1

AN EXCEPTIONAL X-RAY VIEW OF THE YOUNG OPEN CLUSTER NGC 6231: WHAT XMM-NEWTON HAS TAUGHT US

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ABSTRACT

Considered as the core of the Sco OB1 association, the young open cluster NGC 6231 harbours a rich O-type star population. In 2001, the XMM-Newton satellite targeted the cluster for a nominal duration of about 180 ks. Thanks to the detector sensitivity, the EPIC cameras provided an unprecedented X-ray view of NGC 6231, revealing about 600 point-like sources. In this contribution, we review the main results that have been obtained thanks to this unprecedented data set. Concerning the Otype stars, we present the latest developments related to the so-called *canonical* $L_{\rm X} - L_{\rm bol}$ relation. The dispersion around this relation might actually be much smaller than previously thought. In our data set, the sole mechanism that yields a significant deviation from this scheme is wind interaction. It is also the sole mechanism that induces a significant variation of the early-type star Xray flux. In a second part of this contribution, we probe the properties of the optically faint X-ray sources. Most of them are believed to be low mass pre-main sequence stars. Their analysis provides direct insight into the star formation history of the cluster.

Key words: Stars: fundamental parameters – Stars: early-type – X-rays: individuals: NGC 6231 – X-rays: stars – Open clusters and associations: individuals: NGC 6231.

1. INTRODUCTION

Hot stars are known to be strong but soft X-ray emitters since the launch of the EINSTEIN satellite in December 1978 (Harnden et al. 1979; Seward et al. 1979). Although historically several hypotheses have been put forward to explain the origin of this X-ray emission, it is now commonly accepted that the latter is produced by shocks occurring within the denser layers of the wind. These shocks, believed to result from the growth of instabilities of the line driving mechanism, heat the wind material to temperatures of the order of ten million Kelvin, thus producing a substantial amount of soft X-ray emission. From the observational point of view, it was soon realized (e.g. Harnden et al. 1979; Long & White 1980; Pallavicini et al. 1981) that the X-ray luminosities of hot stars were related to their bolometric luminosities through the socalled *canonical* $L_X - L_{bol}$ relation. In its generic form, this relation can be written as follows:

$$L_{\rm X} \approx 10^{-7} L_{\rm bol}.\tag{1}$$

The X-ray luminosities of O-type stars seem however to present a large scatter around this relation (e.g. Berghöfer et al. 1997), typically of about a factor 2 to 3.

Beside the *intrinsic* emission of single stars, massive binaries are often more X-ray luminous compared to equivalent single stars (Pollock 1987; Chlebowski & Garmany 1991). This additional X-ray emission is usually interpreted as the signature of a wind interaction resulting either from the collision of the winds of the two stars of the system or, if the wind from one component is much stronger than the other, from the interaction of the overwhelming wind with the secondary photosphere. This Xray emission might further undergo phase-locked modulations, resulting from the variation of the absorption along the line of sight. In eccentric binaries, such phaselocked modulations might also result from the change of the shock strength due to the varying distance between the two stars.

Considered as the core of the Sco OB1 association, the young open cluster NGC 6231 hosts a rich early-type star population of different sub-spectral types and luminosity classes. Located at a distance of only about 1.6 kpc, it constitutes an ideal target to study the X-ray properties of an homogeneous (in terms of age, reddening, chemical composition, ...) sample of OB-type stars. NGC 6231 was thus chosen as the target of a 180 ks monitoring campaign performed in the framework of the Liège project for the Optical Monitor consortium guaranteed time. Carried out within a 5-day period in September 2001, the campaign actually consisted of six separate pointings of 30 ks each. Nonetheless it forms one of the deepest X-ray

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Figure 1. Combined EPIC-MOS three-color X-ray image of the young open cluster NGC 6231, showing the central part of the fov. It approximately corresponds to MOS CCD#1; the presented field is thus about $5' \times 5'$. The different false colors correspond to different energy ranges: red: 0.5-1.0 keV; green: 1.0-2.5 keV; blue: 2.5-10.0 keV. The color image is also available from the XMM-Newton Image Gallery: http://xmm.vilspa.esa.es/ external/xmm_science/gallery/public/index.php

views ever acquired of a young open cluster, but the particular schedule of the campaign further allows to study the variability of the X-ray properties of the objects on different time scales. The analysis of this remarkable data set is presented in a series of papers (Sana et al. 2005b, 2006a,b) to which we refer for further details.

Beside the XMM-Newton observations, we have also monitored all the O-type stars and some of the brightest B-type stars in the EPIC field of view (fov) by means of high resolution optical spectroscopy (mainly acquired using the ESO spectrograph FEROS). This data set has allowed us to provide further constraints on the physical properties of the early-type stars in NGC 6231 (Sana 2005). In particular, we revised their multiplicity and rederived their spectral classification. Thanks to the quality of the FEROS data, we have detected the secondary signature for eight out of the nine O-type binaries in the EPIC fov. Together with the existing photometry of the cluster (e.g. Sung et al. 1998), the tight constraints on the properties of the early-type stars provide a firm basis for the X-ray analysis. The complementarity between the X-ray and optical data further constitutes one of the strengths of the present work.

2. OBSERVATIONS AND DATA REDUCTION

XMM-*Newton* performed the six successive exposures of our campaign during satellite revolutions 319 to 321. The fov was centered on the colliding wind binary HD 152248

 $(\alpha_{2000} = 16^{h}54^{m}10$?06, $\delta_{2000} = -41^{\circ}49'30$ "1), in the core of the cluster. Position angles (PAs) were very similar through the six exposures. All three EPIC instruments were operated in the Full Frame mode together with the Thick Filter to reject UV/optical light. Due to the brightness of the cluster objects in the fov, the Optical Monitor was switched off throughout the campaign.

The EPIC Observation Data Files (ODFs) were processed using the XMM-Science Analysis System (SAS) v 5.4.1 implemented on our computers in Liège. We applied the emproc and epproc pipeline chains respectively to the MOS and pn raw data to generate proper event list files. No indication of pile-up was found in the data. We then only considered events with patterns 0-12 (resp. 0-4) for MOS (resp. pn) instruments and we applied the filtering criterion XMMEA_EM (resp. FLAG = 0) as recommended by the Science Operation Centre (SOC) technical note XMM-PS-TN-43 v3.0. For each pointing, we rejected periods affected by soft proton flares. For this purpose, we built light curves at energies above 10 keV^1 and discarded high background observing periods on the basis of an empirically derived threshold (adopted as 0.2 and 1.0 cnt s^{-1} for the MOS and pn instruments respectively). The so-defined GTIs (Good Time Intervals) were used to produce adequate X-ray event lists for each pointing from which we extracted images using x- and y-image bin sizes of 50 virtual pixels².

We finally combined the event lists obtained for all six pointings to improve the statistics of faint sources. For this purpose, we used the SAS task *merge*. For each EPIC instrument, we included the event lists resulting from different pointings one by one. We also built merged event lists that combine the twelve MOS or the eighteen EPIC event lists. The Attitude Files generated by the pipeline were merged using the same approach and we adopted, for handling the merged event lists, the Calibration Index File (CIF) and the ODF corresponding to the first pointing.

The total effective exposure times towards the cluster are, respectively for the MOS1, MOS2 and pn instruments, of 176.5, 175.0 and 147.5 ks. Together with the high sensitivity of the XMM-*Newton* observatory, the combination of the six pointings and of the three instruments provides one of the deepest X-ray views of a young open cluster. Fig. 1 shows a three-colour image of NGC 6231 and reveals a densely populated field with hundreds of point-like X-ray sources. We estimate our detection flux limit to lie between about 3×10^{-15} and 1.5×10^{-14} erg cm⁻² s⁻¹ depending on the position on the detectors and on the source spectrum.

For each source, we finally adopted a circular extraction region with a radius corresponding to half the distance

¹Expressed in Pulse Invariant (PI) channel numbers and considering that 1 PI channel approximately corresponds to 1 eV, the adopted criterion is actually $PI > 10\,000$.

²Though the physical pixels of the EPIC MOS and pn detectors have an extent on the sky of respectively $1''_1$ and $4''_1$, the virtual pixels of the three instruments correspond to an extent $0''_05$. The obtained images have thus a pixel size of $2''_5$.



Figure 2. ISM-absorption corrected X-ray luminosities in the 0.5-10.0 keV band plotted vs. bolometric luminosities. The different symbols indicate the different properties of the sources. Spectral type: O (filled symbols), B (open symbols). Luminosity class: supergiant (black), giant (red), main sequence (blue). Multiplicity: binary (triangles), presumably single RV-variable star (squares), presumably single RV-constant star (circles). Best-fit linear relations in the log – log plane for O (Eq. 2) and B (Eq. 3) stars are indicated by the dashed and the dotted lines respectively. The two vertical bars in the upper part of the graph give the expected 1- σ deviation for B (σ_B) and O (σ_O) type stars.

to the nearest neighbouring X-ray source. Due to the crowded nature of the cluster core in the X-rays and to the limited spatial resolution of the EPIC detectors, the back-ground could not be evaluated in the immediate vicinity of the stars, but had to be taken from the very few source free regions. The details are given in Sana et al. (2006a). We then used the appropriate redistribution matrix files (rmf) provided by the Science Operations Centre (SOC), according to the position of the considered source on the detectors. We built the corresponding ancillary response files (arf) using the ARFGEN command of the SAS software. The spectra were finally binned to have at least 10 counts per bin.

3. THE OB STAR POPULATION

Prior to our scientific analysis, we first went through a deep overview of the existing literature and databases on NGC 6231 and we made a census of the early-type star population in the observed fov. Our census mainly relies on selected published works (see references in Sana et al. 2005b), on the Catalog of Galactic OB Stars (Reed 2003) and on the WEBDA³ and SIMBAD⁴ databases. This re-

³http://obswww.unige.ch/webda/

⁴http://simbad.u-strasbg.fr/Simbad/

sulted in 108 objects among which 92 B-stars, 15 O-stars and one WR system (WR 79).

All the O-type stars were detected by XMM-Newton as soft but strong sources, which allowed us to study the complete population rather than a subsample of it. On the other hand, only about 20% of the B-type stars could be associated with an X-ray source. Using the XSPEC software, we adjusted the X-ray spectra of the different sources associated with early-type objects. In doing so, we used up to three-component thin thermal plasma models (mekal models) allowing for a distinct local absorption column (wabs model) for each component and accounting for additional absorption by the interstellar medium (ISM). The latter column was held fixed to a value computed from the reddening of the different objects, using the typical colours of Schmidt-Kaler (1982) and the gas to dust ratio of Bohlin et al. (1978). Using the best-fit models, we finally computed the X-ray luminosities, corrected for the ISM absorption column only. We also recomputed the bolometric luminosities, adopting our revised spectral classification and the bolometric correction scale of Schmidt-Kaler (1982). Fig. 2 presents the location of the different objects in the $L_{\rm X} - L_{\rm bol}$ diagram. Note that Fig. 2 is restricted to objects fitted with at least 2-temperature mekal components. Reasons for this are given in Sana et al. (2006a).

3.1. The O-type stars

Focusing in a first step on the O-type stars, we note a clear linear relation in the $\log - \log$ plane. However several points deviate significantly from this canonical relation. HD 152248 (O7.5III(f) + O7III(f), Sana et al. 2001) presents clear evidence for a wind-wind interaction that we traced both from the optical and X-ray domains. 2-D hydrodynamical simulations of the collision further reasonably reproduce the observed modulations of the Xray flux of the system, lending further support to this interpretation (Sana et al. 2004). CPD-41°7742 (O9V + B1.5V, Sana et al. 2003) X-ray light curve also displays clear though apparently complex modulations of its X-ray flux, that we have however related to a wind interaction of a peculiar kind. In this O+B system, the dominant primary wind most probably crashes into the secondary surface. A simple phenomenological model of such a windphotosphere interaction indeed reproduces pretty well the main features of the X-ray light curve (Sana et al. 2005a). It is thus clear that the two latter systems are not representative of the intrinsic X-ray emission of single O-type stars. Excluding these two points, a least-square linear fit yields:

$$\log L_{\rm X} - \log L_{\rm bol} = -6.912(\pm 0.153) \tag{2}$$

where the X-ray luminosity is given in the 0.5-10.0 keV band. It is interesting to note that we also adjusted a power-law relation (thus in the form $\log L_{\rm X} = \Gamma \times \log L_{\rm bol} + K$). However, as indicated by a F_{χ} -test (see e.g. Bevington 1969), this additional parameter does not improve significantly the quality of the fit compared to



Figure 3. Hertzsprung-Russell diagram of the EPIC sources with optical counterparts in the Sung et al. (1998) catalogue. Evolutionary tracks from Siess et al. (2000) for masses of 0.2, 0.3, 0.4, 0.5, 0.7, 1.0, 1.5, 2.0, 2.5, 3.0, 4.0, 5.0, 6.0 and 7.0 M_{\odot} are overplotted. Filled dots, filled diamonds and open triangles indicate respectively $H\alpha$ emitting stars, $H\alpha$ candidates and stars with no evidence for emission. The thick solid line shows the ZAMS, while the dashed lines correspond to isochrones for ages of 0.5, 1.5, 4.0, 10.0 and 20.0 Myr.

the scaling law of Eq. 2. In the following, we thus decide to adopt the simplest form of the canonical relation, as quoted in Eq. 2. One of the most outstanding results lies however in the limited dispersion (of only about 40%) of the X-ray luminosities around the best fit relation. Compared to the scatter (a factor of 2 to 3) observed by Berghöfer et al. (1997), this suggests that the intrinsic X-ray emission of O-type stars might be much more constrained by the physical properties of the star than previously assumed. It is also remarkable that, within our sample, only the binaries present a significant modulation of their X-ray flux, suggesting thus a wind interaction origin. Excluding the case of HD 326329, probably contaminated by a neighbouring flaring source, extra emission produced in a wind interaction region is also the only mechanism that yields a significant deviation from the canonical $L_{\rm X} - L_{\rm bol}$ relation. All in all, our analysis suggests thus that the intrinsic X-ray emission from single O-type stars might be rather stable, both in terms of time-variability and of scattering compared to the mean $L_{\rm X} - L_{\rm bol}$ relation.

3.2. The B-type stars

Turning to B-type stars, their distribution in the $\log L_{\rm X} - \log L_{\rm bol}$ plane also suggests the presence of a linear relation, although as quoted above, only about 20% of these objects are seen in the X-rays. Indeed the linear correlation coefficient is $r \sim 0.75$, corresponding to a confi-



Figure 4. Distribution of the ages of X-ray selected PMS objects as interpolated from the isochrones derived from the Siess et al. (2000) evolutionary tracks. PMS candidates with $\Delta(R - H\alpha) \ge 0.12$ are indicated by the solid line, while those with $\Delta(R - H\alpha) < 0.12$ are indicated by the dashed line. The total numbers of objects with $\Delta(R - H\alpha) \ge 0.12$ and $\Delta(R - H\alpha) < 0.12$ are respectively 93 and 303.

dence level of 0.99 in favour of the presence of a correlation between $\log L_{\rm X}$ and $\log L_{\rm bol}$. A linear least-square fit yields:

$$\log L_{\rm X} = 0.22(\pm 0.06) \log L_{\rm bol} + 22.8(\pm 2.4) \tag{3}$$

However, we emphasize that the undetected B-type stars were not taken into account in the derivation of the present relation. The fact that about 80% of them lie below our detection threshold suggests that either X-ray emission from B-type stars is not an intrinsic property of such stars or, at least, that it is not fully governed by their bolometric luminosities. In the latter case, we could only be detecting the upper envelope of a largely scattered distribution in such a way that, by coincidence, the detected sources suggest the presence of a linear relation. Beside these considerations, one may further note that about one third of the detected B sources present flaring-like activities during the time-span of our XMM-Newton campaign. Their X-ray spectral properties are further reminiscent of those of PMS stars. It is therefore difficult to definitely conclude whether the detected X-ray emission is directly associated with the B-type stars or if it is rather produced by PMS stars either as the secondary component in a binary system or being located by chance along the same line of sight.

4. THE OPTICALLY FAINT X-RAY SOURCES

Beside the early-type stars, the EPIC images reveal several hundreds of additional point-like sources that clus-



Figure 5. Locations of the NGC 6231 O-type stars in the H-R diagram. Symbol shapes and colours provide different indications on the object nature: black, supergiant; red, giant; blue, main sequence; triangle, belonging to a binary system (filled triangles indicate the heaviest star of the system while open triangles stand for the less massive companion); square, presumably single, RV-variable star; circle, presumably single, constant-RV star. The evolutionary tracks from Schaller et al. (1992) have been plotted (plain lines) together with isochrones (dotted lines) computed for ages ranging from 2 to 10 Myr with a step of 2 Myr. The figure appears in colour in the electronic version of this work.

ter towards the core of NGC 6231, suggesting a physical link with the cluster. These are typically fainter but harder than the O-type stars (Sana et al. 2005b). As a first step, we compared the X-ray source list with different existing optical/IR catalogues, adopting a limited crosscorrelation radius of 3". As a result, almost 80% of the Xray sources in the XMM-Newton fov could be associated with at least one optical/IR counterpart. In particular, we made use of an extended version of the UBV(RI)_C $H\alpha$ photometric catalogue of Sung et al. (1998). Roughly, the latter work covered a square field of $20' \times 20'$ that is inscribed within the 15' radius fov of the EPIC cameras. NGC 6231 being a quite young open cluster (age~3-5 Myr, Baume et al. 1999), we expect that the lower mass stars have not reached the ZAMS yet. Being probably still embedded in their natal clouds, they might suffer a heavy circumstellar absorption. X-ray emission is however one of the best selection criteria for these objects (Sung & Bessell 2004) and the present XMM-Newton image of NGC 6231 might form one of the best censuses of the cluster PMS population so far. $H\alpha$ emission is a further well known property of the classical T Tauri stars. Among the 536 X-ray sources located within the field covered by the Sung et al. (1998) catalogue, we indeed identified 93 candidates displaying a significant excess in the $R-H\alpha$ colour index (adopted as $\Delta(R-H\alpha) > 0.12$, see Sana et al. 2006b, for details).

5

Fig. 3 presents the location of these optically faint Xray sources in the Hertzsprung-Russell diagram. Most of them are indeed located above the ZAMS as expected for PMS objects. Comparing with PMS evolutionary tracks of Siess et al. (2000), it appears that most of them are low-mass stars ($M < 2 M_{\odot}$) that started their formation about 2 to 4 Myr ago. The distribution of the ages of these X-ray selected PMS stars is presented in Fig. 4 and suggests that star formation in NGC 6231 might have started at least 10 Myr ago at a relatively slow rate. The latter then slowly increased to culminate in a starburstlike event about 2 to 4 Myr ago, a period that also corresponds to the formation of the cluster massive stars (see Fig. 5). It is further interesting to note that, neither in Figs. 3 nor 4, a clear difference appears between the H α emitting X-ray sources (probably classical T Tauri stars) and those that do not present evidence of such emission (probably weak-line T Tauri stars). No difference could also be found in their respective spatial distribution in the studied fov.

5. CONCLUSIONS

We briefly presented some of the main achievements of an XMM-Newton monitoring campaign of the young open cluster NGC 6231 in the Sco OB1 association. Of a nominal duration of 180 ks, it was actually split into 6 separate pointings spread over 5 days. Clearly it constitutes one of the deepest X-ray observations of a young open cluster and its particular scheduling allowed us to probe the variability of the detected sources on different time scales. The EPIC cameras revealed a crowded fov with more than 600 X-ray sources. The large majority of these could be identified with an optical/IR counterpart and their location in the H-R diagram suggests that most of them are actually low-mass ($M < 2 M_{\odot}$) PMS stars. Their study seems to indicate that the star formation in NGC 6231 was probably not an instantaneous event but might have started at least 10 Myr ago at a relatively slow rate. The bulk of the cluster stellar population has however started its formation during a starburst-like event about 2 to 4 Myr ago, an epoch during which the most massive stars of the cluster were also formed.

XMM-Newton also detected the complete O-type star population in the EPIC fov. Being strong but soft emitters, these objects clearly dominate the EPIC images. Restraining our analysis to the 0.5-10.0 keV band, we derived a new value for the $L_X - L_{bol}$ canonical relation, expressed in the form of a scaling law. One of the most outstanding results is the limited dispersion of the O-type star X-ray luminosities around this new canonical relation compared to the one observed by previous studies. It is clear that the fact that we have been able, among others, to identify and reject the colliding wind binary systems from the fit has helped to reduce the scattering. The particular homogeneity of our sample, notably in terms of age, metallicity and reddening, might have played a crucial role in this regard. Finally, it is also worth to note that, within our sample, variability of the X-ray flux is only observed for probable colliding wind binaries. It is further the only mechanism that seems to produce strong deviations from the *canonical* relation. All in all, our analysis suggests thus that the *intrinsic* X-ray emission from single O-type stars might be much more stable than previously thought, both in terms of time-variability and of deviation from the mean $L_{\rm X} - L_{\rm bol}$ relation.

The comparison of the present results with others, derived in an homogeneous way from the study of other young open clusters, will therefore be of particular interest to probe the *universality* of the *canonical* relation. It could further help to investigate the influence of other important parameters, such as age and metallicity, which might crucially affect the *intrinsic* X-ray emission of O-type stars.

Finally we note that, compared to XMM-*Newton*, future X-ray missions should definitely combine a high sensitivity with an increased spatial resolution. The latter is indeed crucial in very crowded fields such as the one studied in this contribution. We also note that, while dealing with such an extended data set, 12 months is a very short time. One can thus wonder whether the proprietary policy could not be extended to allow scientists to perform in-depth studies in good conditions.

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