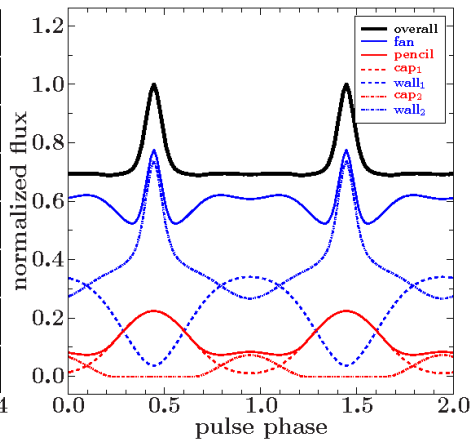
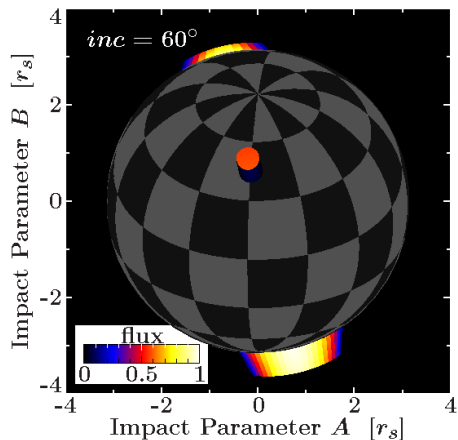
observer:

$$inc$$

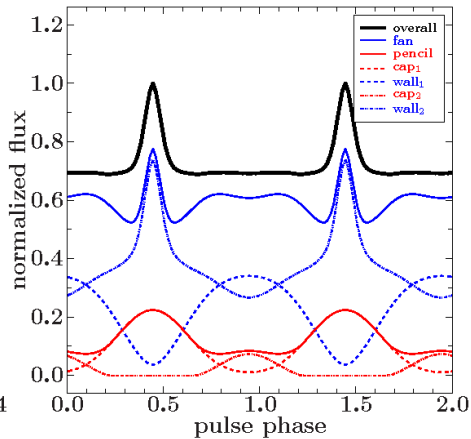
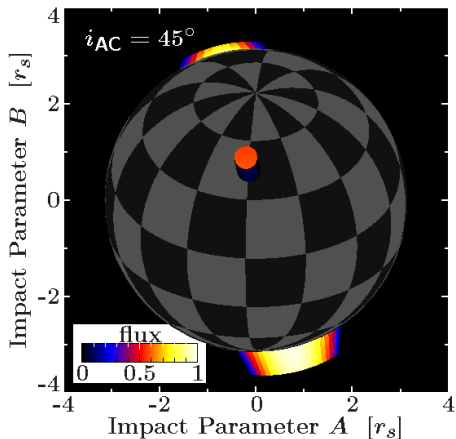
beam pattern:

$$I_E(\vec{R}, \vec{k}_0, \dots)$$

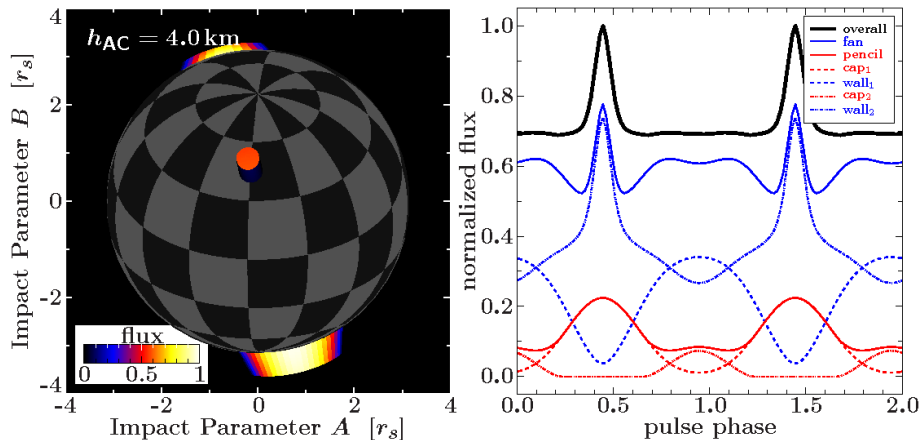
Impact of the observers inclination



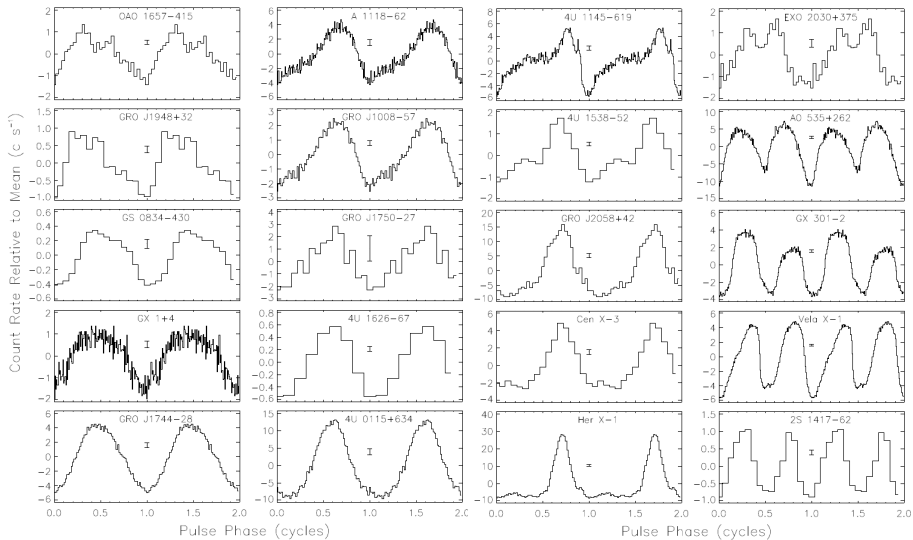
Impact of the inclination of the magnetic field



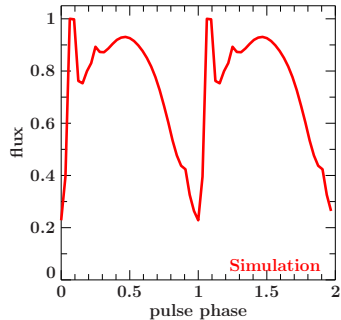
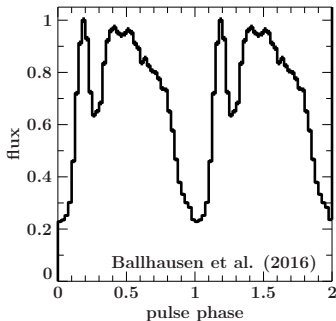
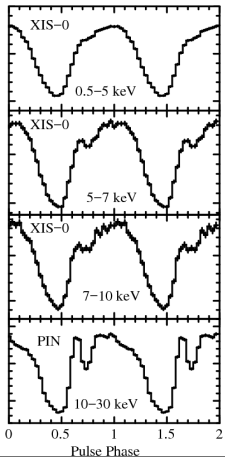
Impact of the height of the accretion column



Outlook



Pulse profile of KS 1947+300



The narrow peak can be explained with strong light bending while changes in energy relate to changes in height

References

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