

# Searching for redshifted 2.2 MeV neutron-capture lines from accreting neutron stars: theoretical X-ray luminosity requirements and INTEGRAL/SPI observations

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23 October 2024



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**SPOILER ALERT**  
only upper limits

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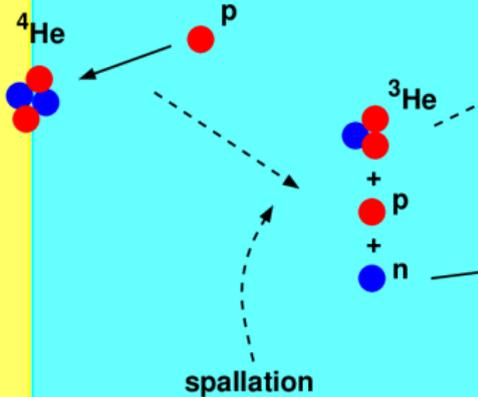
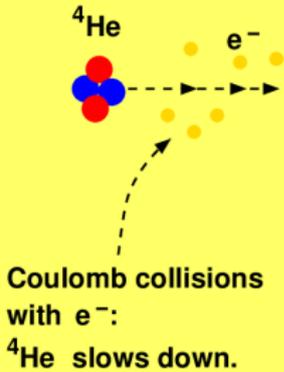


- Kinetic energy of matter falling onto a NS is  $\sim 100$  MeV/nucl.: ions can produce nuclear reactions;  $\gamma$  – rays are emitted by the star. (Schwartzman 1970).
- Neutron capture by a proton,  $n(p, \gamma)D$ , with  $\gamma = 2.223$  MeV, is observable in accreting NSs (Reina, Treves, Tarengi 1974; Brecher & Burrows 1980; Bildsten et al. 1992, 1993).

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# Path to $\gamma$ -ray production

accretion flow



- ${}^3\text{He}$  absorbs a  $n$ ;
- collision with  $p$ ;
- fusion reaction.

$p(n, \gamma), D$   
 $n$ - $p$  recombination  
 $\gamma = 2.223 \text{ MeV}$

NS

INCIDENT HELIUM DESTRUCTION CHANNELS						
SPALLATION REACTION	FRAGMENT TYPE*					
	$p$	$n$	$D$	${}^3\text{H}$	${}^3\text{He}$	
(1) ${}^4\text{He} + p \rightarrow p + n + {}^3\text{He}$ .....	...	0.40	...	...	0.82	
(1a) ${}^3\text{He} + p \rightarrow p + p + D$ .....	0.06	...	0.15	...	...	
(1b) ${}^3\text{He} + p \rightarrow p + 2p + n$ .....	0.06	0.02	...	...	...	
(2) ${}^4\text{He} + p \rightarrow p + p + {}^3\text{H}$ .....	0.28	...	...	1.00	...	
(2a) ${}^3\text{H} + p \rightarrow p + p + 2n$ .....	0.12	0.07	...	...	...	
(2b) ${}^3\text{H} + p \rightarrow n + {}^3\text{He}$ .....	-0.20	0.07	...	...	0.07	
(2c) ${}^3\text{H} + p \rightarrow D + D$ .....	-0.20	...	0.05	...	...	
(2d) ${}^3\text{H} + p \rightarrow p + n + D$ .....	...	0.07	0.05	...	...	
(3) ${}^4\text{He} + p \rightarrow D + {}^3\text{He}$ .....	-0.60	...	0.15	...	0.11	
(4) ${}^4\text{He} + p \rightarrow p + p + n + D$ .....	0.24	0.19	0.30	...	...	
(4a) $D + p \rightarrow p + p + n$ .....	0.12	0.09	...	...	...	
(5) ${}^4\text{He} + p \rightarrow p + D + D$ .....	...	...	0.30	...	...	
(5a) $D + p \rightarrow p + p + n$ .....	0.12	0.09	...	...	...	

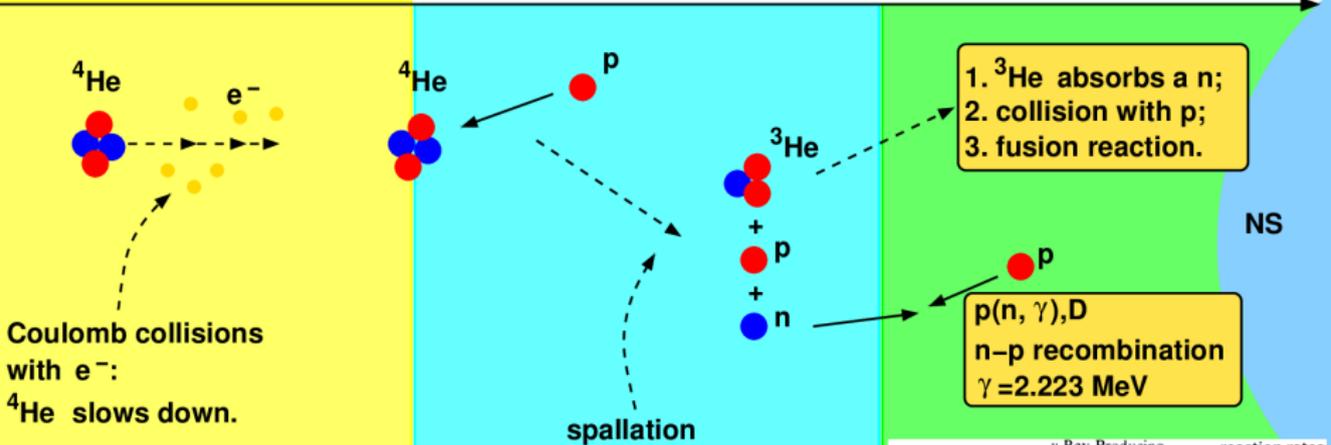
\* The entries are the fractional contribution from each reaction to the production of a particular species. These fractions were determined at an infall energy of 200 MeV nucleon<sup>-1</sup>.

$\gamma$ -Ray Producing		reaction rates
$p(n, \gamma)D$ .....	2.22	$7.3 \times 10^{-26}$
$D(p, \gamma){}^3\text{He}$ .....	5.49	$3.1 \times 10^{-27}$
${}^3\text{H}(p, \gamma){}^4\text{He}$ .....	19.81	$1.4 \times 10^{-26}$

\* Reaction rates at  $T = 10^7 \text{ K}$  in units  $\text{cm}^3 \text{ s}^{-1}$ .

# Path to $\gamma$ -ray production

accretion flow



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Detailed 2.2 MeV production mechanism in accreting NS:

- Bildsten, Salpeter, Wasserman, 1992, 1993 (Apj 384 and 408);
- Reina, Treves, Tarenghi 1974 (A&A 32, 317)

# Gravitational redshift

- Photons emitted with an intrinsic energy  $E_0$  in the atmosphere of a NS of radius  $R$  and mass  $M$  experience a gravitational redshift to  $E$ .
- Gravitational redshift  $E/E_0$  gives directly the stellar compactness:

$$\frac{R_{\text{NS}}}{M_{\text{NS}}} = \frac{2G}{[1 - (E/E_0)^2]c^2}$$

⇒ independent method to constrain the EoS.

# Line intensity

- number of 2.2 MeV photons escaping the NS atmosphere per one atom of accreted helium

- $Y$ : mass fraction of  ${}^4\text{He}$  in the accretion flow

$$F_{n,2.2\text{MeV}} = Q \cdot \frac{Y}{4} \cdot \frac{1}{E_i} \cdot F_x$$

- X-ray flux ( $F_x \approx \dot{N}_b E_i / 4\pi d^2$ )

- $E_i = GMm_p/R \approx 0.22m_p c^2$ : kinetic energy of a baryon entering the NS atmosphere

$$F_{n,2.2\text{MeV}} \sim 1.2 \times 10^{-6} \text{ ph cm}^{-2} \text{ s}^{-1} \left( \frac{Q}{10^{-2}} \right) \left( \frac{Y}{0.25} \right) \left( \frac{162 \text{ MeV}}{E_i} \right) \times \left( \frac{F_x}{3 \times 10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1}} \right)$$

(Bildsten et al. 1993)

## Observations:

Sco X-1: upper-limit:  $2.5 \times 10^{-5} \text{ ph cm}^{-2} \text{ s}^{-1}$  (COMPTEL; McConnell+1997)

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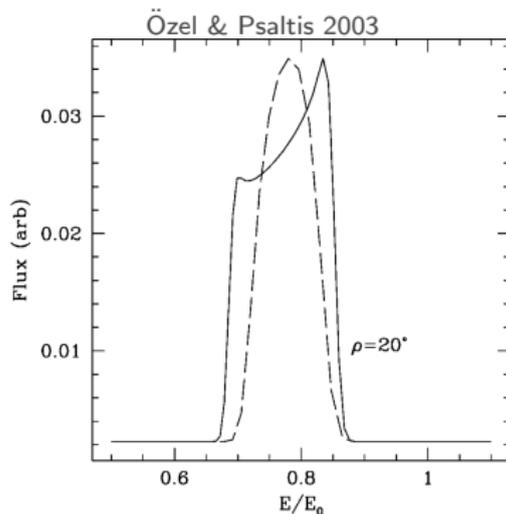
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# Relativistic effects on emission lines of NSs

Line profiles from rotating NS are affected by:

- 1 *Doppler boosts;*
- 2 *Gravitational lensing;*
- 3 *frame dragging;*
- 4 *Stellar oblateness.*

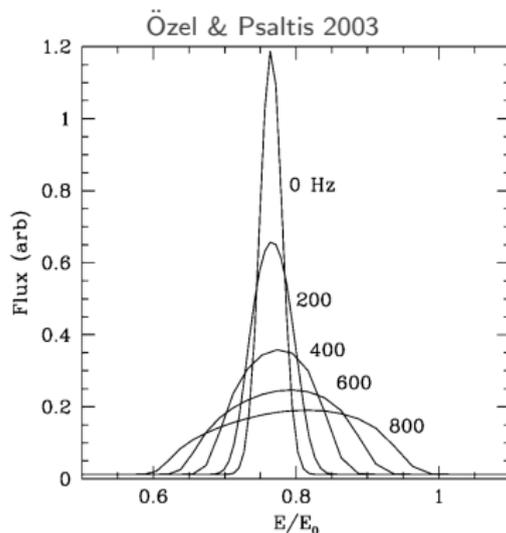


Slow rotators are best suited for searching the 2.2 MeV line (Boggs & Smith 2006; Çaliskan et al. 2009).

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# Optimal $L_x$ of an XRP for the emission of 2.2 MeV photons

- Efficiency of 2.2 MeV photon production per one  ${}^4\text{He}$  accreted, decreases as  $E_i$  becomes smaller;
- $Q \approx 0.04 \exp(-300/E_{i,\text{MeV}}^{1.1})$  (Ducci+2024)
- at high  $\dot{M}_{\text{acc}}$ , radiative force decelerates the accretion flow:  $E_{\text{kin}}$  is reduced;
- at  $L_{\text{crit}} \approx 10^{37}$  erg/s ( $B \approx 10^{12}$  G), the flow is completely decelerated ( $E_{\text{kin}} = 0$ );
- at  $L_x < L_{\text{crit}}$ :  $v \approx v_{\text{ff}} \sqrt{1 - \frac{L_x}{L_{\text{crit}}}}$
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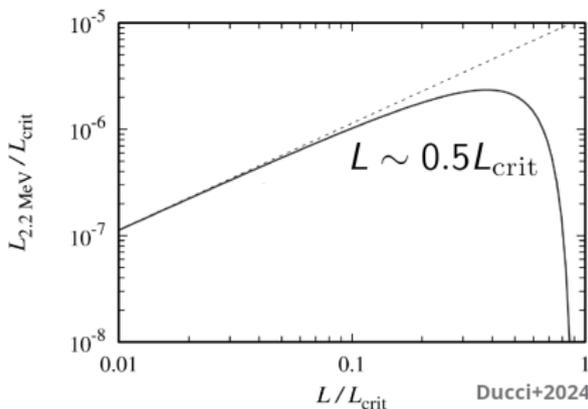
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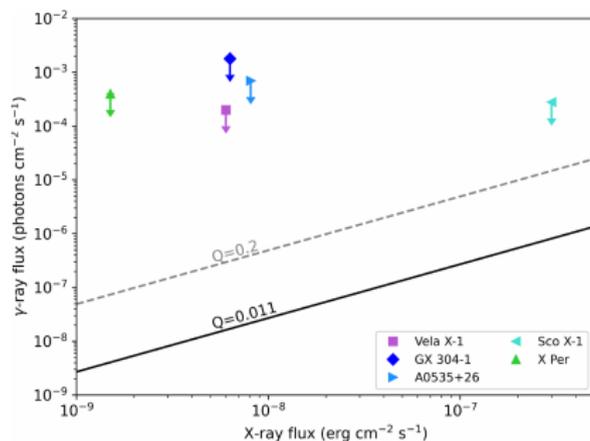
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**Fig. 1.** Expected luminosity of the 2.2 MeV line,  $L_{2.2\text{MeV}}$ , as a function of the total accretion luminosity  $L$  of an XRP. Both axes are scaled by the critical accretion luminosity  $L_{\text{crit}}$ . At low mass accretion rates and luminosity, the flux in the 2.2 MeV line is proportional to the total accretion luminosity. At high mass accretion rates, however, the radiative force decelerates the accretion flow above the NS surface, which results in a sharp drop in luminosity in the 2.2 MeV line.

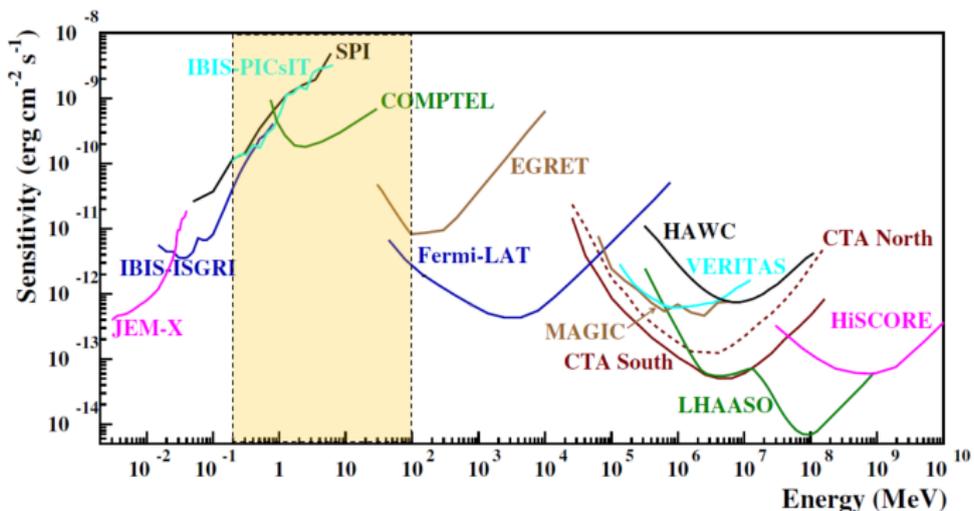
# SPI upper-limits vs expectations

Source name	net exposure (ks)	$L_x$ ( $\text{erg s}^{-1}$ )	$3\sigma$ u.l. 2.2 MeV line			
			$10^{-4} \text{ph cm}^{-2} \text{s}^{-1}$			
			FWHM: 10 20 40 100 (keV)			
A 0535+26	1631	$3 \times 10^{36}$	7.5	9.5	11	16
GX 304-1	381	$3 \times 10^{36}$	18	15	22	36
Vela X-1	5345	$3 \times 10^{36}$	2.4	3.0	3.8	7.2
X Persei	3050	$6 \times 10^{34}$	4.4	5.2	8.2	9.8
Sco X-1	4495	$\sim 10^{38}$	2.8	3.6	5.3	9.6



data analysed with: SPIDAI: <https://sigma2.irap.omp.eu/integral/spidai>

# 'MeV gap' and future MeV missions



- COSI (~ 2027; see talk by Julien Malzac on Thursday);
- COSI will achieve a  $3\sigma$  line point source sensitivity of  $2 \times 10^{-6}$  ph cm<sup>-2</sup> s<sup>-1</sup> in 1 Ms;
- concept missions: e-ASTROGAM, MASS, MeVGRO, ...

# Flux concentrating telescopes

- Smaller detector sizes → lower instrumental background;
- a viable option:  $\gamma$ -ray optics that employ the **Laue lenses**: Bragg diffraction from arrays of crystals (e.g., [Virgilli+2022a](#));
- mission concepts *ASTENA* ([Virgilli+2022b](#)); *FIONA* (IHEP)

$$E \propto \frac{F}{dr}$$

where:

- $F$ : focal length;
- $r$ : crystal distance from axis;
- $d$ : spacing of the crystal lattice planes.

*Drawbacks:*

- Technological challenges (production of crystals, mounting, alignment, ...);
  - strongly energy dependent: **high sensitivity on a limited pass-band**.
- *possible solution*: **tunable Laue lens** ([Lund 2021](#)): change  $F$  and orientation of the crystals.

