



# Planetary Terrain Analysis for Robotic Missions

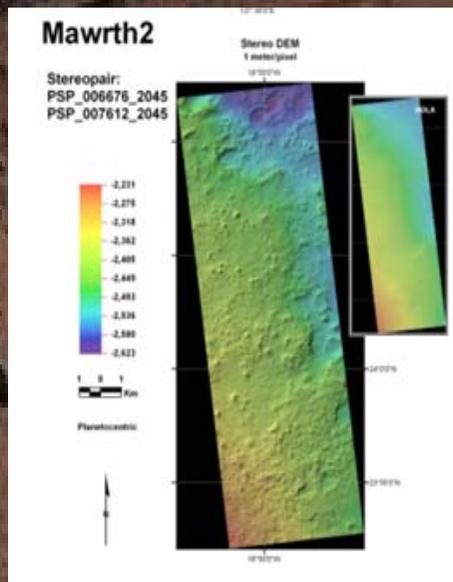
V. Masarotto, L. Joudrier, J.Hidalgo Carrio, L. Lorenzoni

- From early studies to actual design of a planetary rover mission the knowledge of the type of terrain is crucial:
  - engineering constraints for EDL are deeply related to terrain morphology,
  - rover missions need a reference terrain for design and verification of surface mobility (e.g. Navigation, distance travelled per sol).
  - Rover and landing system capabilities are both constraining the landing site selection.

# Why terrain analysis



In general knowledge *a priori* of the terrain is not possible.



# Why terrain analysis

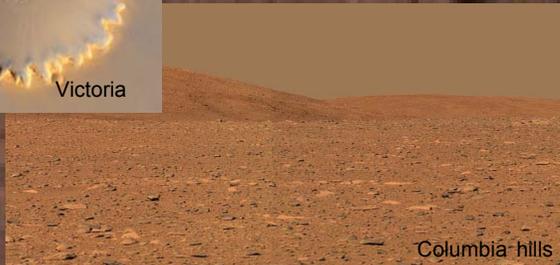
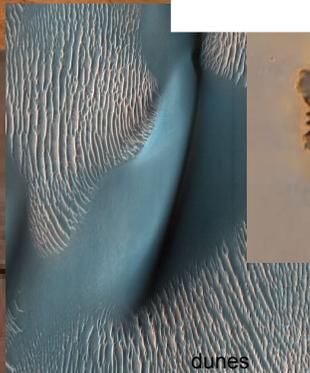


Mars presents a huge diversity of features and hazards



**Computer simulations** to support rover design

Advantages: repeatability, speed, low-cost and flexibility in the definition of parameters and constraints.



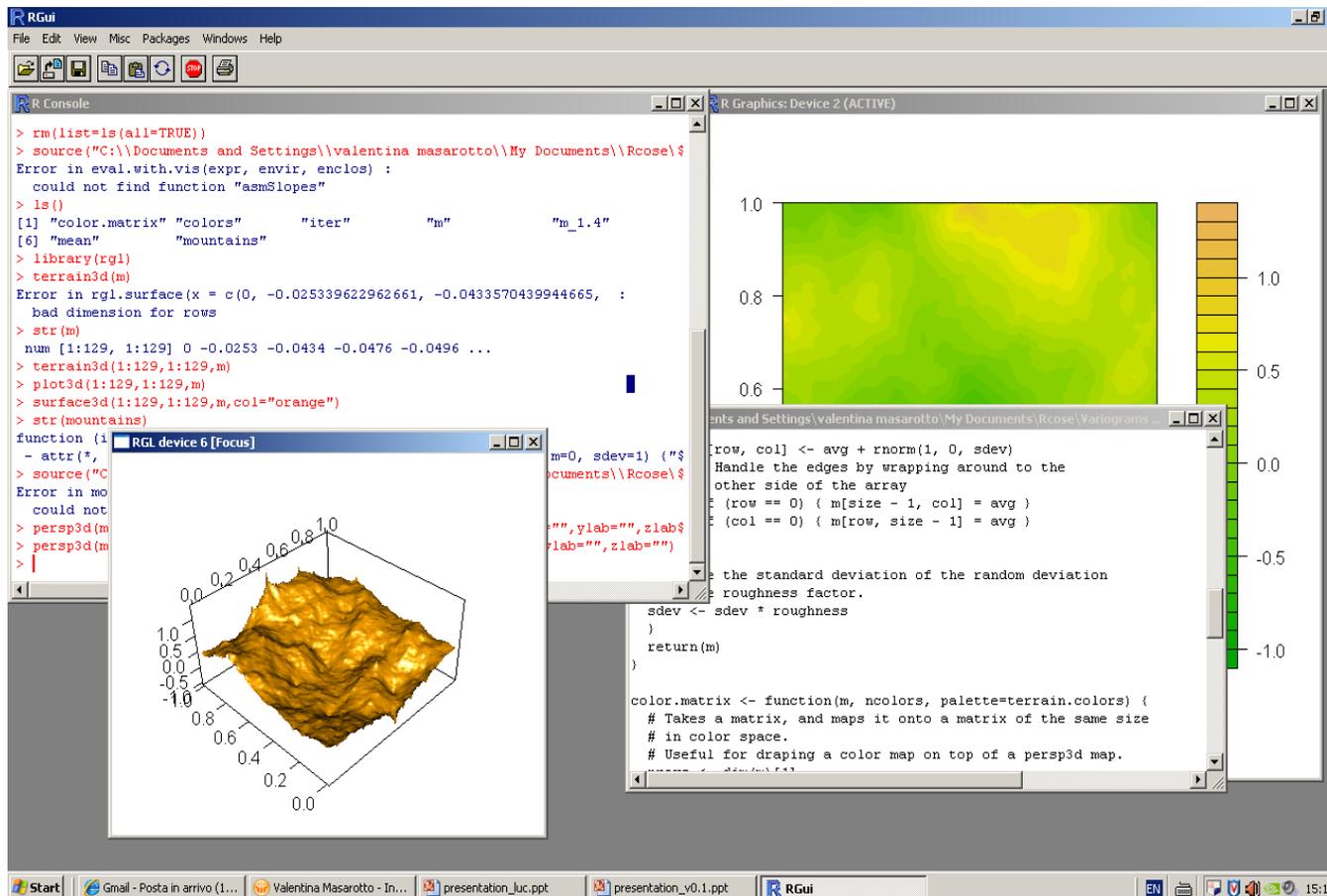
- Usually a reference terrain is given to help mission design, knowing that the actual Martian terrain will be different.
- The primary parameters which describe surfaces of a terrain given its DEMs are:
  - slopes,
  - aspects,
  - rocks.



Analysis of real terrain to deduce requirements for the reference terrain.

- Definition of the slopes computation algorithm **Adirectional Slope Method**  
+ Slopes distribution for the reference terrain.
- Brief recall on rocks distribution.
- Examples of terrain generation methods.

- All simulations have been run in the statistical environment **R**.
- Analysis of the DEMs has been done importing the geo reference files in the geographical information system **GRASS**.



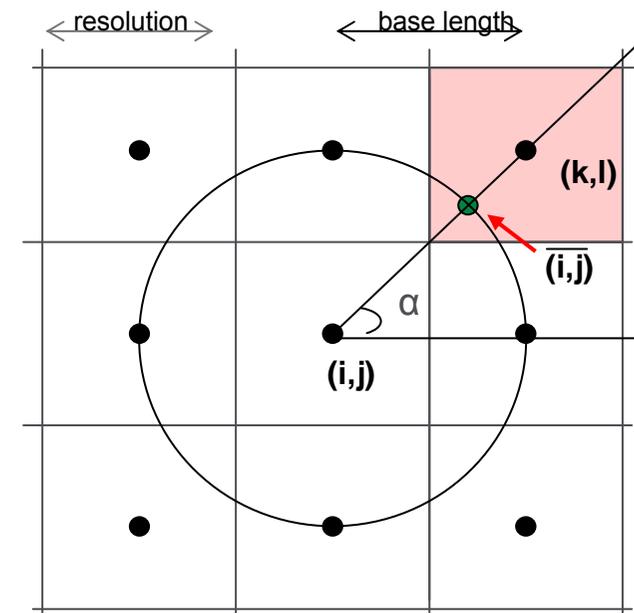
Both are  
free and  
open  
source

# ASM + terrain requirements

**Def:** The *adirectional slope* in a point is given by the absolute value of the maximum slope computed around the point, measured at a specific length scale.

## Adirectional Slope Method:

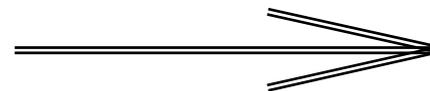
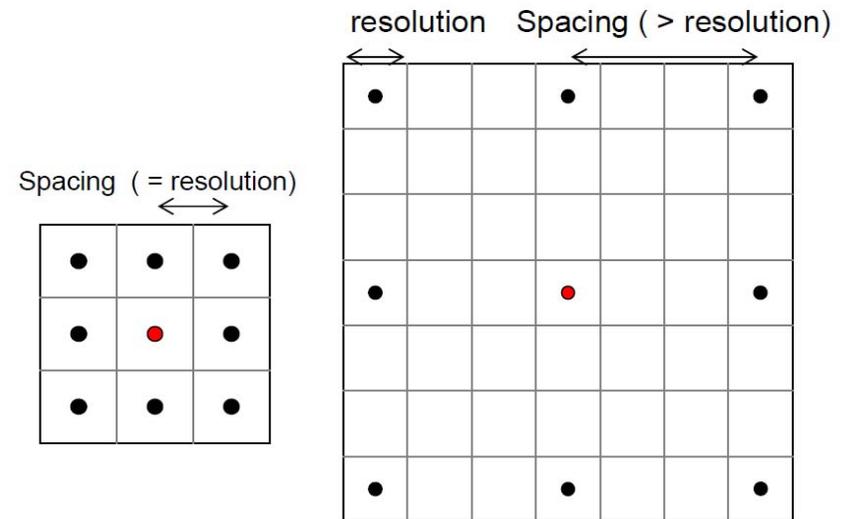
- Set a base length  $L$  and an angle  $\alpha$ .
- Consider a circle of radius  $L$  around  $P_{(i,j)}$ .
- $\alpha$  identifies  $P_{(i,j)}$  on the circle.
- Pick  $P_{(k,l)}$  as the closest DEM point to  $P_{(i,j)}$ .
- Compute the slope between  $P_{(k,l)}$  and  $P_{(i,j)}$ .
- Repeat for increments of  $\alpha$ .
- The slope in  $P_{(i,j)}$  is the maximum value.



# A similar method

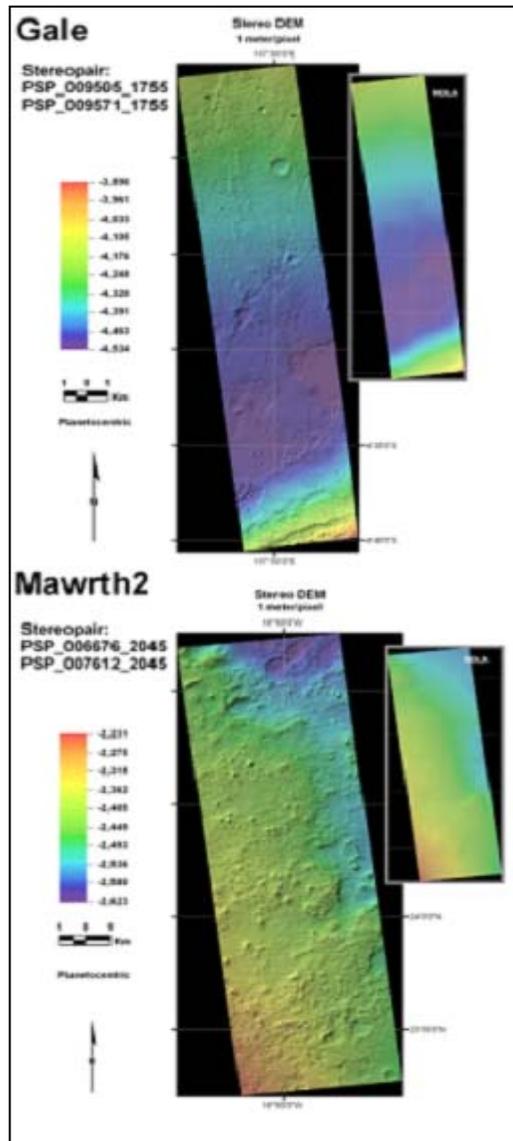
## Steepest neighbour:

- Pick the steepest of the 8 adjacent neighbours, considering the real distance on the grid.
- Equal to ASM when  $L = \text{res}$ , but limits the computation to 8 points only when  $L > \text{res}$ .

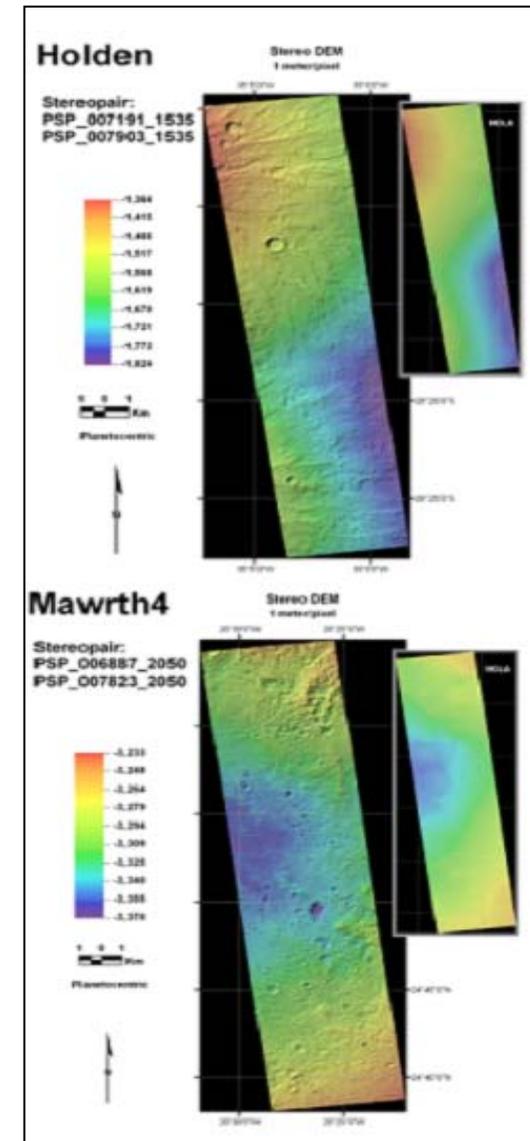


misses higher slopes

# Terrains analysis



- ASM applied to four potential landing sites for MSL to study their slopes distribution.
- DEMs from HiRISE stereo camera.
- Analysis of the DEMs is done importing the geo reference files in GRASS and then running ASM in R.



- **Goal:** define one known probability density function at specific base length that describes the slopes distribution of the four candidate landing sites.

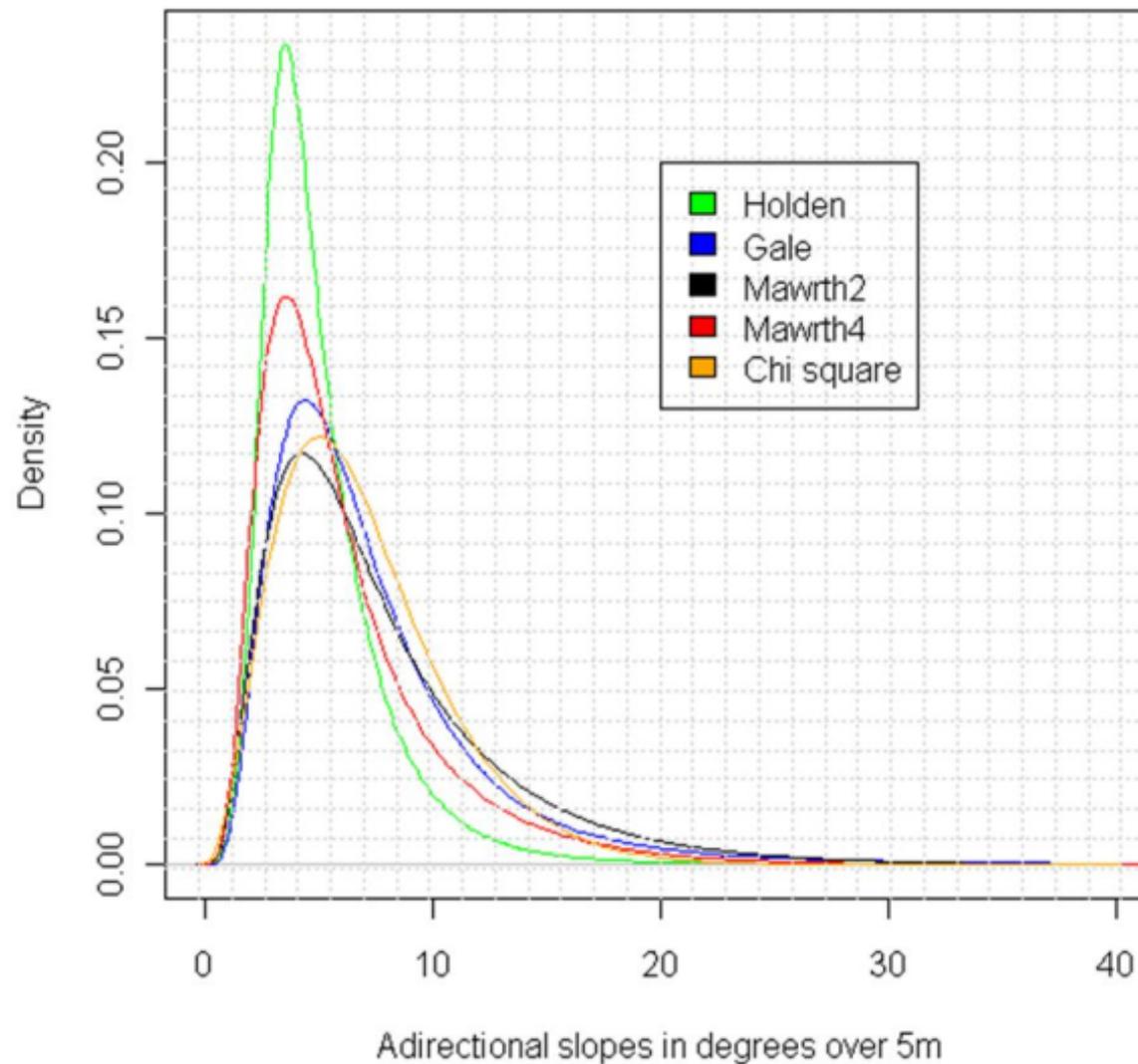


**requirements for the reference terrain**

- ESA focused on slopes computed over 5m and 100m distance.
- Assumption: over 5m the surface is flat (but inclined !)
  - ⇒ **rocks added on a second stage,  
craters not considered (avoided by rover)**

# Slope distribution over 5m

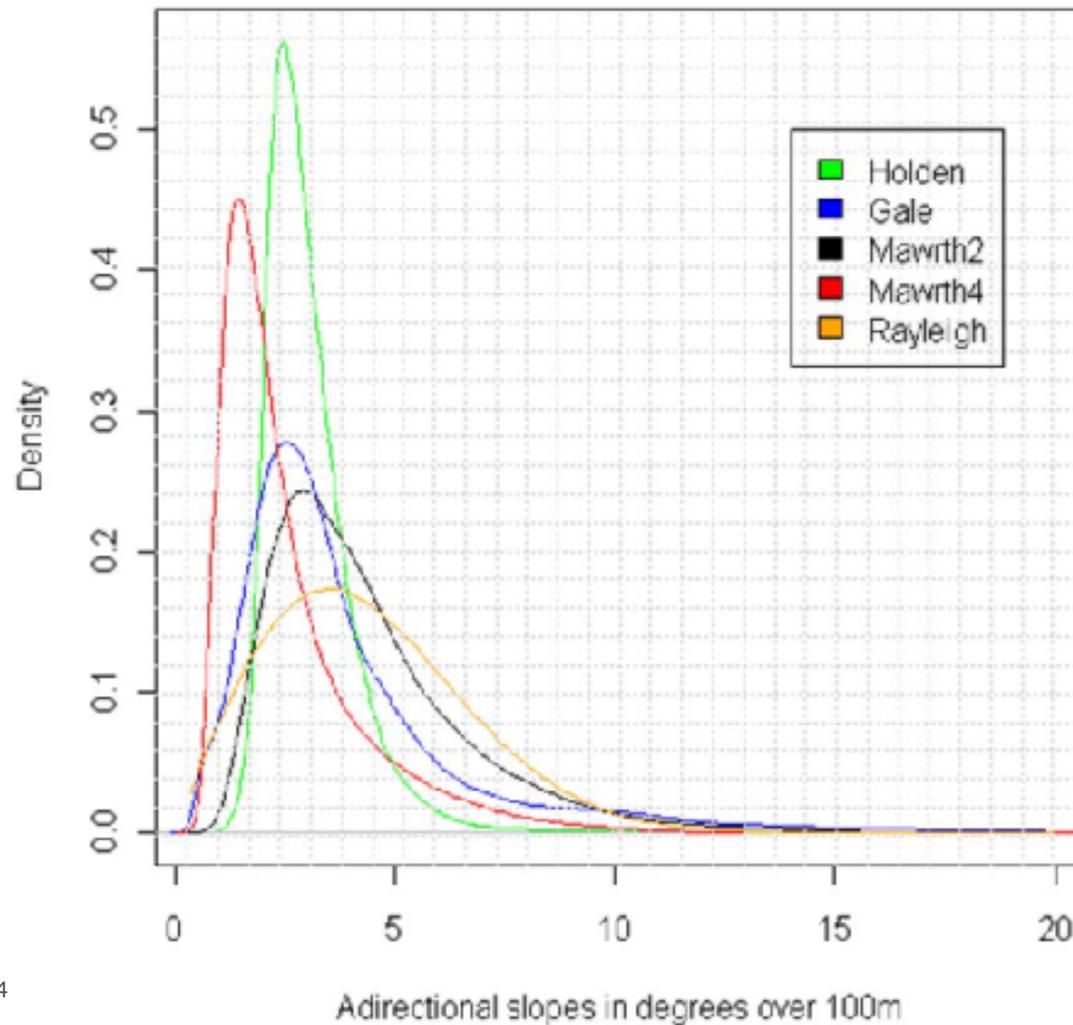
## Mars Analysis results - Adirectional Slopes



Chi square!

# Slopes distribution over 100m

Mars Analysis results - Adirectional Slopes



Rayleigh!

## Requirements for the reference terrain

5m base length:

maximum slope (99.7<sup>th</sup> percentile): 21.5°  
Chi-square distribution

100m base length:

maximum slope (99.7<sup>th</sup> percentile): 12°  
Rayleigh distribution

On top: ROCKS

# Rocks

- Golombek et Rapp  $\implies$  the size-frequency distribution of rocks could be fit with exponential functions.

- Cumulative fractional area covered by rocks of diameter greater than a given D:

$$F(D) = k \exp(-q(k) * D)$$

with

$$q(k) = 1.79 + 0.152/k;$$

$$k = 0.069 \text{ (ExoMars).}$$

- Cumulative number of rocks:

$$N(D) = \int_D \frac{F}{\text{area}}$$

- $N(D)$  is known given  $F$  and  $k$  (deterministic model). But we need a probabilistic one.
- Golombek *et al.*  $\longrightarrow$  the probability of having  $n$  rocks over a surface of area  $S$  is an **homogeneous 2-dimensional Poisson spatial process** of mean  $N*S$ , i.e.

$$p_{S,N}(n) = \frac{N^n S^n}{n!} \exp(-NS)$$

- How to generate it?  
Compute  $p_{S,N}(n)$  and scatter the points uniformly over  $S$ .



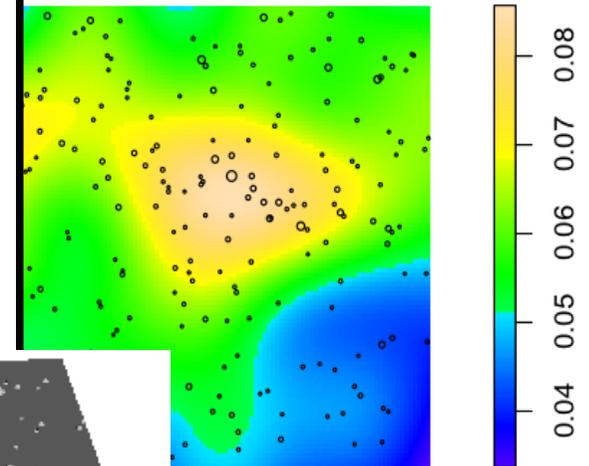
R can do it!

# On a 60x60m terrain

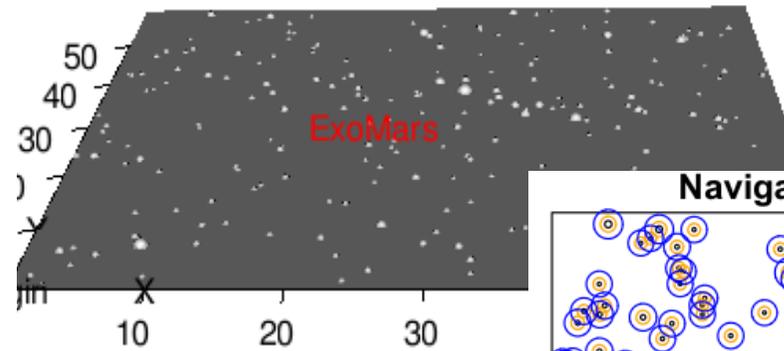
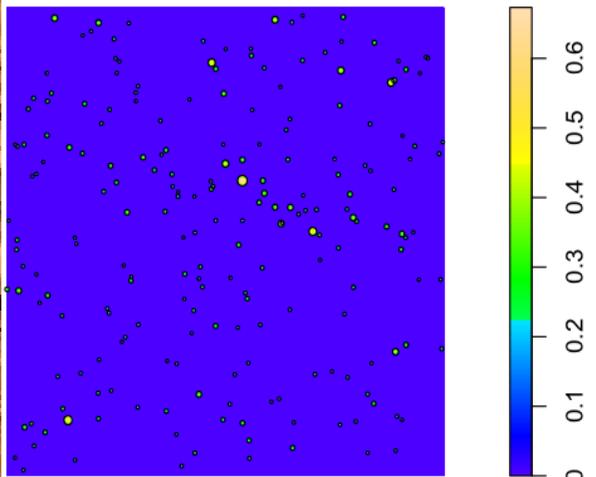


```
##### Input # General Variables #####  
k=0.069 #Percentage of area cover by rocks  
dimin = 0.4 #Minimal diameter [in meters]  
dimax = 2 #Maximum diameter [in meters]  
ratio = 0.5 #Ratio between height and diameter  
areaLength = 60 #Side of square area to generate [in meters]  
terrainResolution = 0.1 #Resolution for the DEM [in meters]  
  
#Variables for the Navigable Path Image  
navThreshold = 0.4 #rocks diameter threshold  
#The Navigation Map will be create to rock > (strict) to the navThreshold diameter value  
roverRadius = 0.8 [in meters]
```

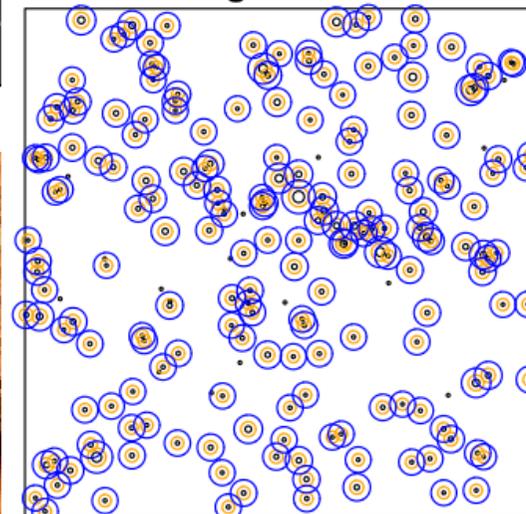
Density Map



Digital elevation rocks map



Navigable Area



# Virtual terrain

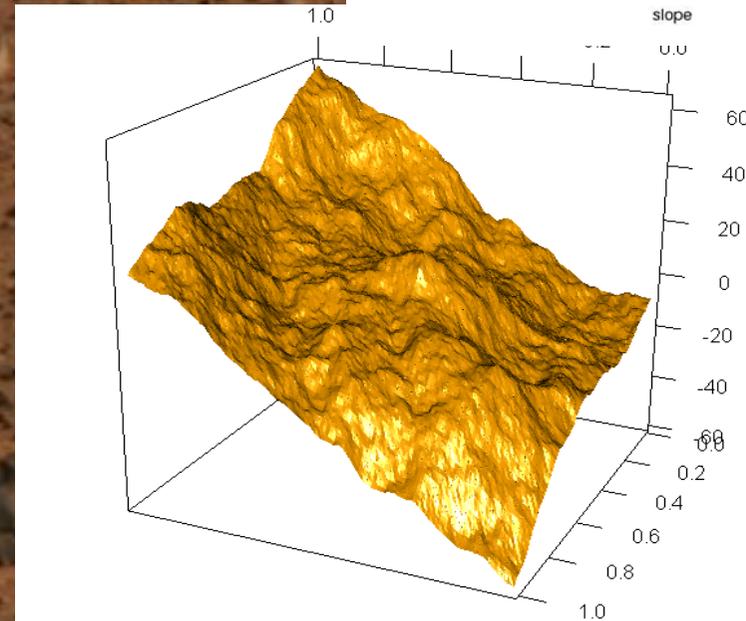
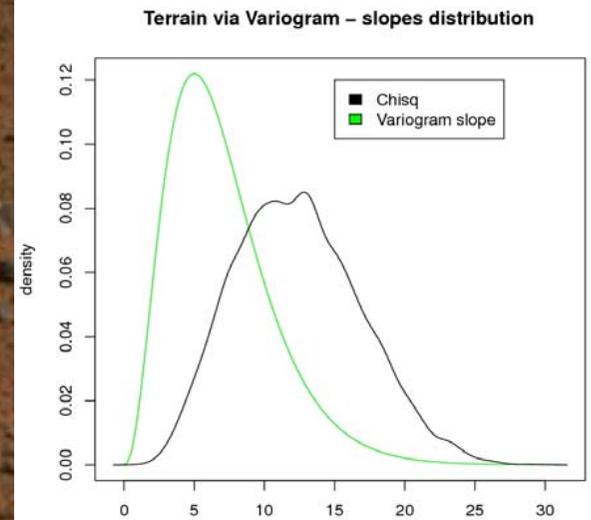
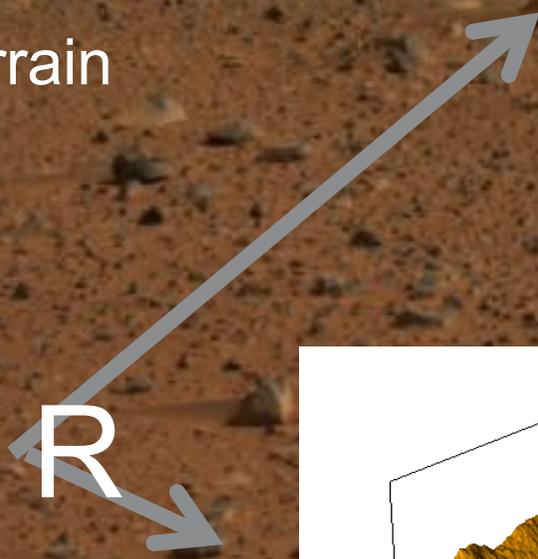
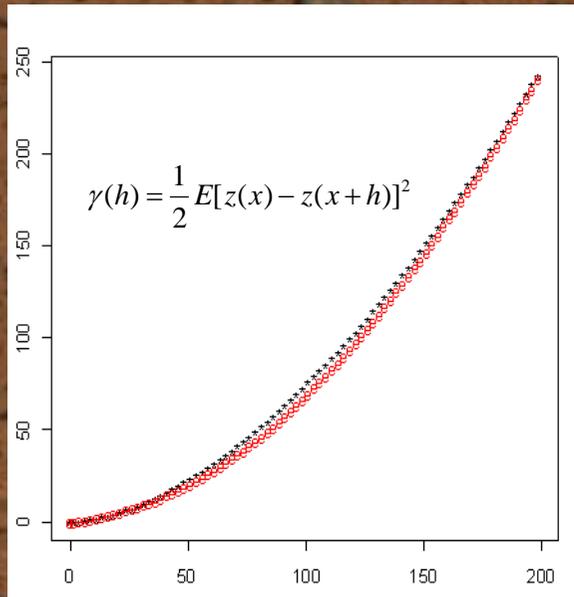
# Terrain generations



## Variogram



R on real terrain  
(Mawrth2 here)

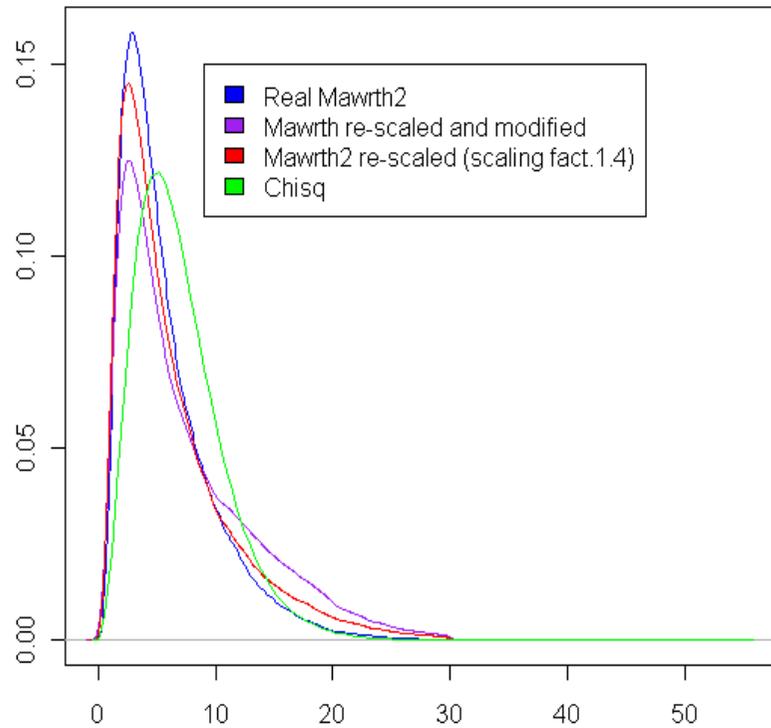


## Fractals

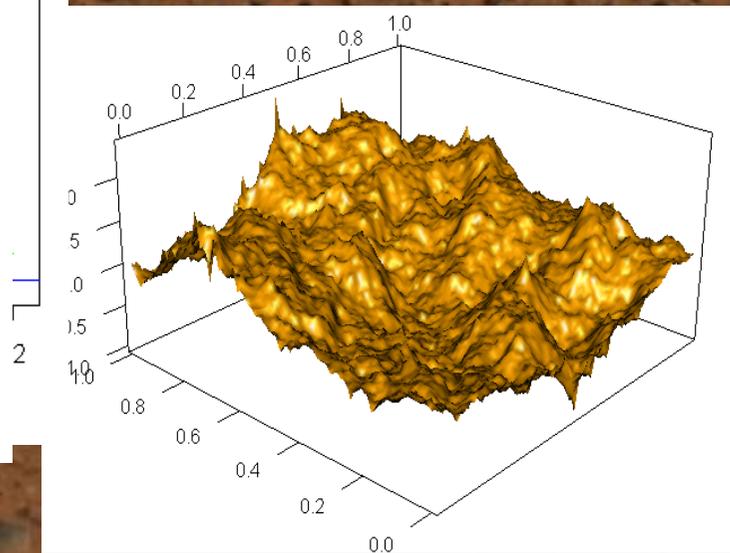
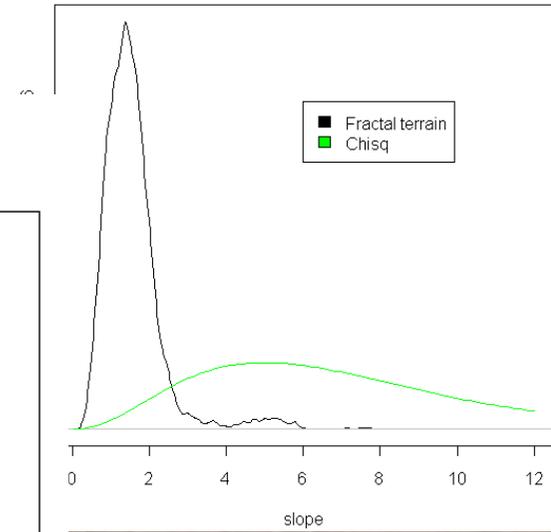


### Manual rescaling

Rescaling Mawrth2, DEM 5m Resolution

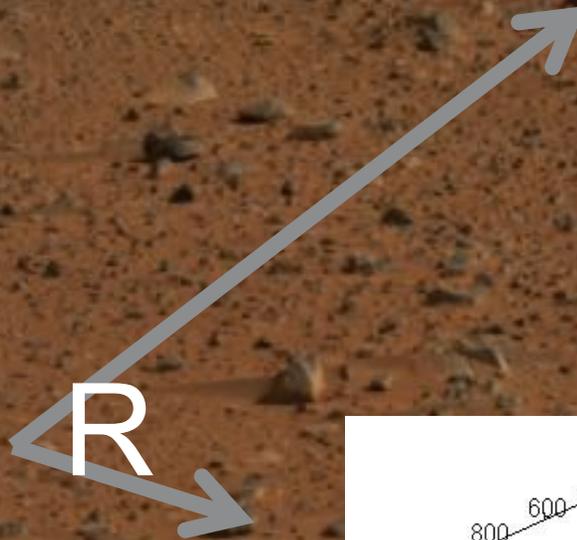
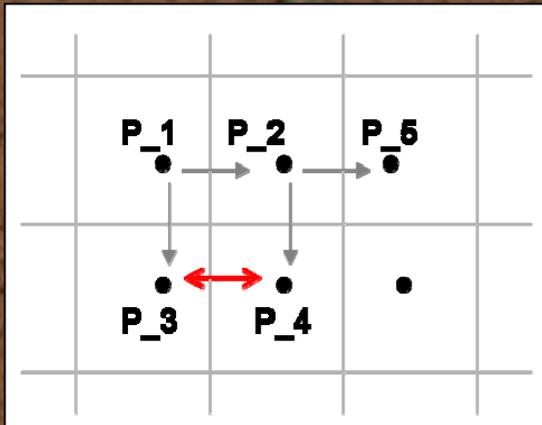


Slopes for a fractal terrain

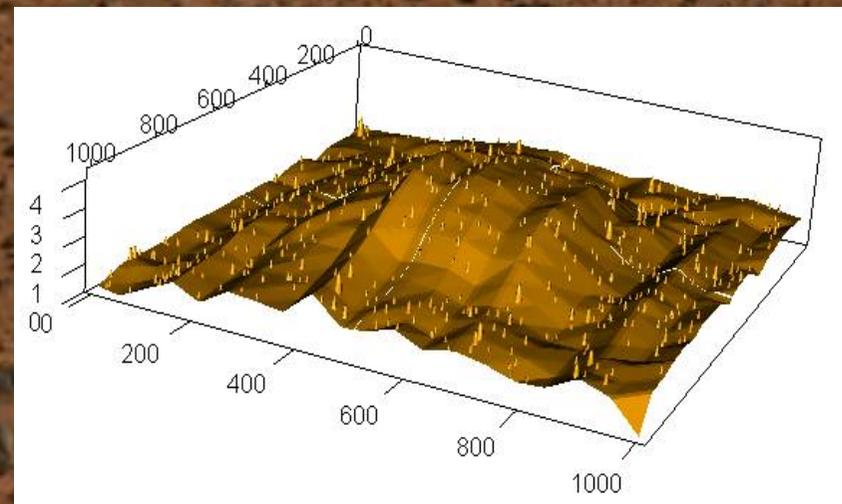
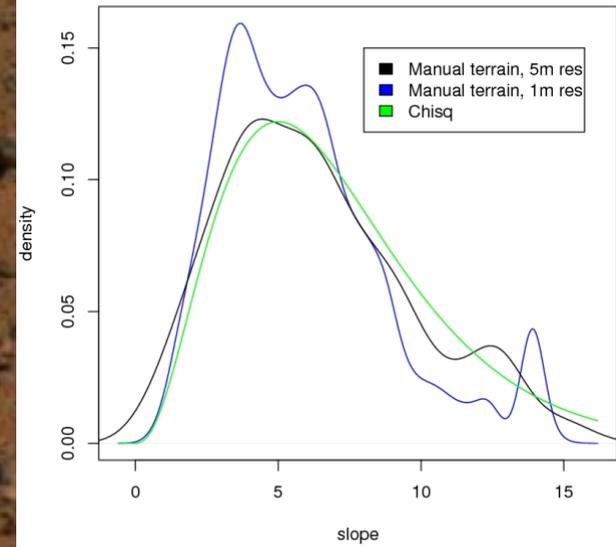


# Terrain generations

Manual terrain



Slope distribution - Manual terrain



- Introduction of ASM and its role for terrain assessment/generation.
- Extremely flexible, free, open-source softwares.
- Match between 5m and 100m requirements.
- Improve appearance of the manual terrain/ manual rescaling.
- Other generation techniques?
- Implementation for rover design.

A composite image showing the blue and white horizon of Earth on the left and the reddish, cratered surface of Mars on the right, set against a black background.

Thank you for your  
attention.