

Towards a theoretical determination of the geographical distribution of meteoroids impacts on Earth

Jorge I. Zuluaga* & Mario Sucerquia

*Solar, Earth and Planetary Physics Group, SEAP
Universidad de Antioquia*

** jorge.zuluaga@udea.edu.co*

Solar, EAarth & Planetary Physics



Meteoroids 2016
6-10 June, Noordwijk (NL)



Are impacts on Earth spatially (and/or temporarily) uniform?

Jorge I. Zuluaga* & Mario Sucerquia

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Meteoroids 2016
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Where could be the next Chelyabinsk?

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5-10 June, Noordwijk (NL)





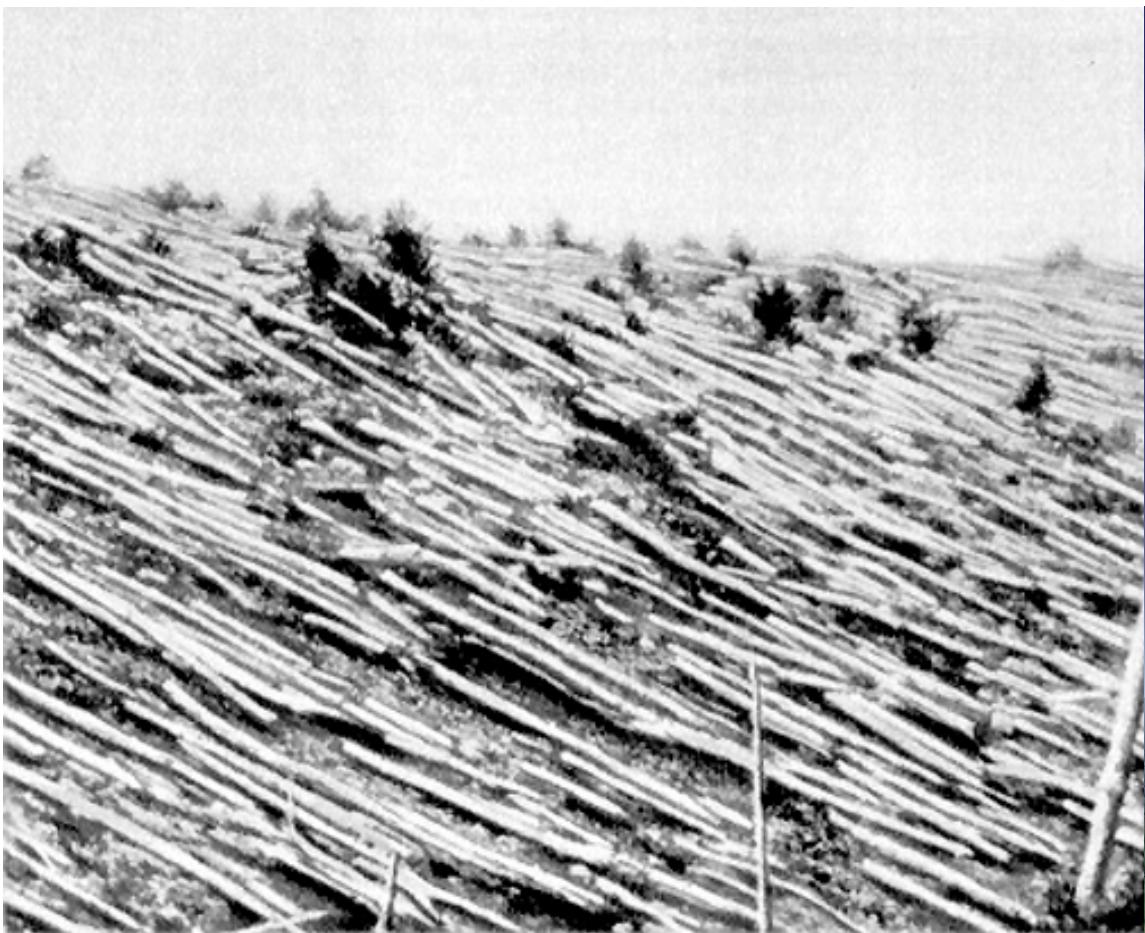
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30 Junio, 1908, ~ 7:14 a.m. LMT



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15 February, 2013, ~ 9:20 a.m. LMT



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Where did they happen?...



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Probability 2 independent events (similar type)
~2,400 km away (uniform distribution)

$$p \sim 0.8\%$$



Probability of having event pairs separated by more than 2,400 km after N impacts is

$$P = (1-p)^N$$

Expected number of events before having at least 1 spatial coincidence:

$$\langle N \rangle = 1/p \sim 100$$

Assuming a mean periodicity of ~40 years for Chelyabinsk-like events we need to wait ~40,000 years to see similar spatial coincidence

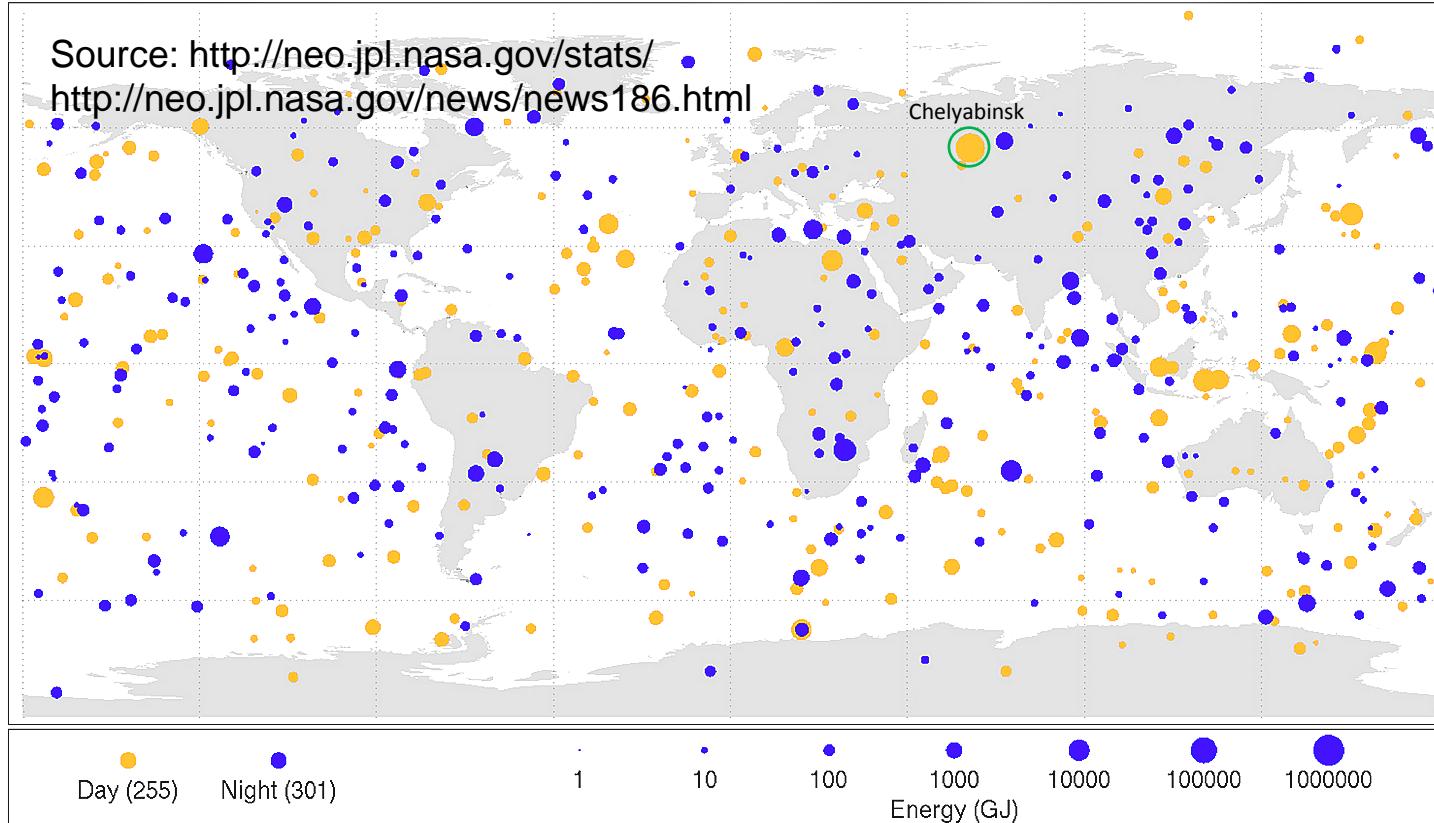
brown+2016

Are impacts uniformly distributed on Earth's surface?

Impacts observed distribution

Bolide events 1994-2013

(Small asteroids that disintegrated in the Earth's atmosphere)

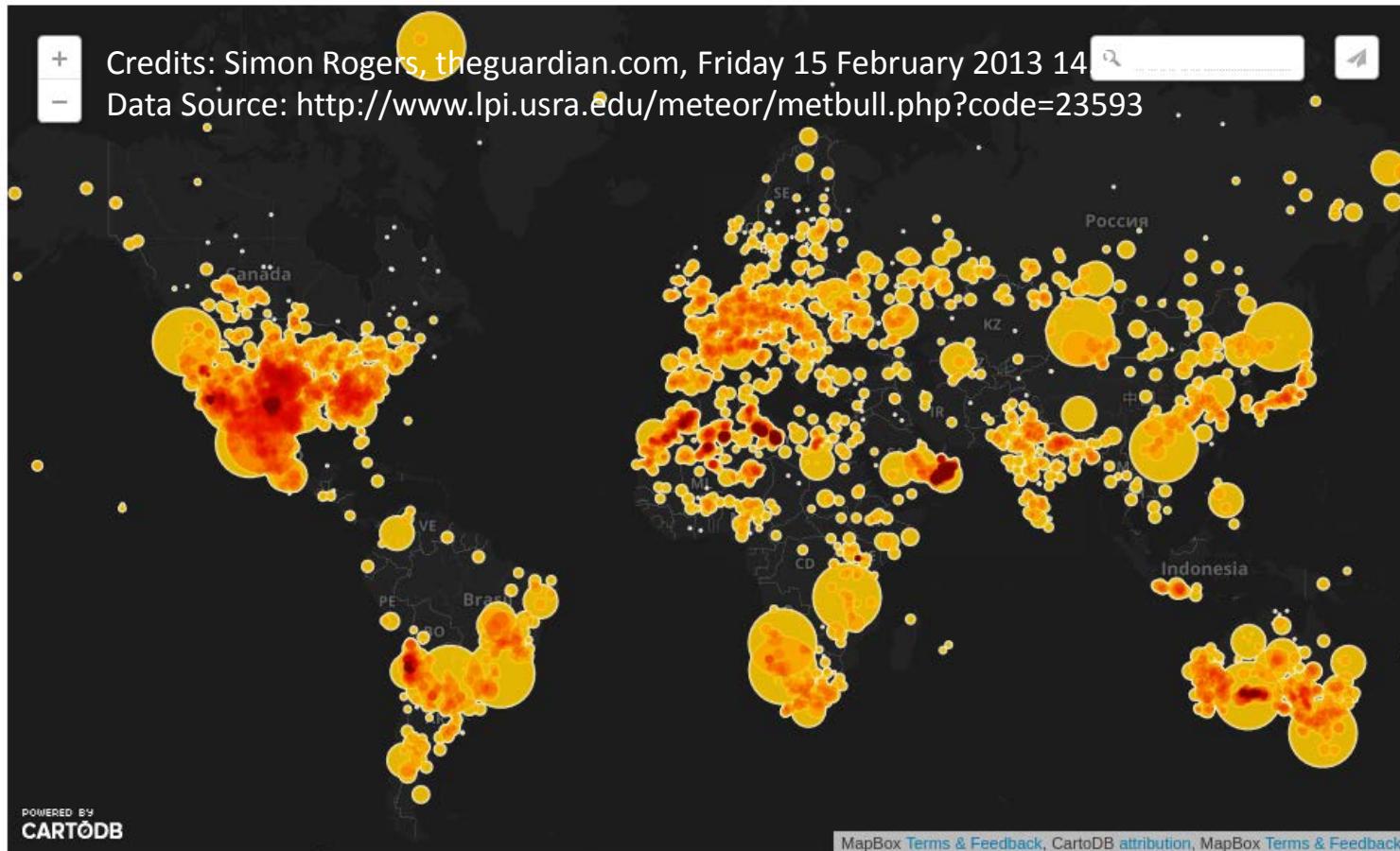


Biases & Caveats:

- Large fireballs
- Low rate events

Impacts observed distribution

Meteor & Meteorites



Biases & Caveats:

- Continents
- Populated & Developed areas
- Mostly nocturnal events
- Large meteoroids

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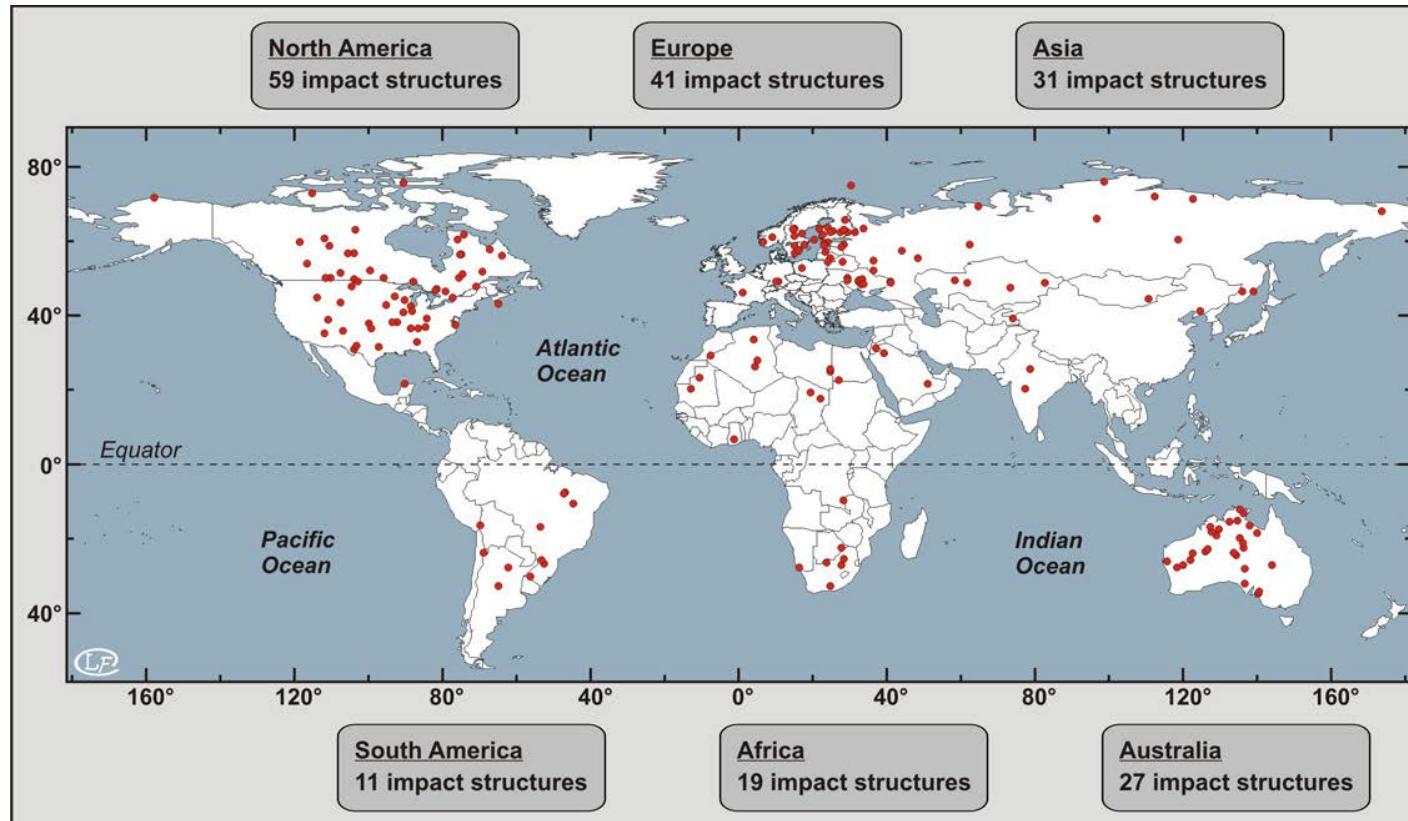
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Impacts observed distribution

Large Craters



Biases & Caveats:

- Very large impacts
- Continental areas
- Geological conditions
- Low weathering areas

Credits: Ludovic Ferriere

Data Source: <http://www.meteorimpactonearth.com/meteorite.html>

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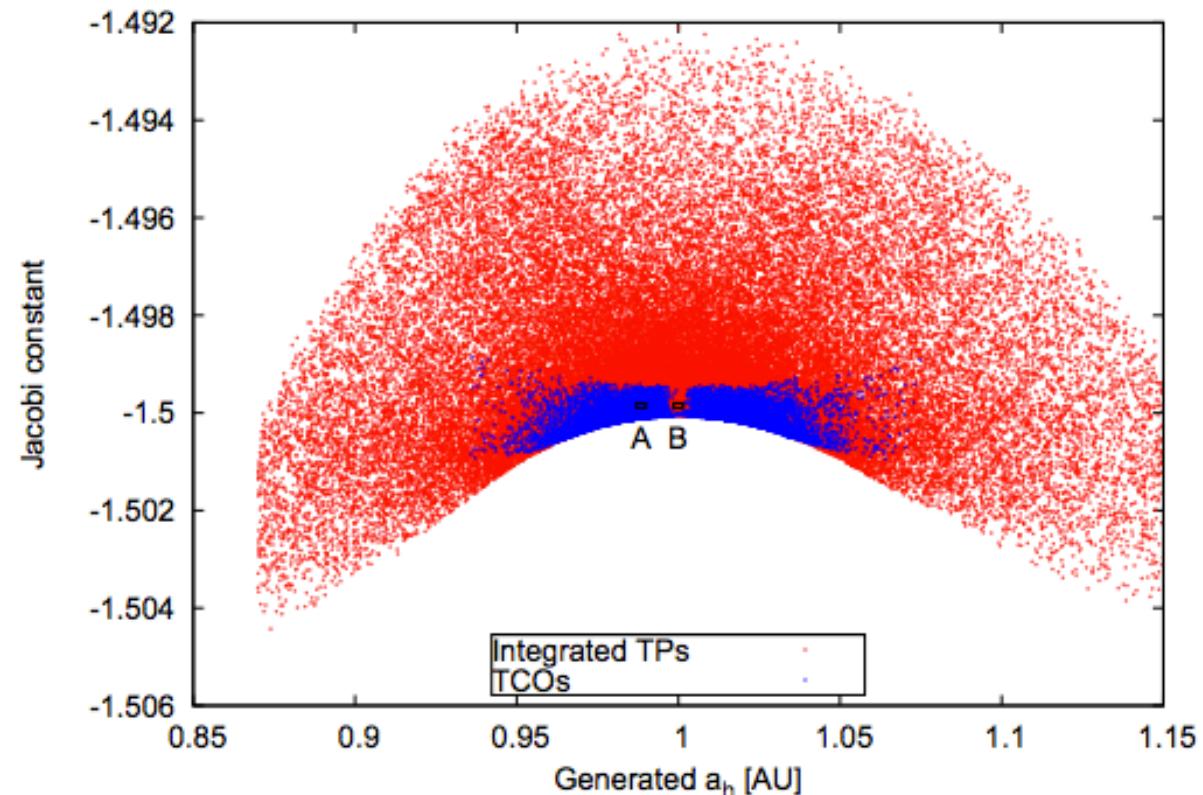
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Can we determine theoretically the distribution of impacts? (regardless impactor size)

Test Particle Integration

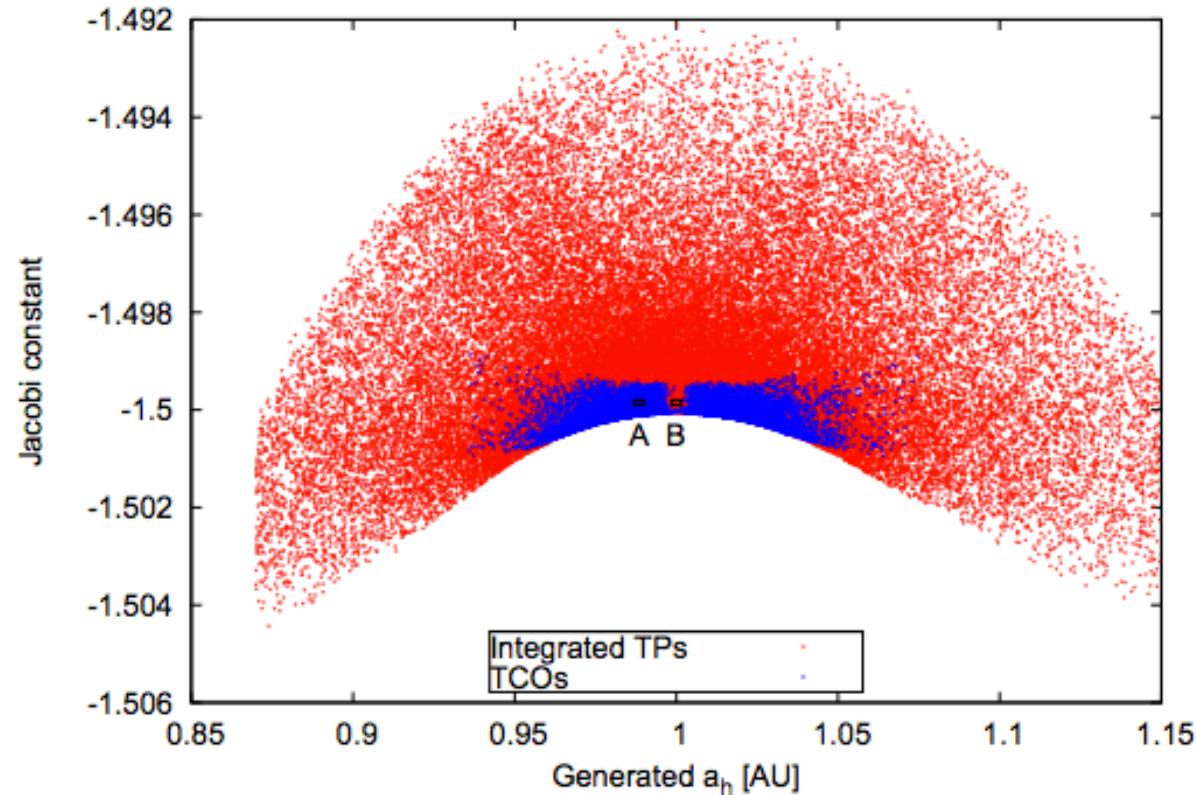


Granvik, Vaubaillon & Jedicke (2012)

Bulk properties of the generated test particles and captured objects

	9,346,396,100
N_{tot}	9,346,396,100
<hr/>	
N_{int}	10,000,000
<hr/>	
Nominal model	
$N_{\text{TCF,short}}$	209,917
$N_{\text{TCF,long}}$	23,771
N_{TCO}	18,096
\bar{L}_{TC}	(62.2 \pm 1.3) d
$\bar{\tau}_{\text{TC}}$	(0.383 \pm 0.059) rev
\bar{L}_{TCO}	(286 \pm 18) d
$\bar{\tau}_{\text{TCO}}$	(2.88 \pm 0.82) rev
Fraction of TCOs with	
$\tau_{\text{TCO}} > 2.88$ rev	11%
$\tau_{\text{TCO}} > 5$ rev	3.4%
$\tau_{\text{TCO}} > 50$ rev	0.1%
$\text{TCO} > 271$ d	26%
$\text{TCO} > 365$ d	15%
$\text{TCO} > 3650$ d	0.1%
<hr/>	
Barycentric model	
$N_{\text{TCF,short}}$	320,748
$N_{\text{TCF,long}}$	34,843
N_{TCO}	4,494
\bar{L}_{TC}	(53.76 \pm 0.11) d
$\bar{\tau}_{\text{TC}}$	(0.21751 \pm 0.00037) rev
\bar{L}_{TCO}	(334.6 \pm 1.7) d
$\bar{\tau}_{\text{TCO}}$	(1.1280 \pm 0.0019) rev

Test Particle Integration

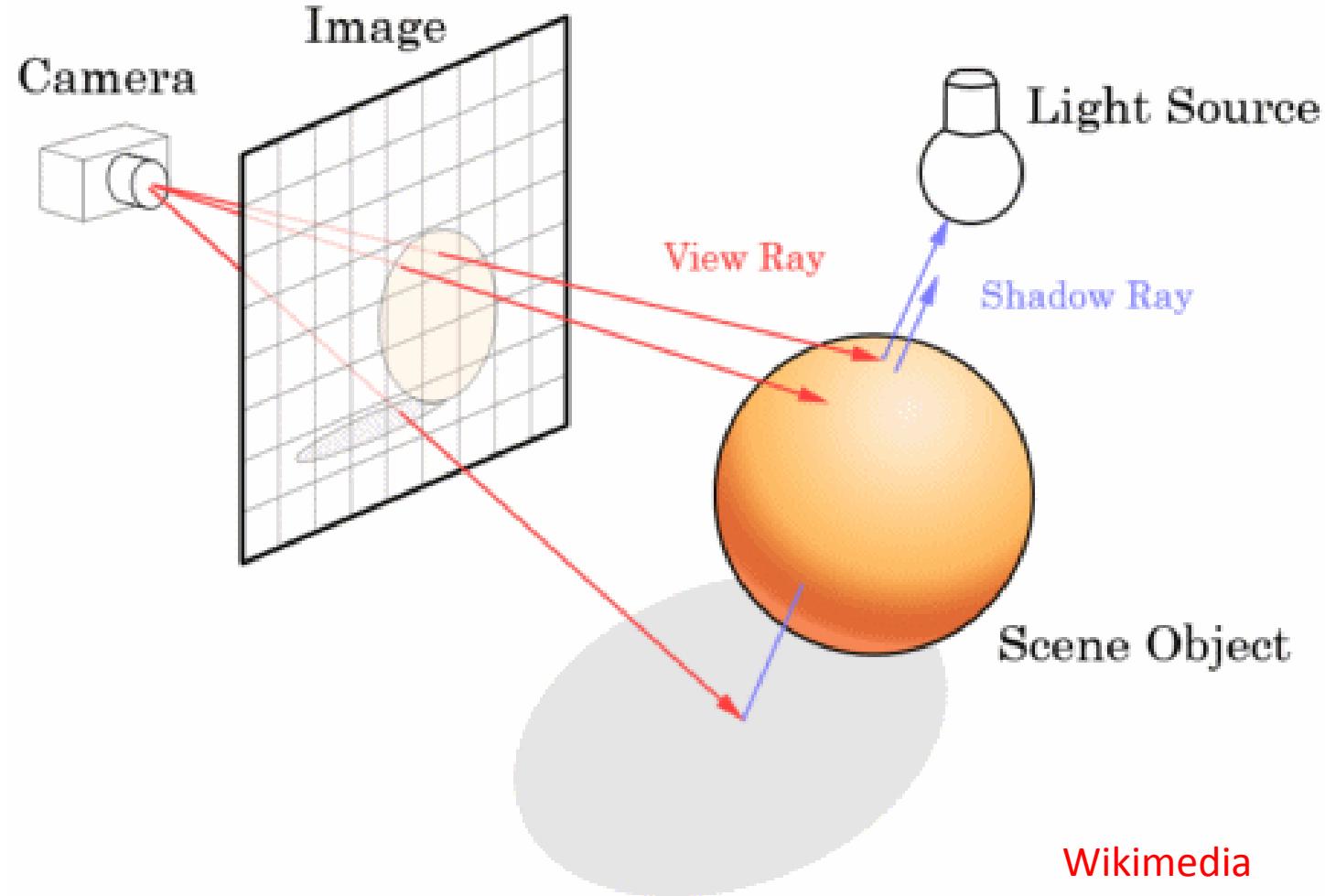


Caveats:

- Low efficiency (many TPs a few impacts)
- Partial covering of the configuration space.
- Sensitive to numerical integration precision

Granvik, Vaubaillon & Jedicke (2012)

Ray Tracing Algorithm



Wikimedia

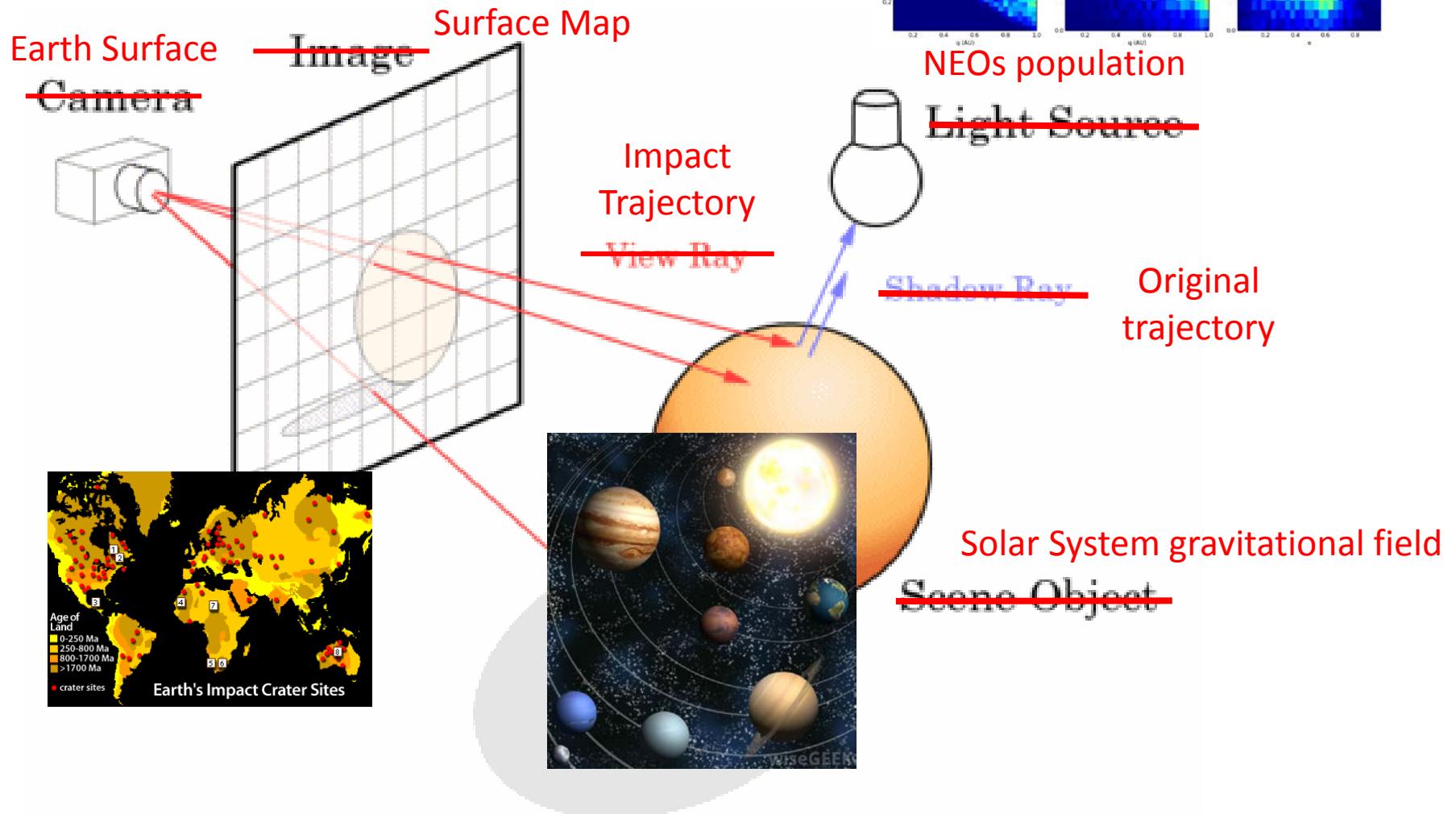
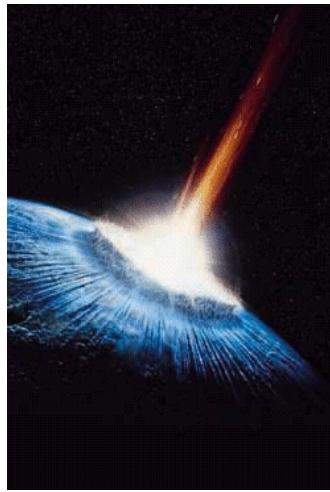
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Ray Tracing Algorithm



Credit: Rikk the Gaijin

Gravitational Ray Tracing (GRT)



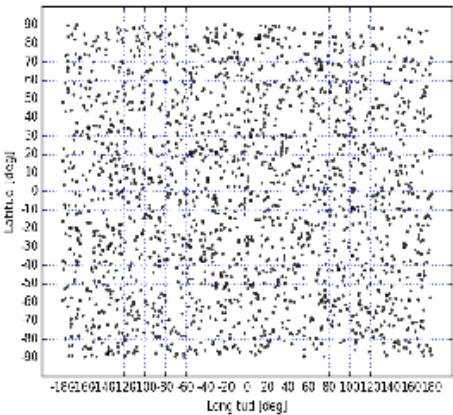
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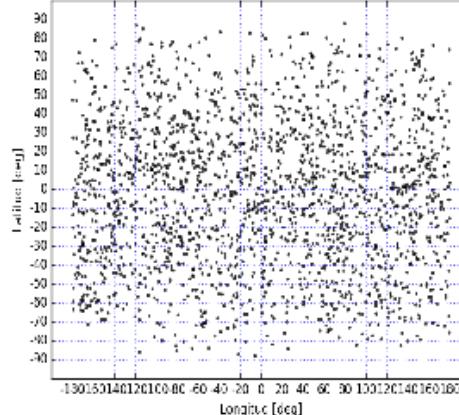
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GRT: initial conditions

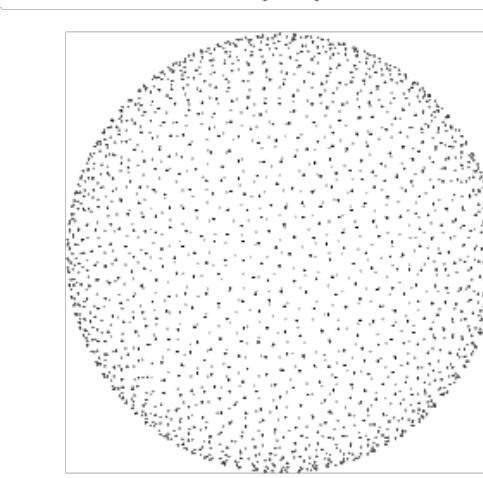
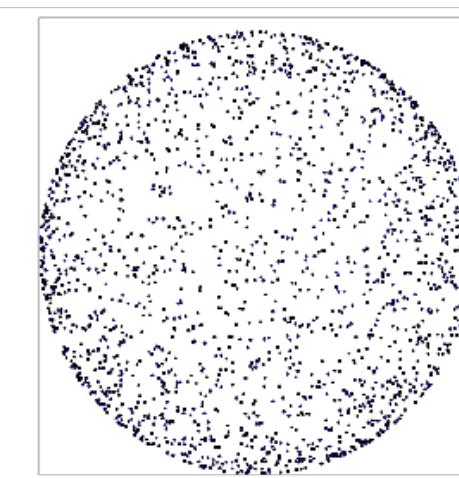
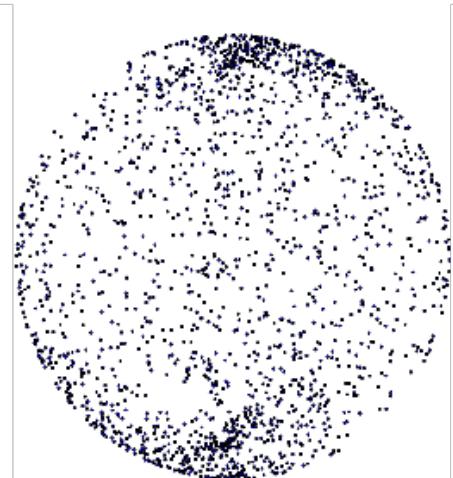
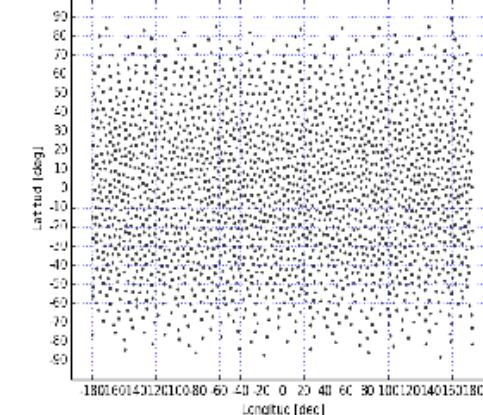
Sampling the Earth Surface



Uniform Distribution

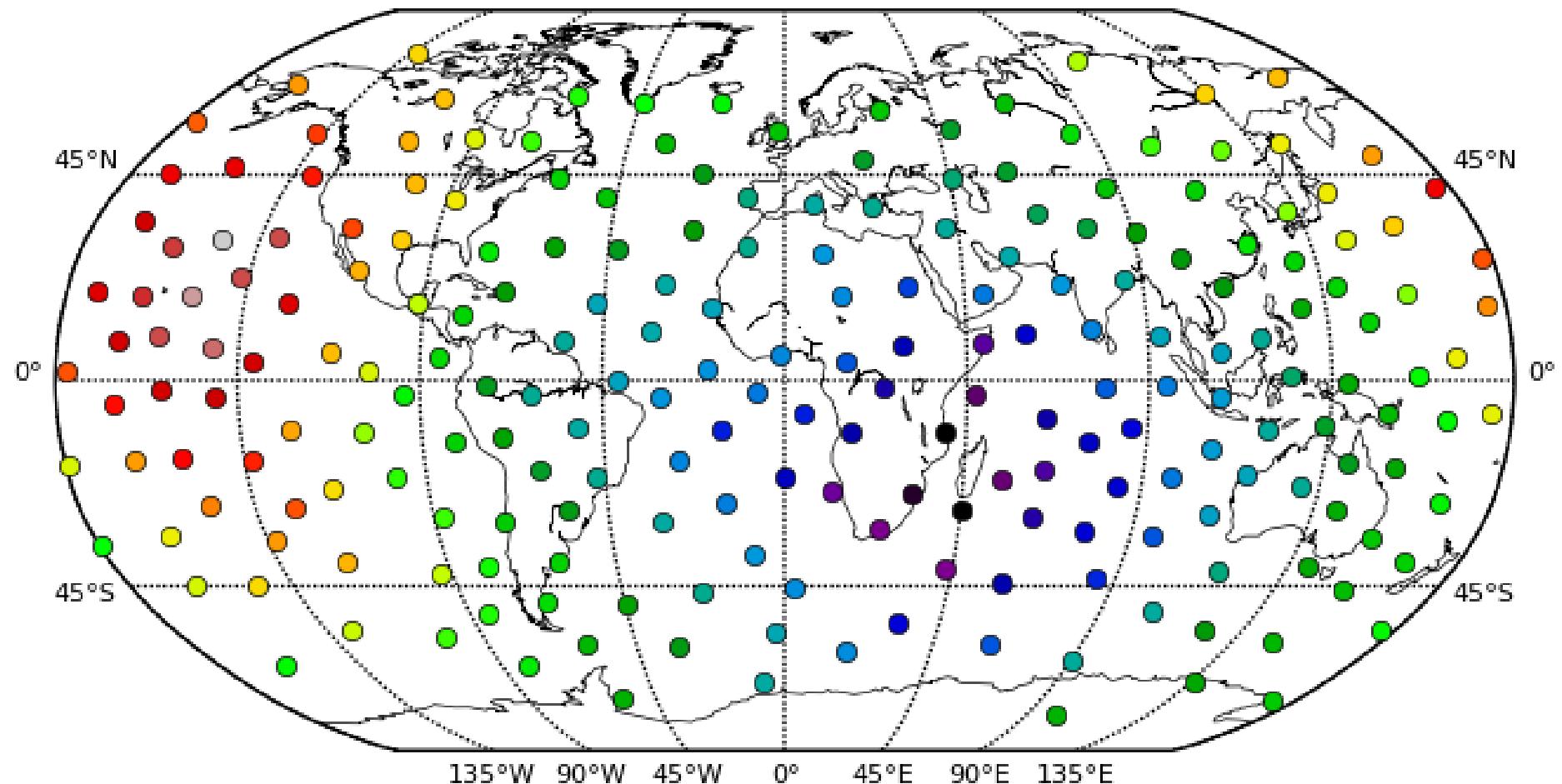


Blue Noise Distribution



GRT: Initial conditions

Distribution of 223 geographical sites with minimum separation of 10 degrees



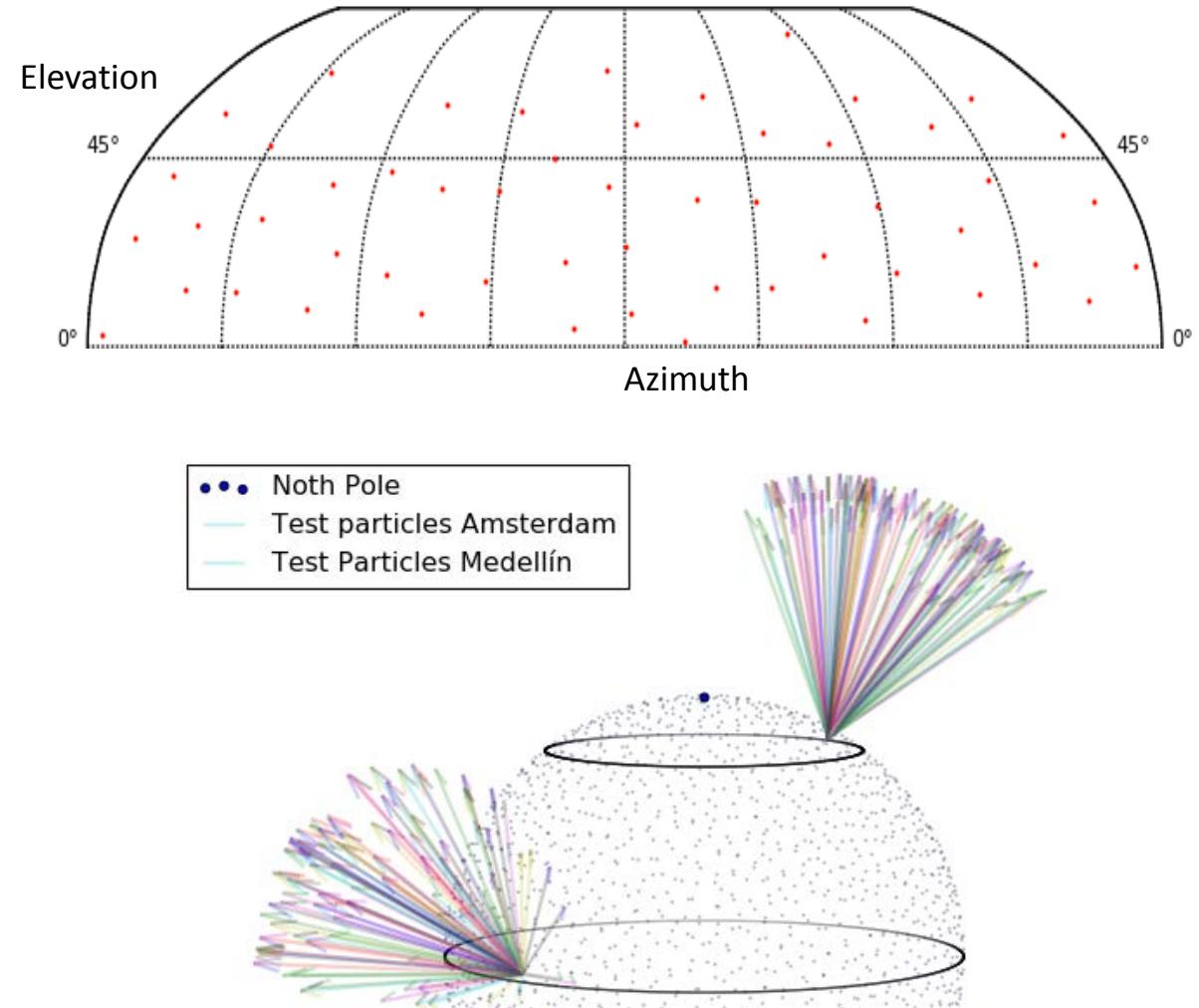
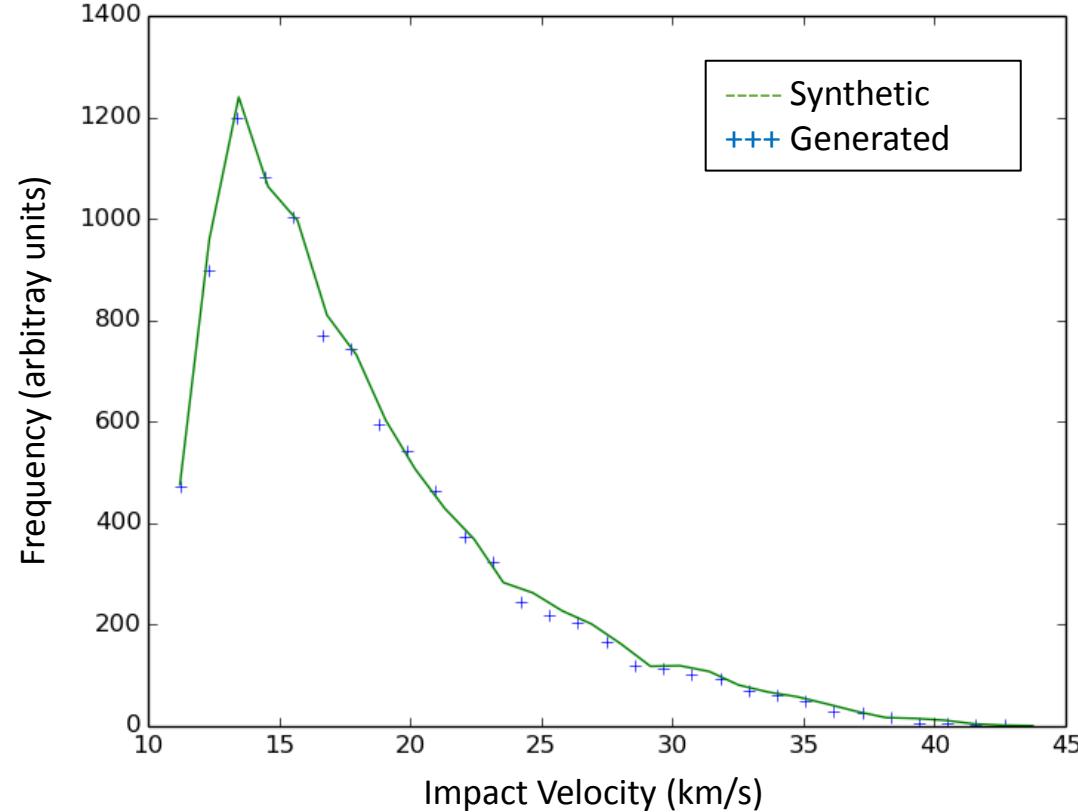
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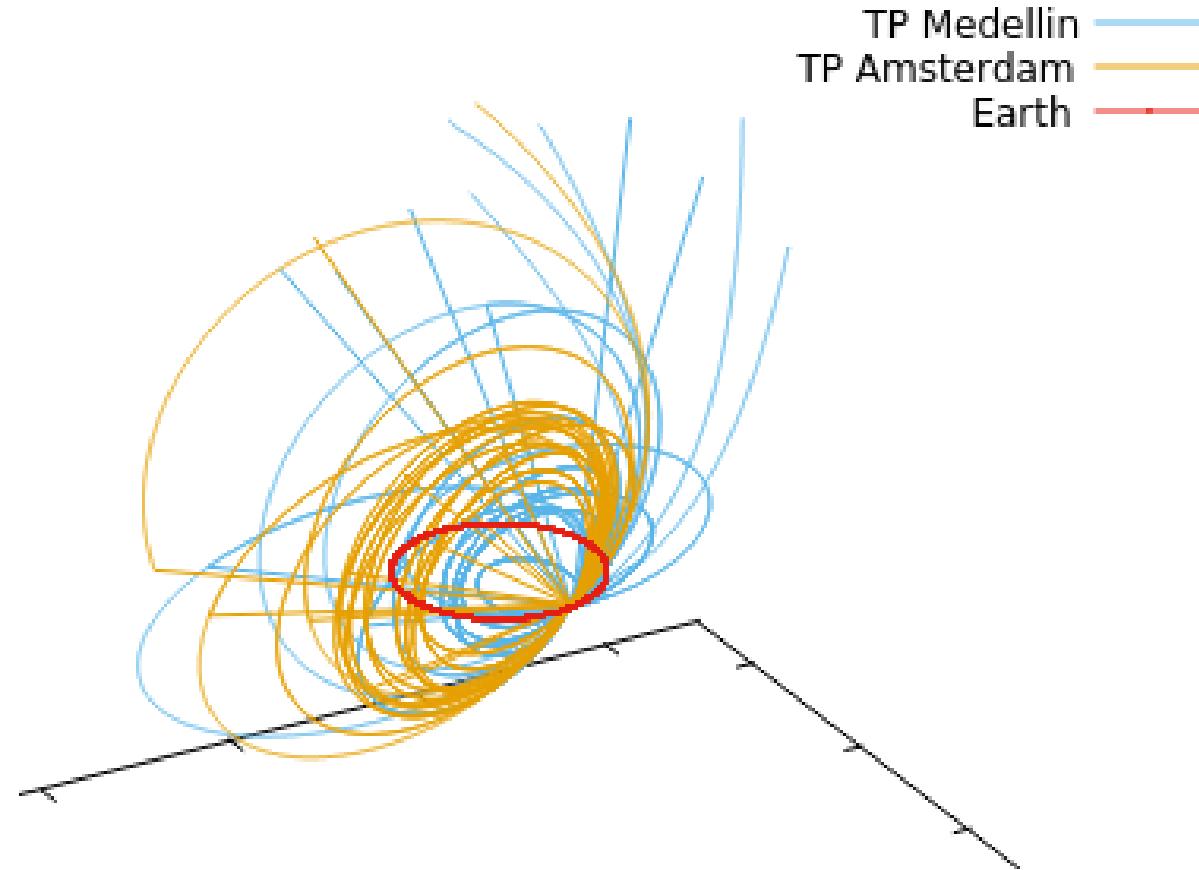
GRT: Initial conditions



We generate local configuration: Azimuth (A), elevation (a), impact velocity (v)

GRT: Ray trajectories

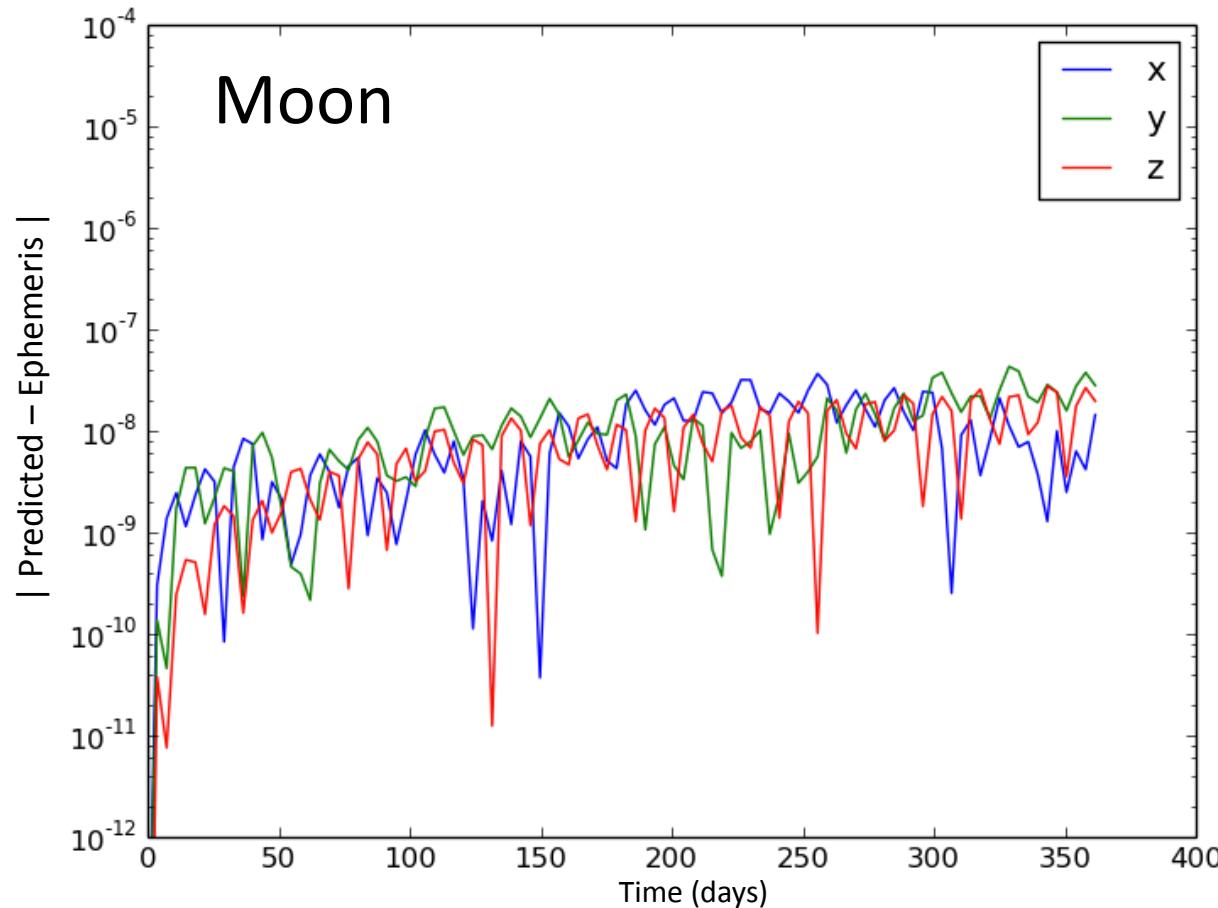
Integration convert local configuration (A, a, v) to orbital configuration (q, e, i)



Integration characteristics:

- Gragg-Burkhill-Stoer Method
- Time of integration:
Max (2 years, 2 Orbital Period)
- All 8 planets + Moon
- Planetary positions:
JPL Ephemeris DE430

GRT: Ray trajectories

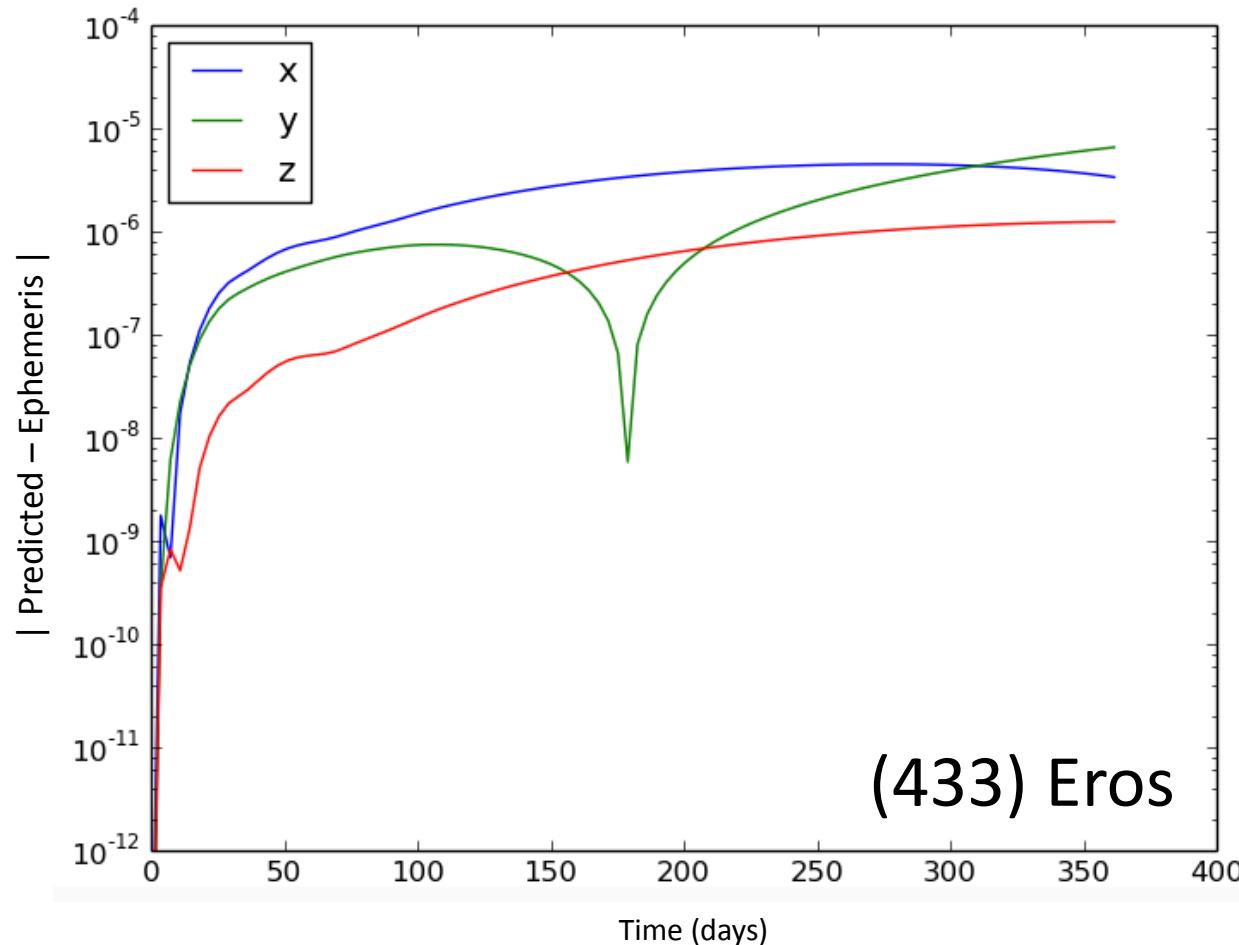


Precision test with the moon as a test particle

Integration characteristics:

- Gragg-Burkhill-Stoer Method
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- Planetary positions:
JPL Ephemeris DE430

GRT: Ray trajectories

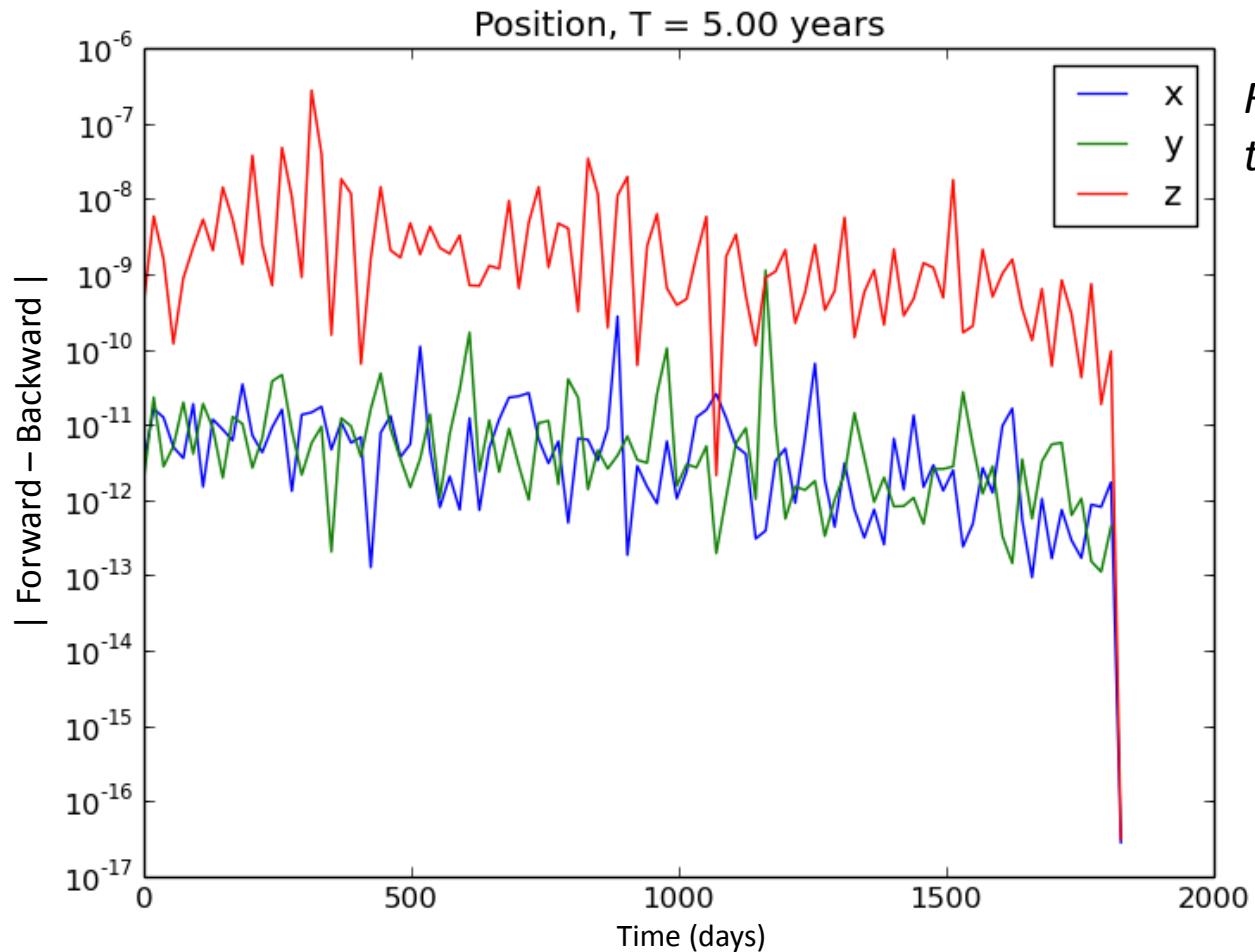


Precision test with *EROS* as a test particle

Integration characteristics:

- Gragg-Burkhill-Stoer Method
- Time of integration:
Max (2 years, 2 Orbital Period)
- All 8 planets + Moon
- Planetary positions:
JPL Ephemeris DE430

GRT: Ray trajectories



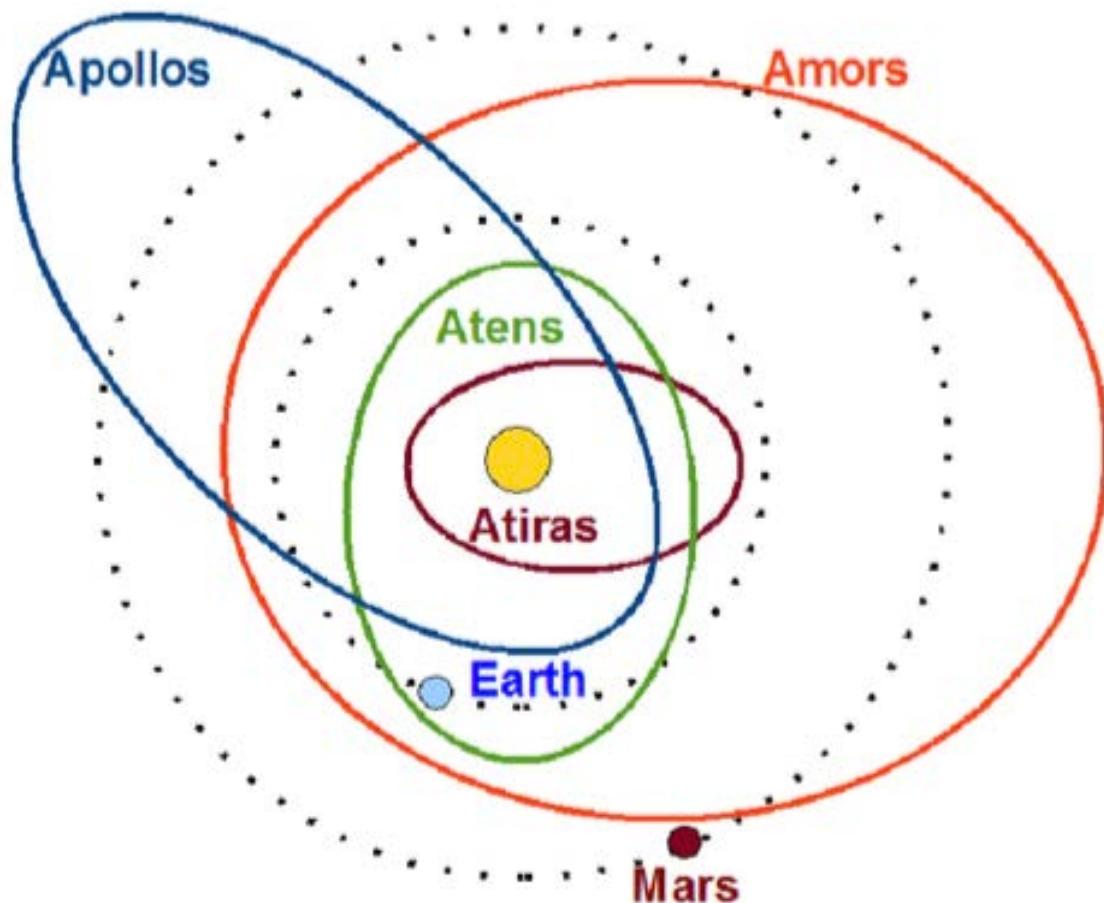
Forward and backward integration test

Integration characteristics:

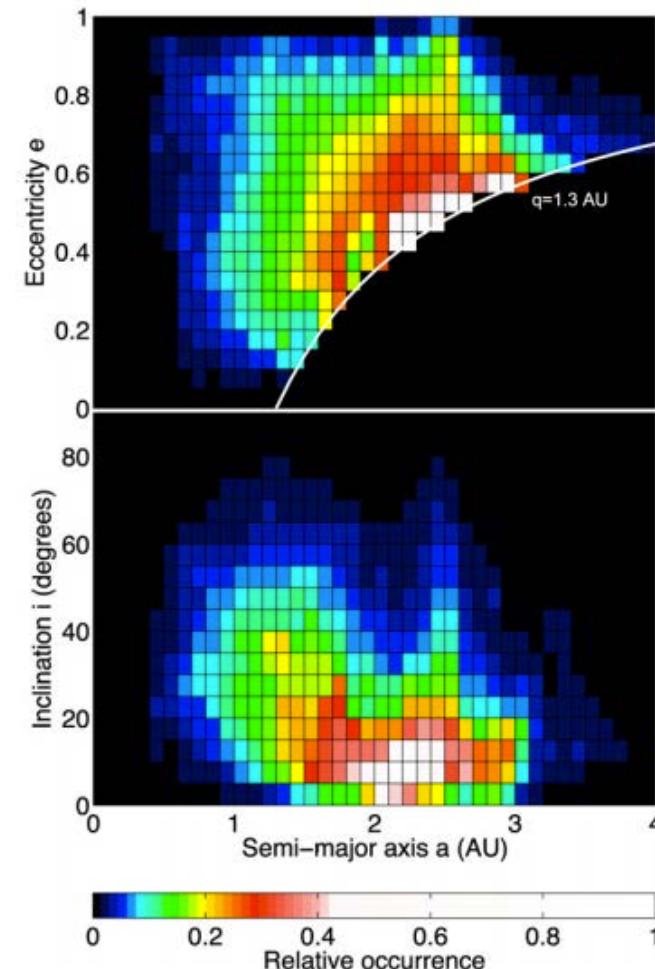
- Gragg-Burkhill-Stoer Method
- Time of integration:
Max (2 years, 2 Orbital Period)
- All 8 planets + Moon
- Planetary positions:
JPL Ephemeris DE430

GRT: Source Intensity (aka. NEOs distribution)

Greenstreet (2007)



Le Feuvre & Wieczorek (2008)



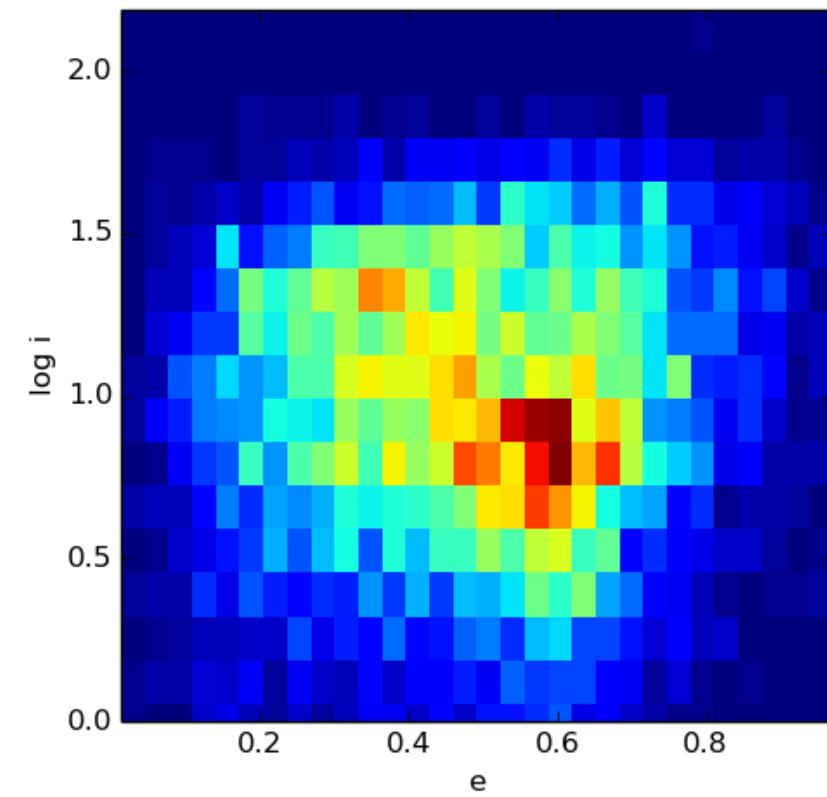
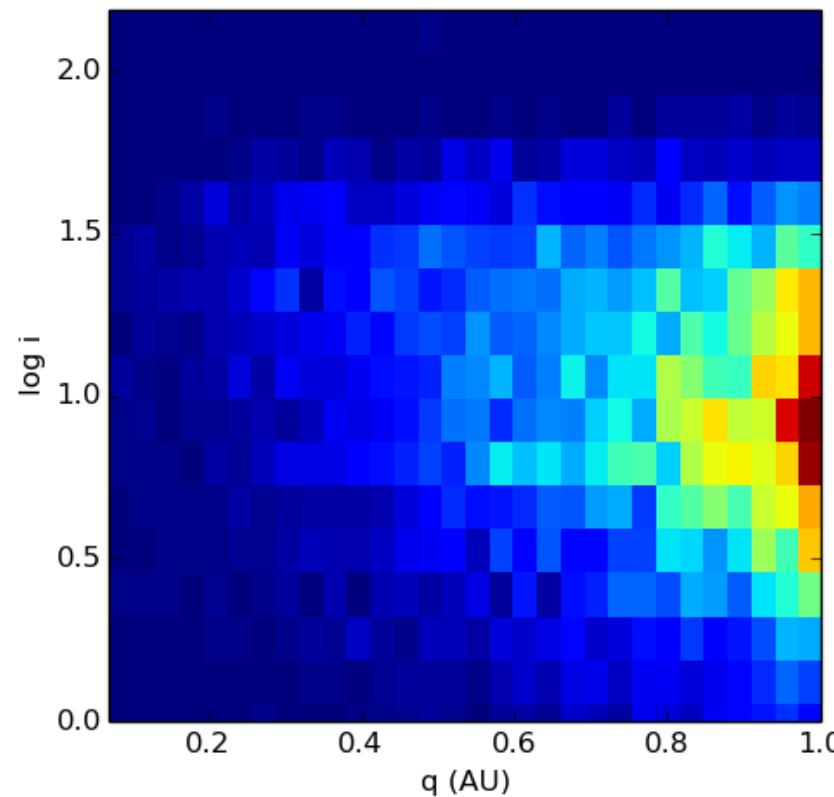
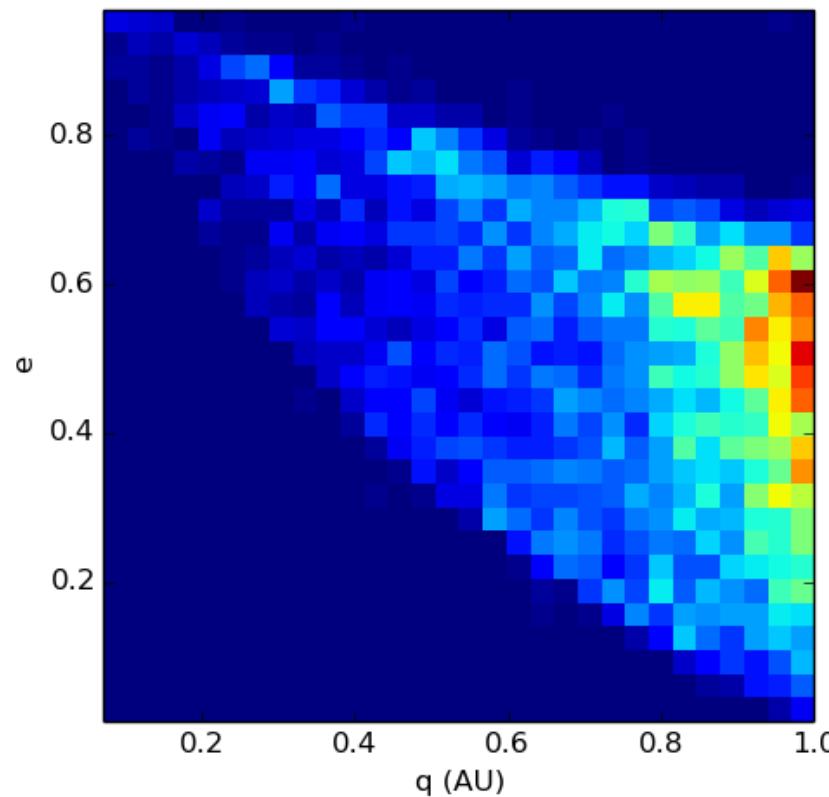
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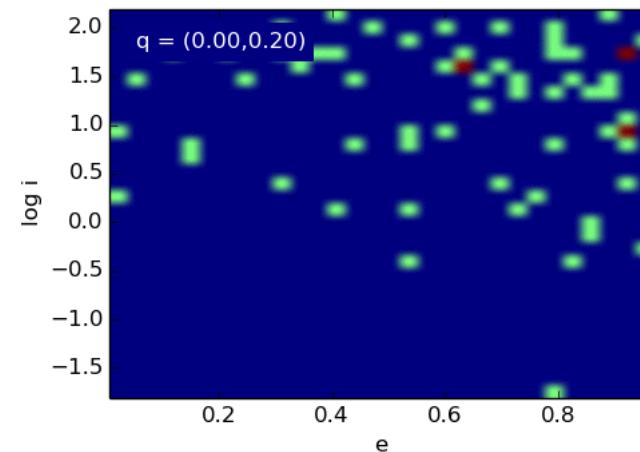
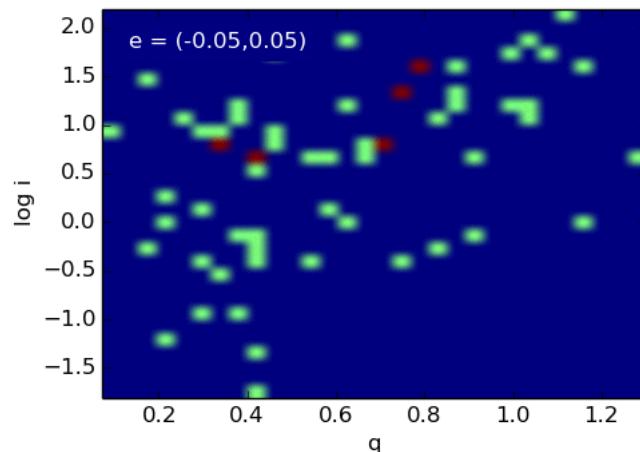
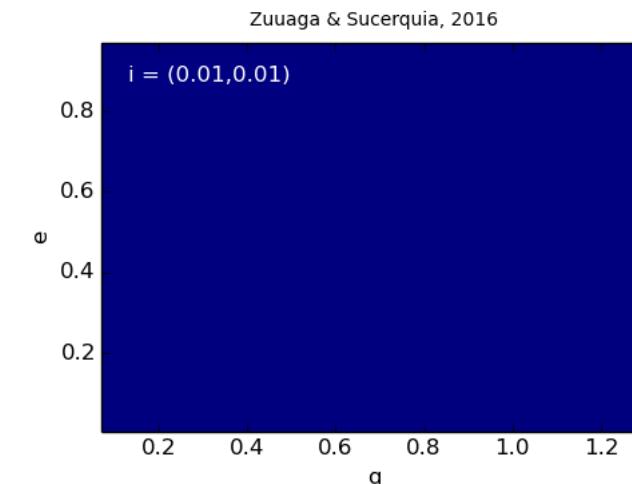
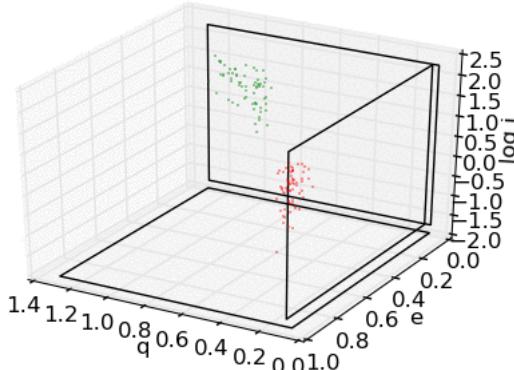
GRT: Source Intensity (aka. NEOs distribution)

Marginal distributions (14291 NEOs)



GRT: Source Intensity (aka. NEOs distribution)

“3D” Distribution

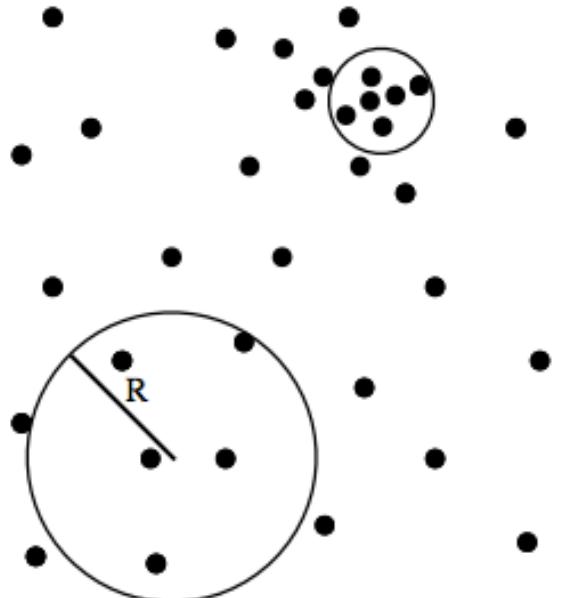


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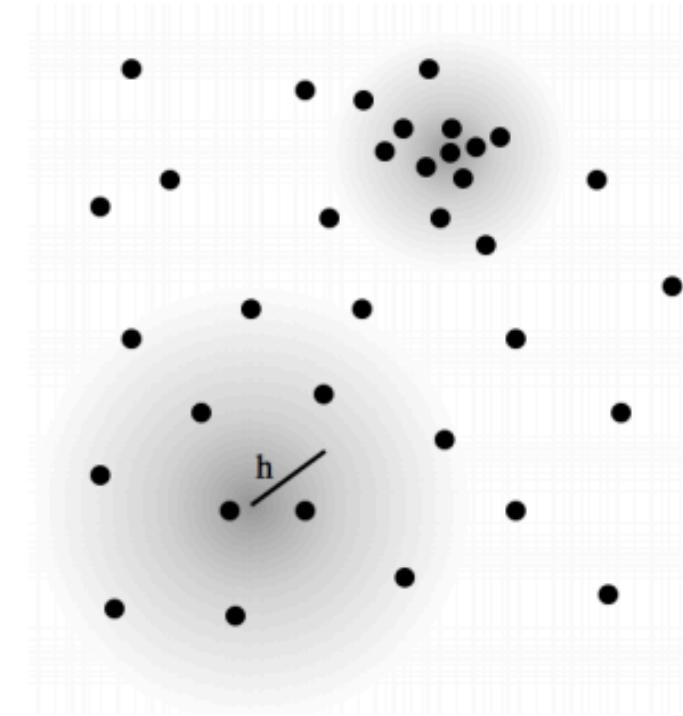
In particle-mesh



Local volume



Weighted Sum



Price, 2012

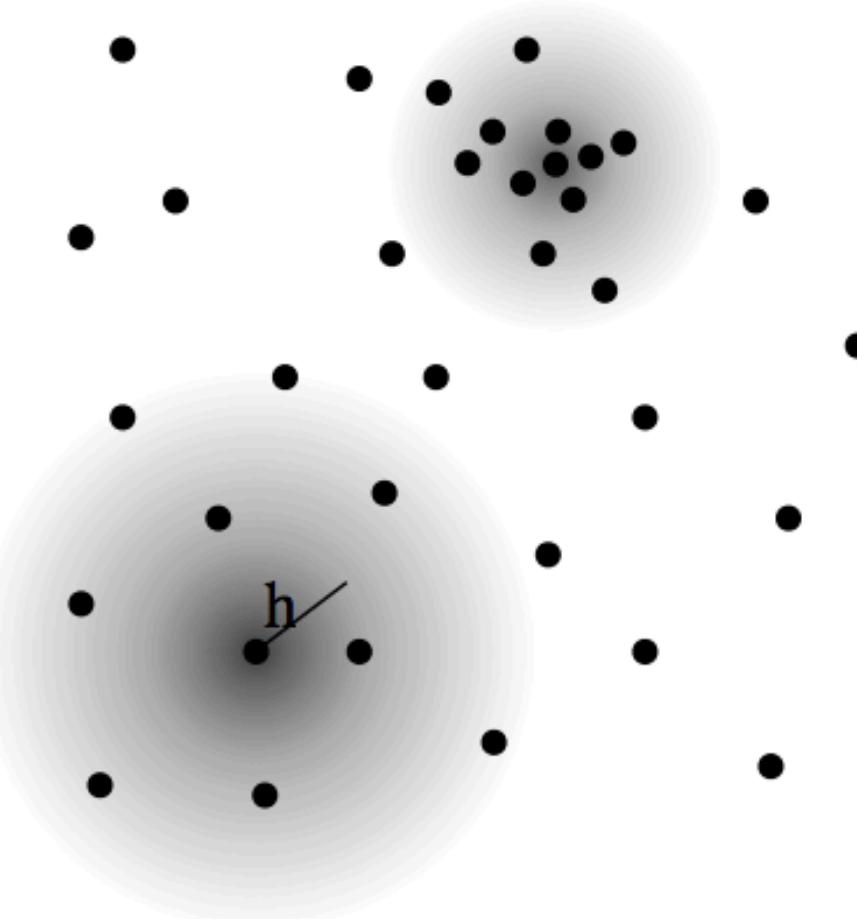
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GRT: Source Intensity (aka. NEOs distribution)



Kernel-weighted
sum:

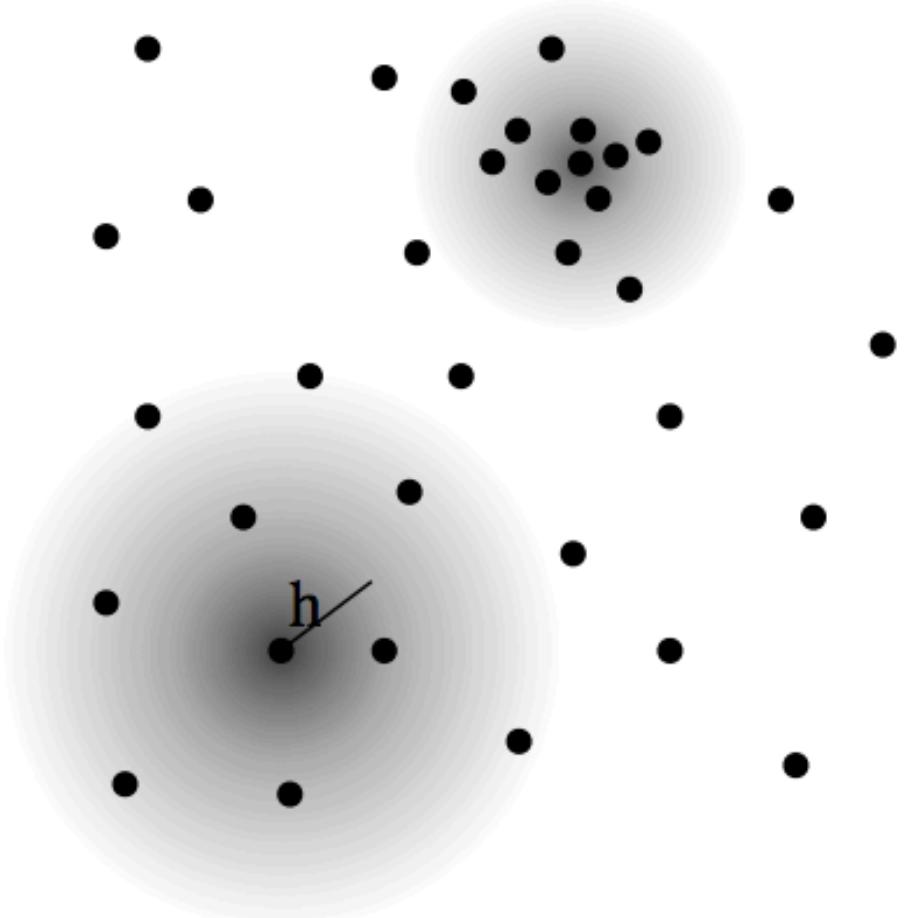
SPH

$$\rho(\mathbf{r}) = \sum_{j=1}^N m_j W(|\mathbf{r} - \mathbf{r}_j|, h)$$

$$w(q) = \sigma \begin{cases} \frac{1}{4}(2-q)^3 - (1-q)^3, & 0 \leq q < 1; \\ \frac{1}{4}(2-q)^3, & 1 \leq q < 2; \\ 0, & q \geq 2, \end{cases}$$

Price, 2012

GRT: Source Intensity (aka. NEOs distribution)



For distances in the q-e-i space we use a **simplified Drummond metric** ([Drummond, 1981](#)):

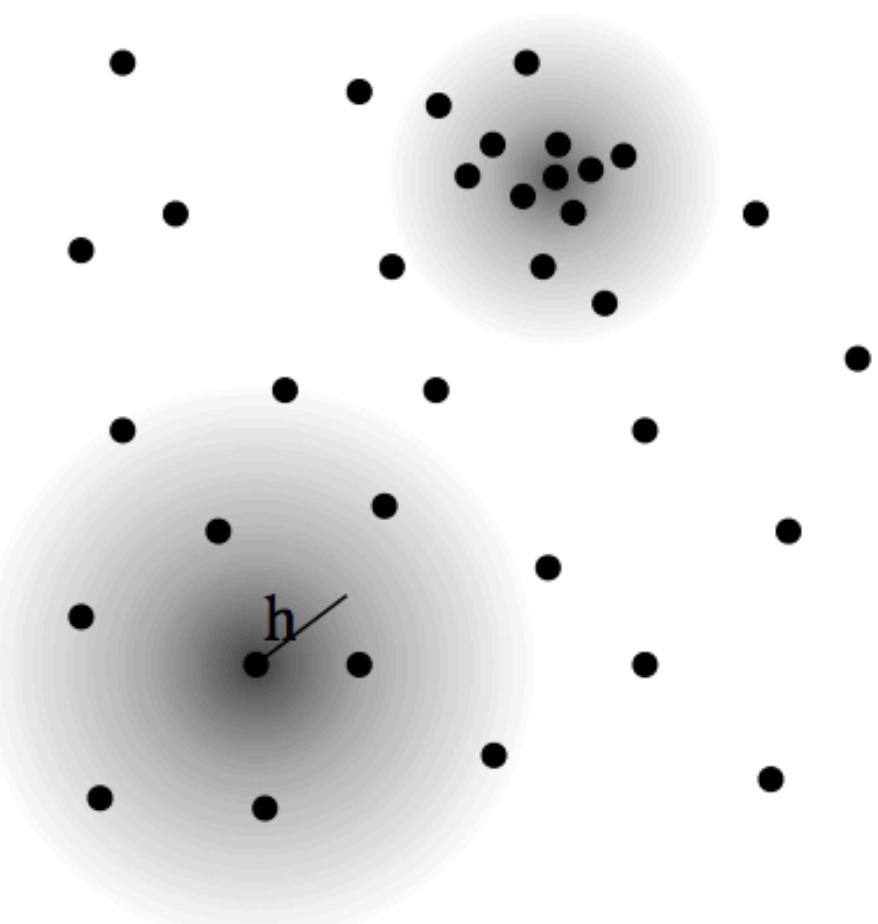
$$D_D^2 \equiv |\vec{x} - \vec{x}_i|^2 = \left(\frac{e - e_i}{e + e_i} \right)^2 + \left(\frac{q - q_i}{q + q_i} \right)^2 + \left(\frac{i - i_i}{180^\circ} \right)^2$$

Source intensity (number density) around a given “ray” footprint $\mathbf{x}:(q,e,i)$ is given by an SPH-like formula ([Price, 2012](#)):

$$n(\vec{x}) = \sum_i W(|\vec{x} - \vec{x}_i|, h)$$

After experiencing with different scale lengths, we find that $h = 0.1$ better fits our purposes.

GRT: Source Intensity (aka. NEOs distribution)



Probability of having an impact with parameters A , a , v which is associated with a ray terminal configuration $\mathbf{x} = (q, e, i)$ is given by:

$$P(A_j, a_j, v_j) \sim n(\vec{x}_j)$$

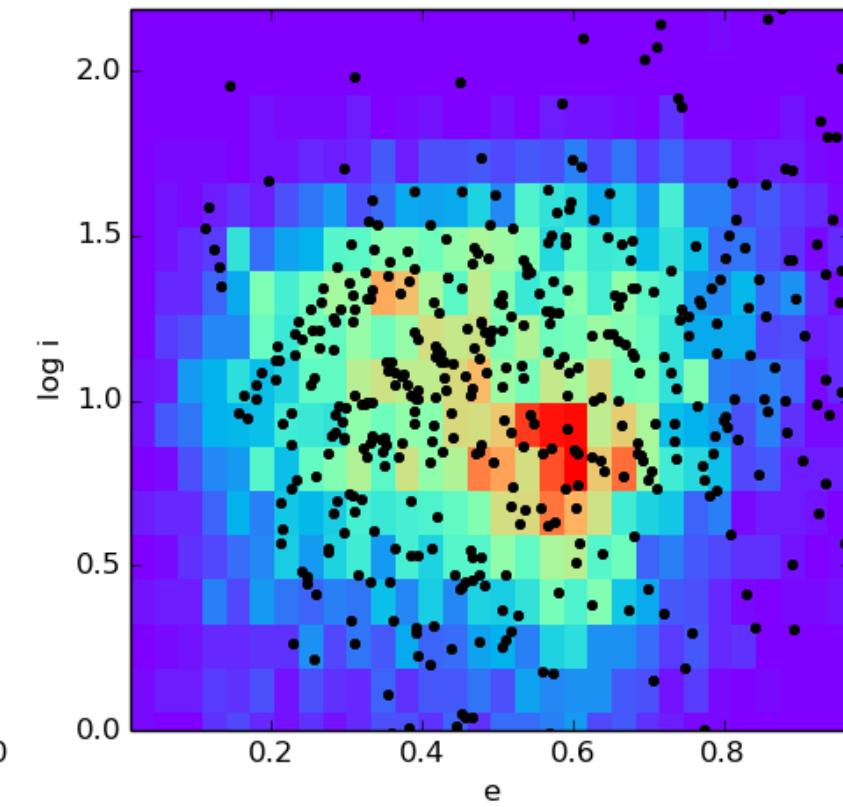
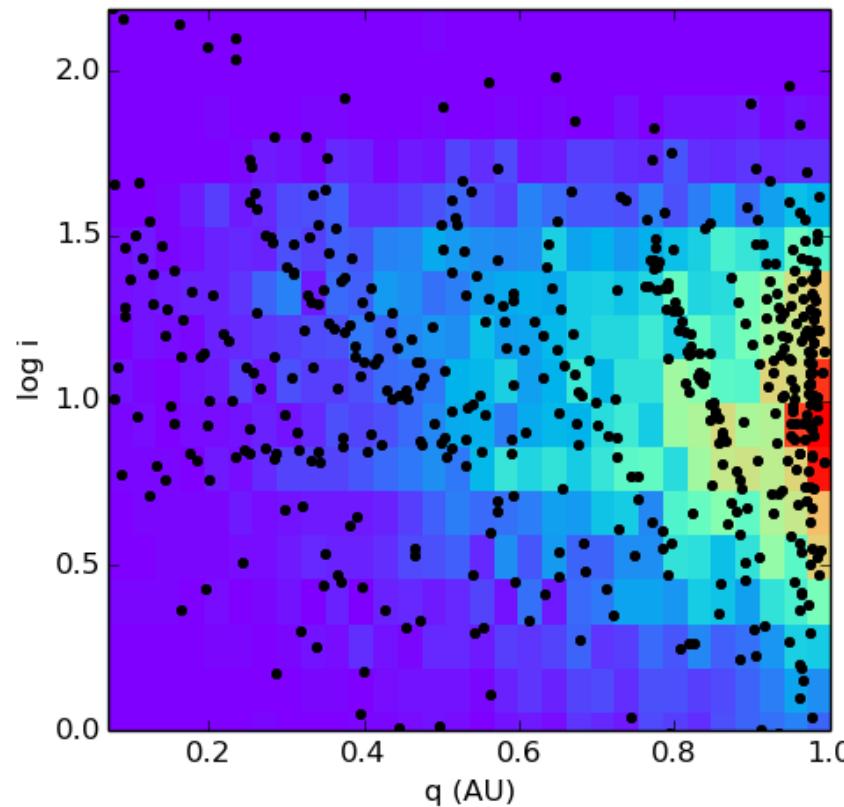
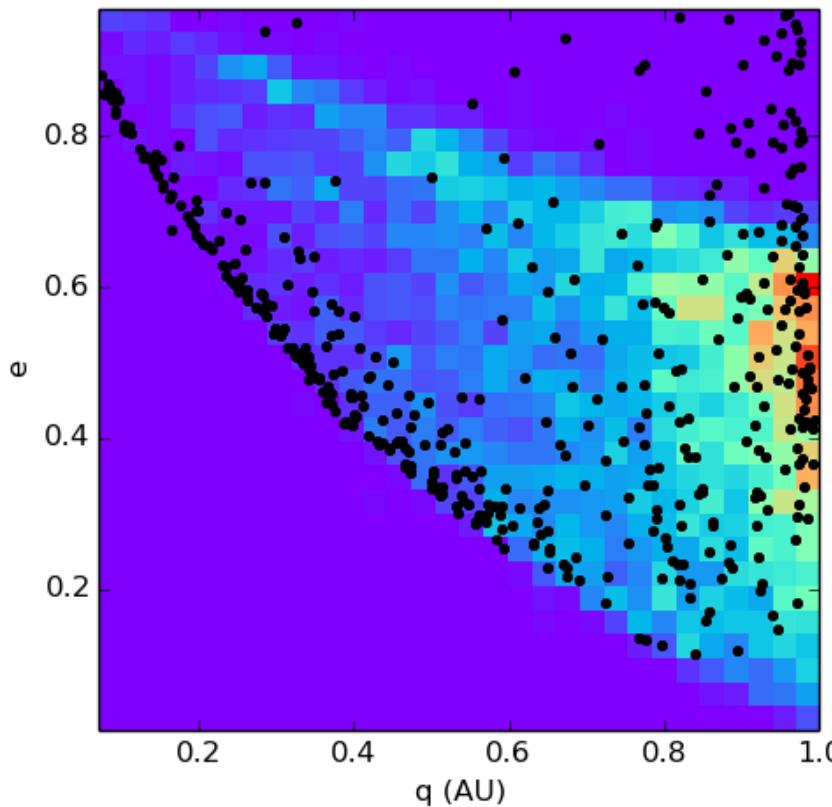
The total relative probability of having an impact on a given site is approximated as:

$$P(\text{site}) \sim \sum_j P(A_j, a_j, v_j)$$

GRT: Preliminary* results

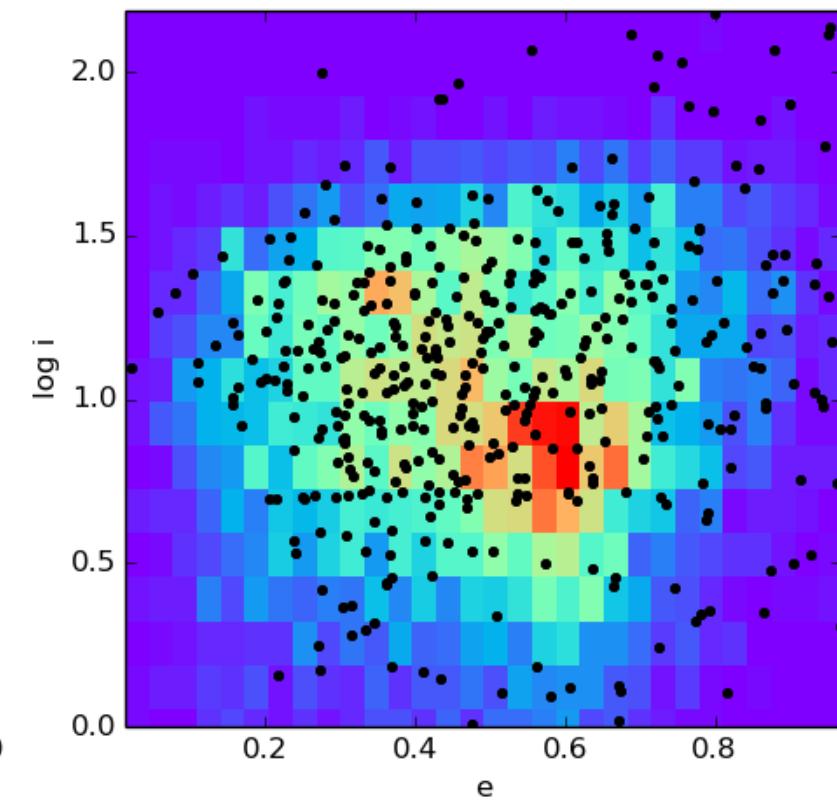
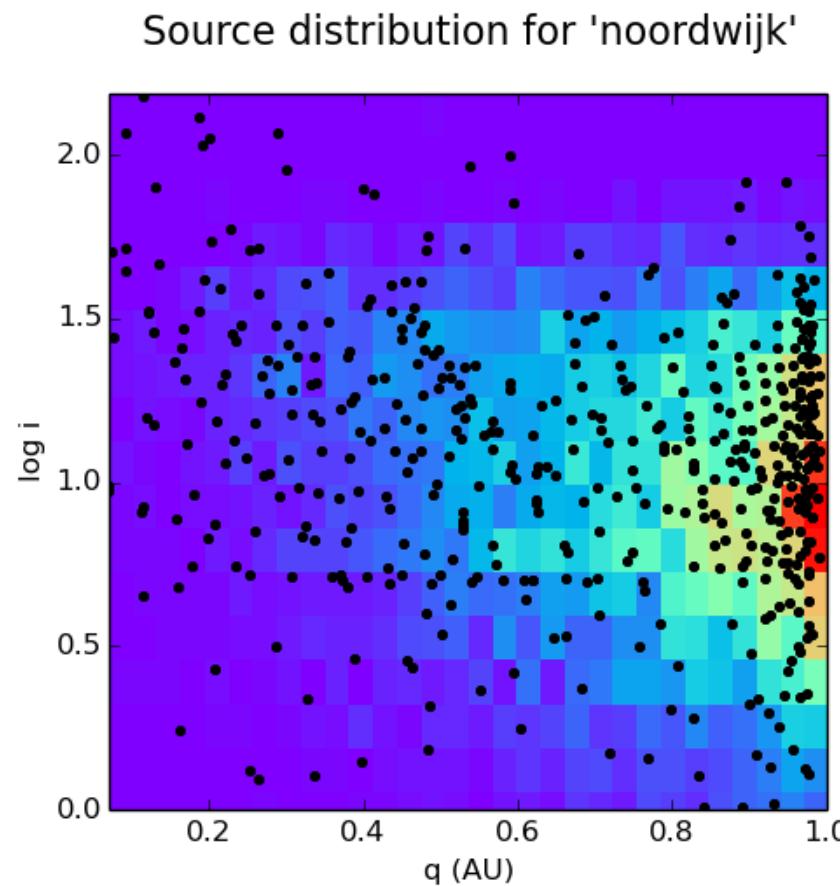
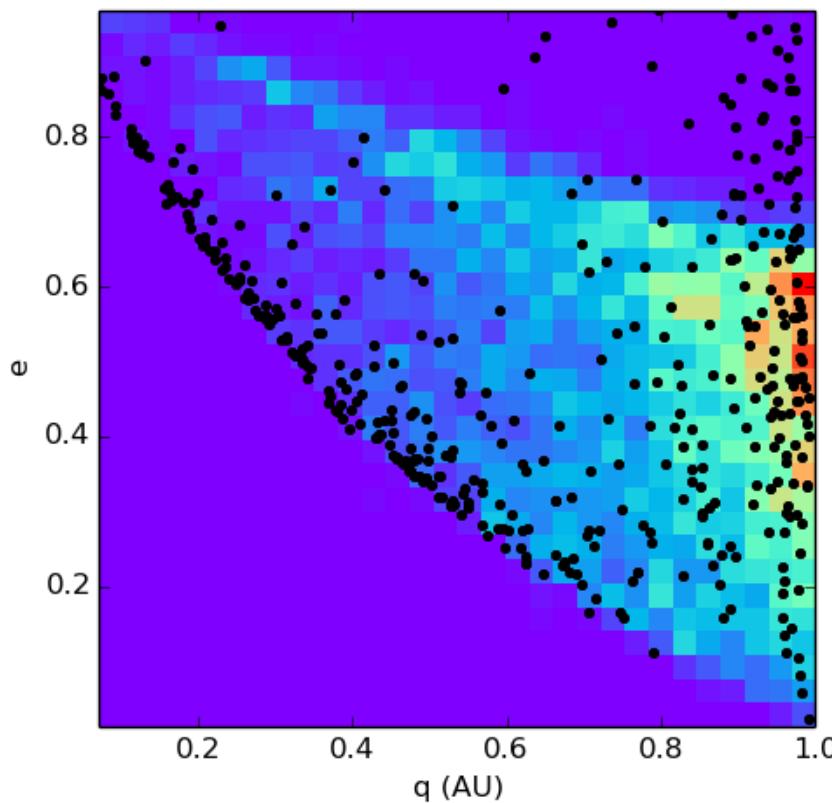
15 February 2013, 03:20 UTC

Source distribution for 'chelyabinsk'



GRT: Preliminary results

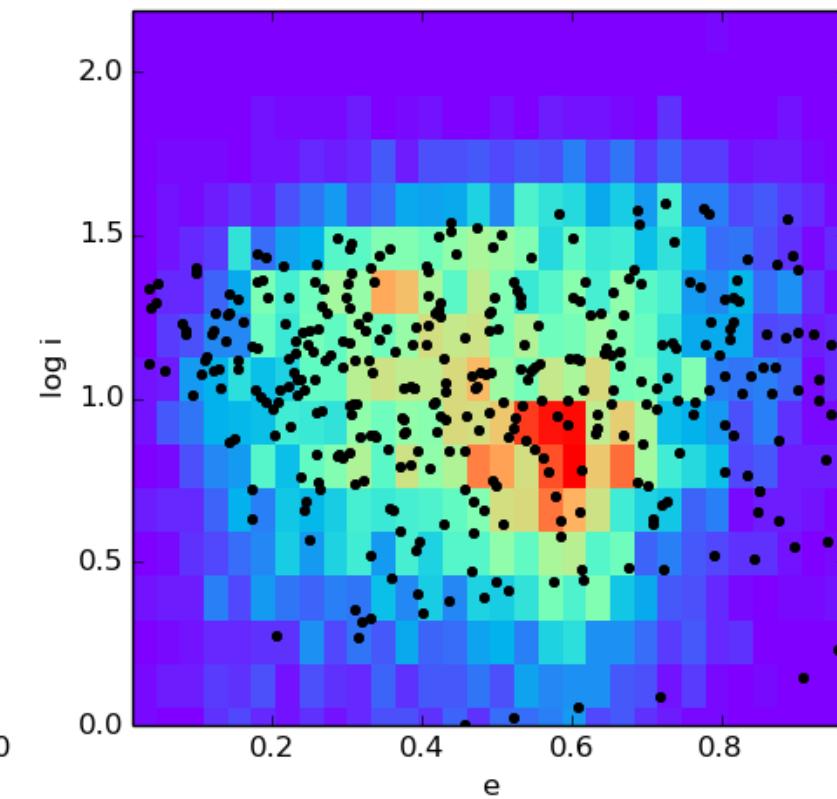
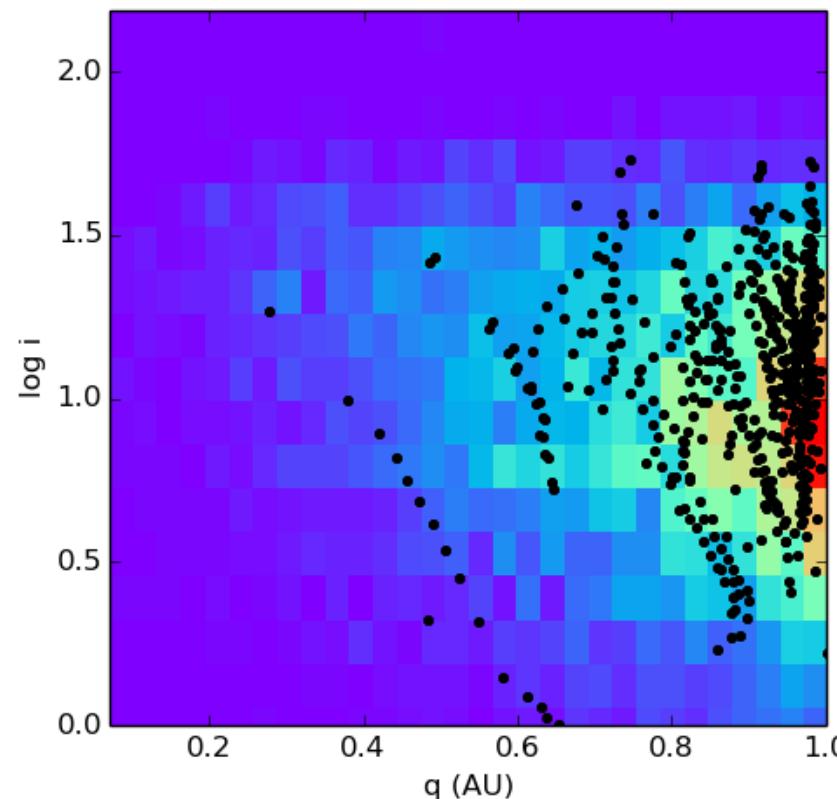
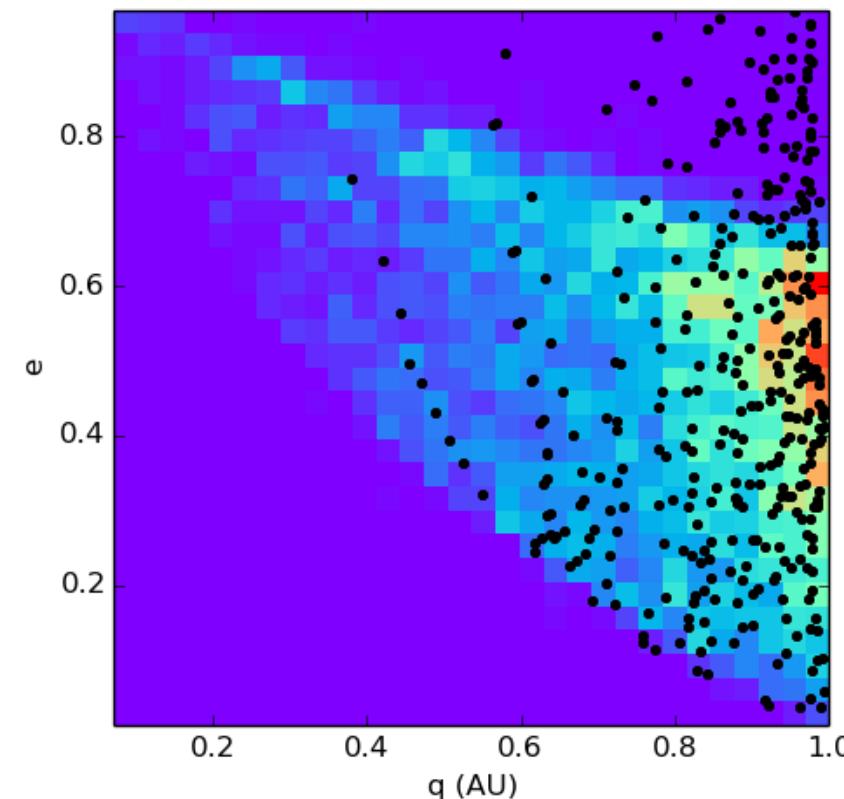
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GRT: Preliminary results

15 February 2013, 03:20 UTC

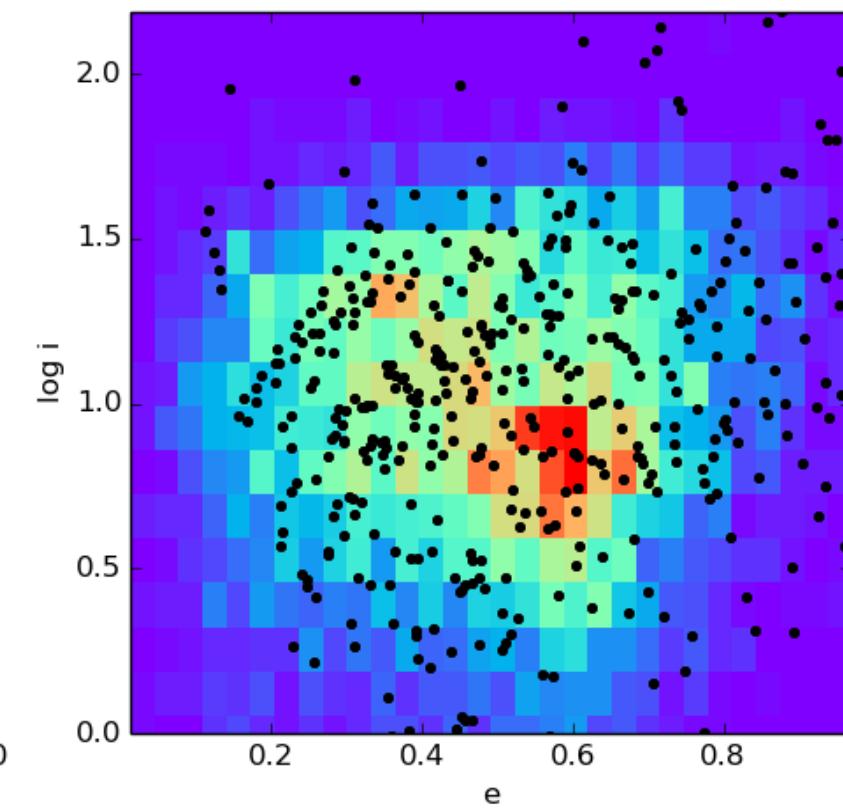
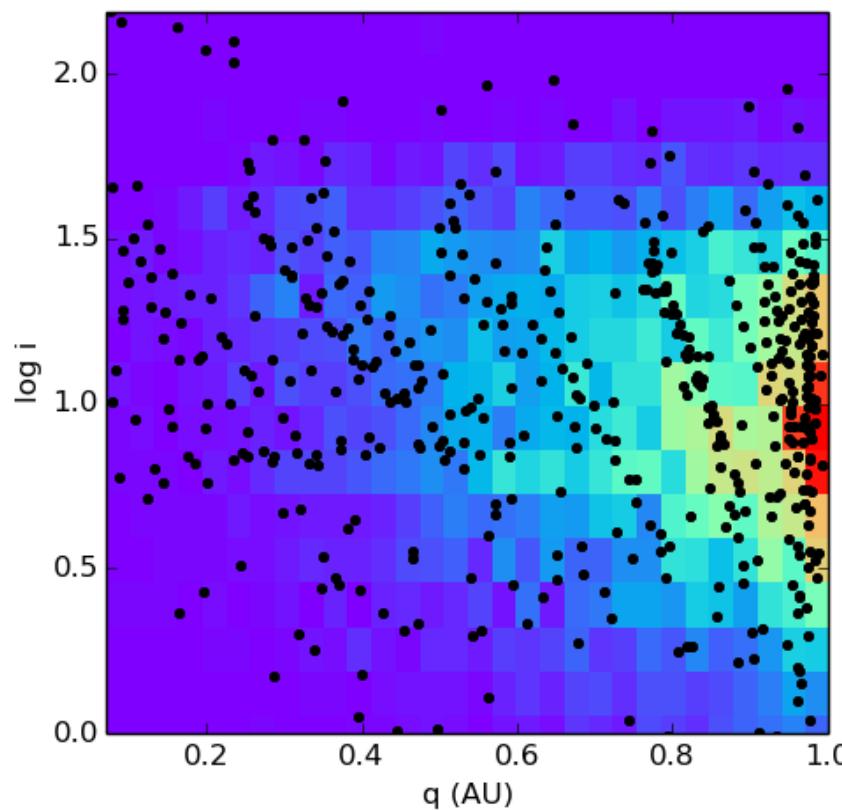
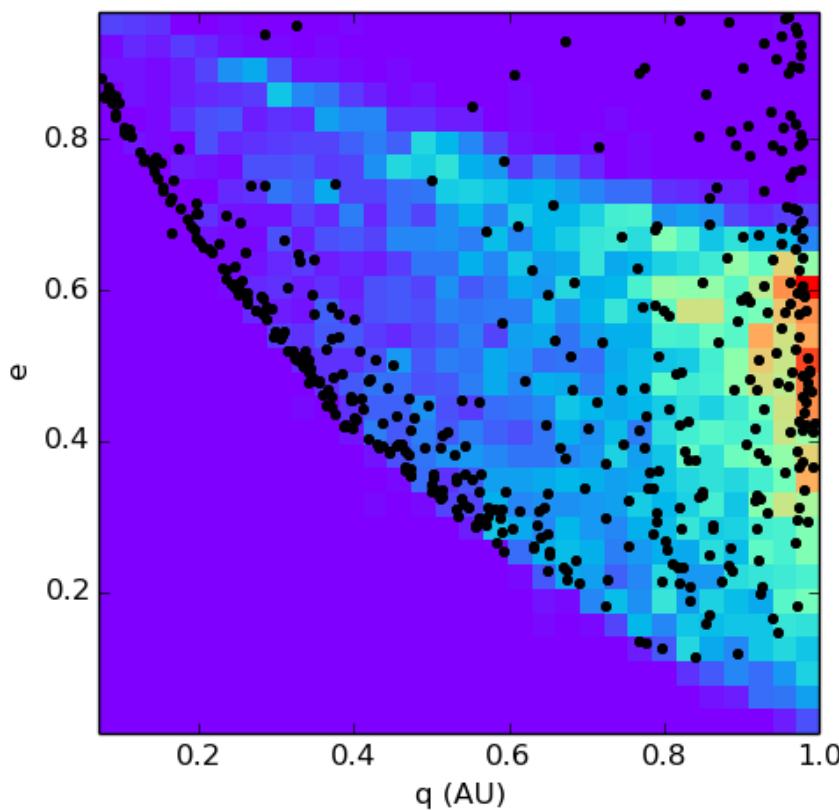
Source distribution for 'hawaii'



GRT: Preliminary results

15 February 2013, 03:20 UTC

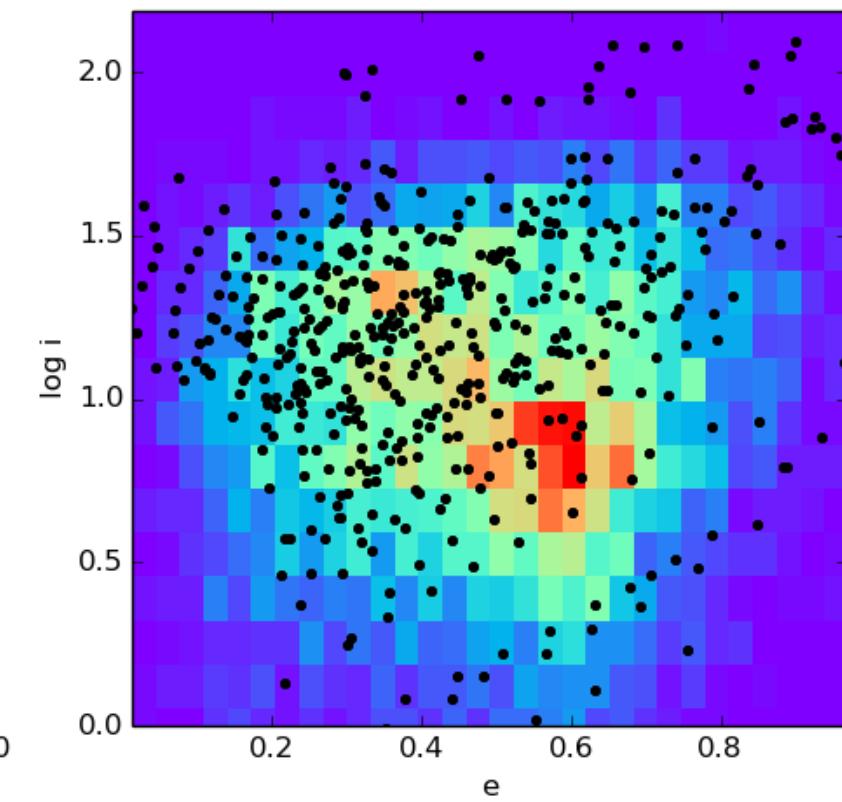
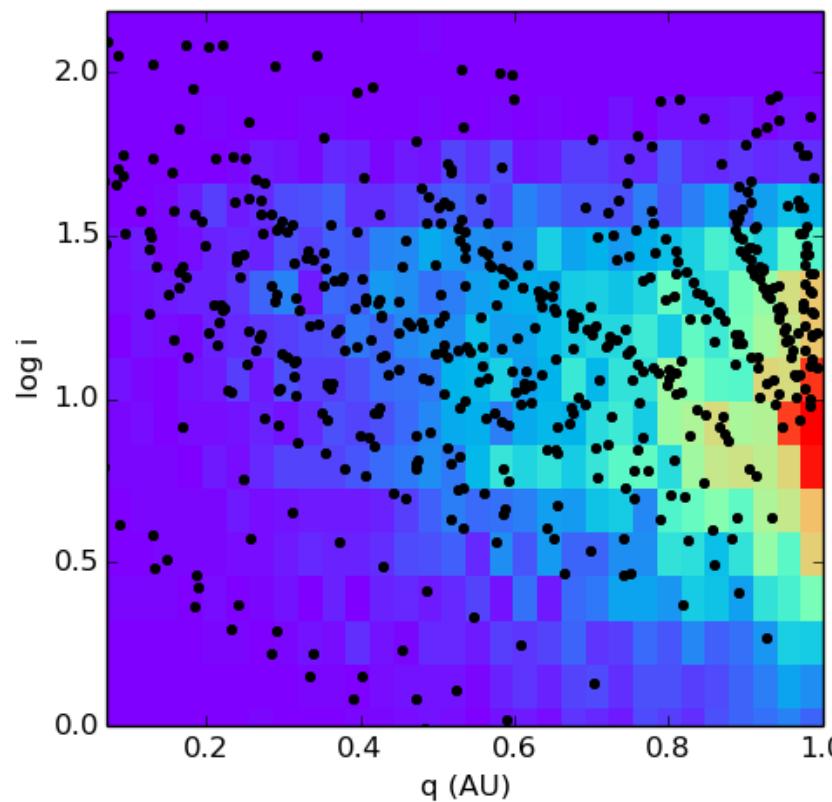
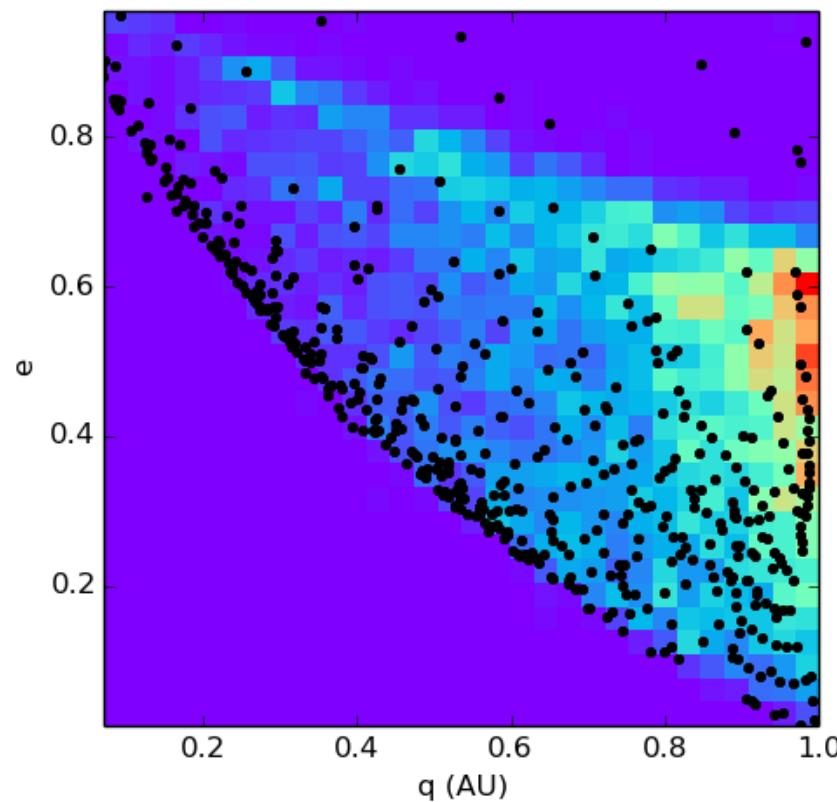
Source distribution for 'chelyabinsk'



GRT: Preliminary results

15 February 2013, 03:20 UTC

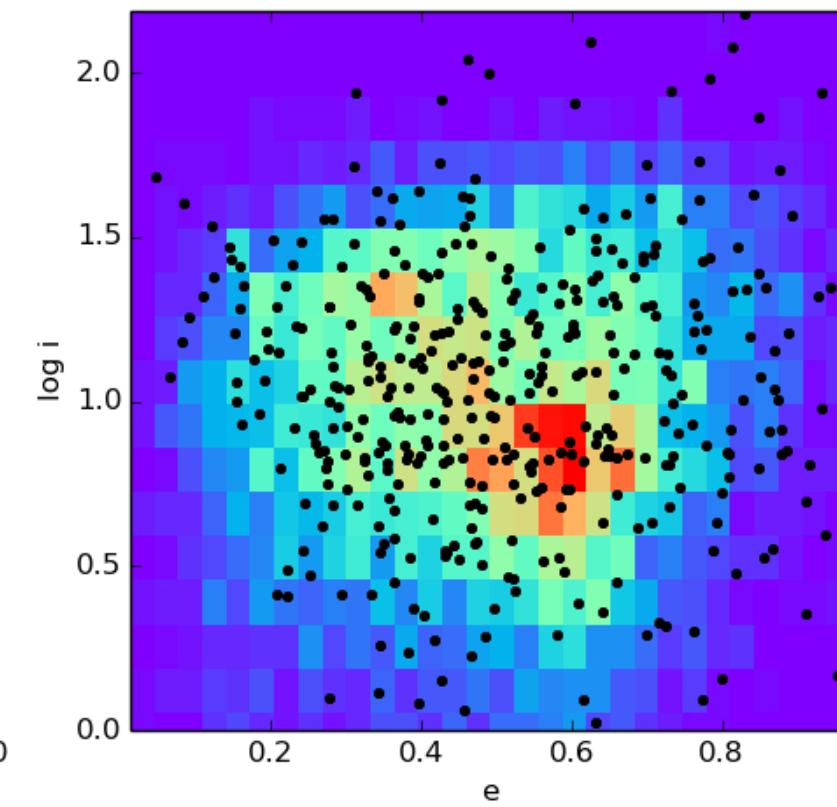
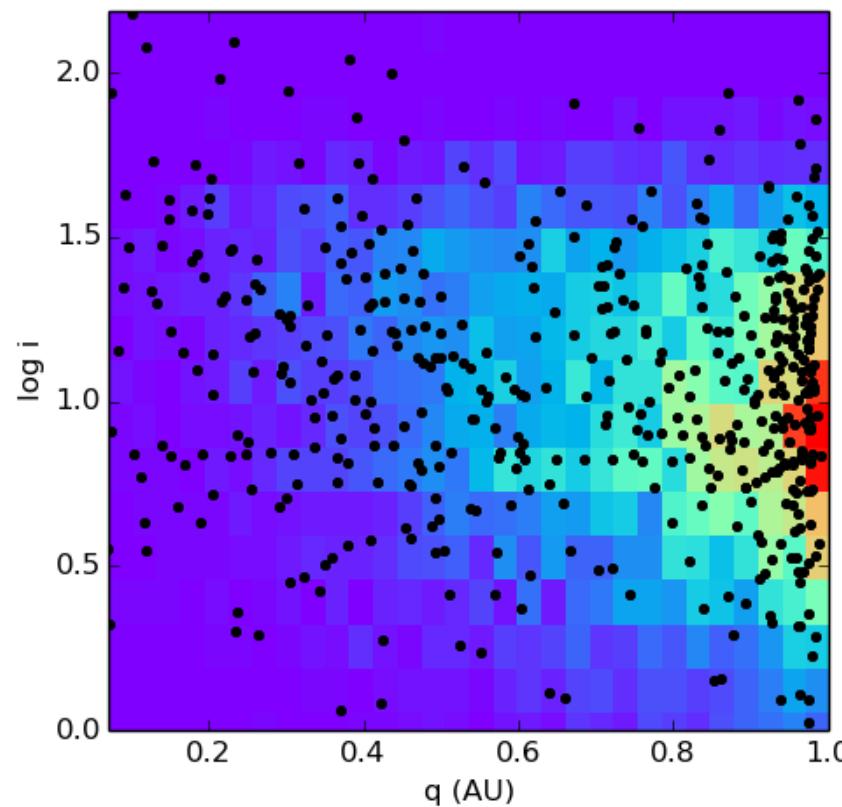
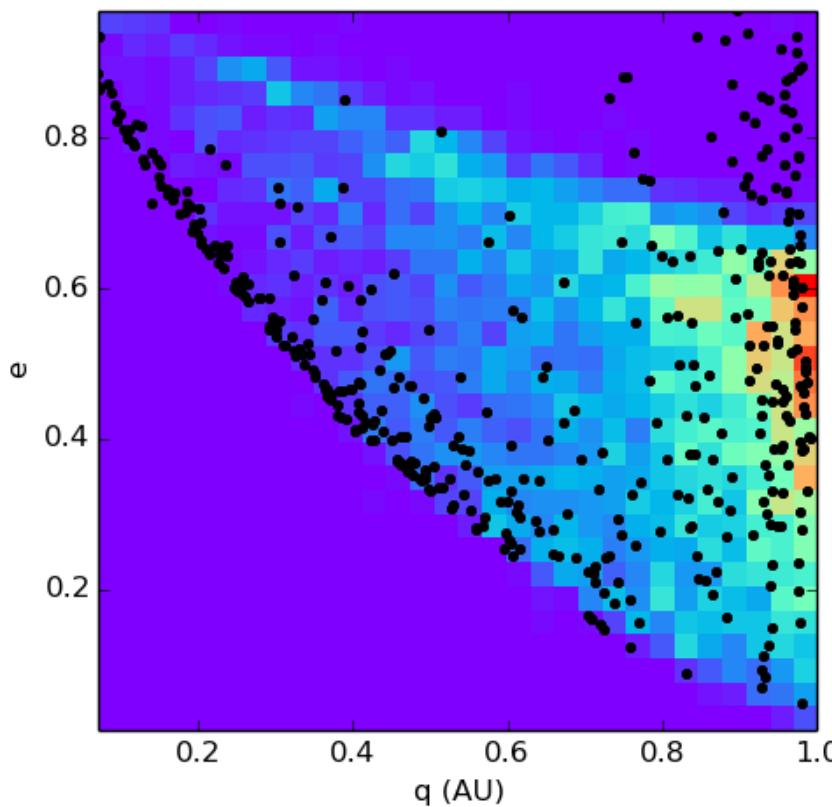
Source distribution for 'madagascar'



GRT: Preliminary results

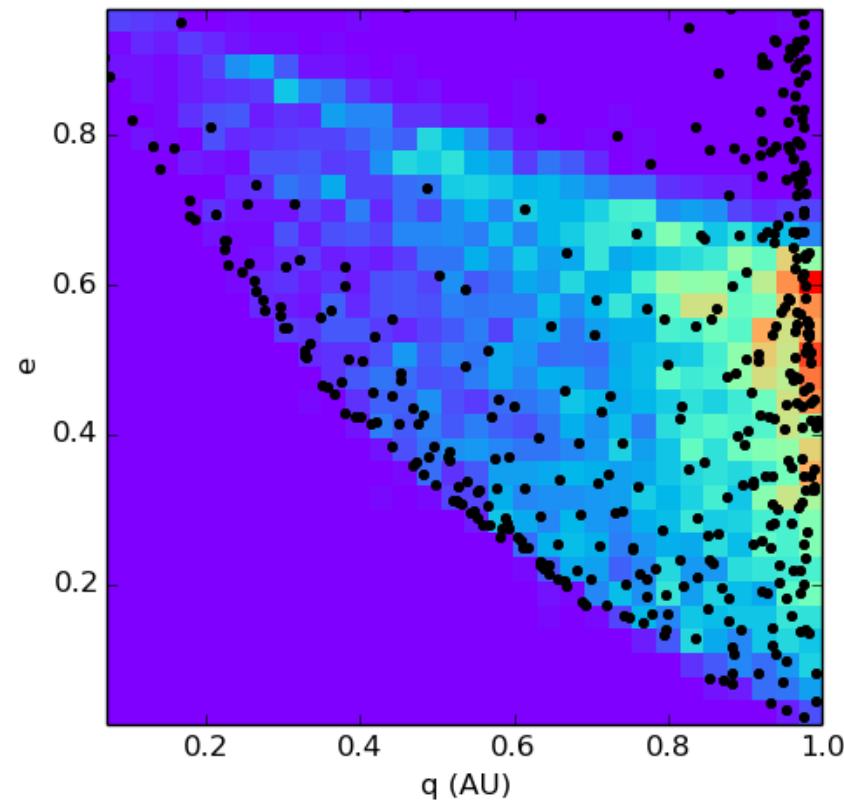
15 February 2013, 03:20 UTC

Source distribution for 'mcmurdo'

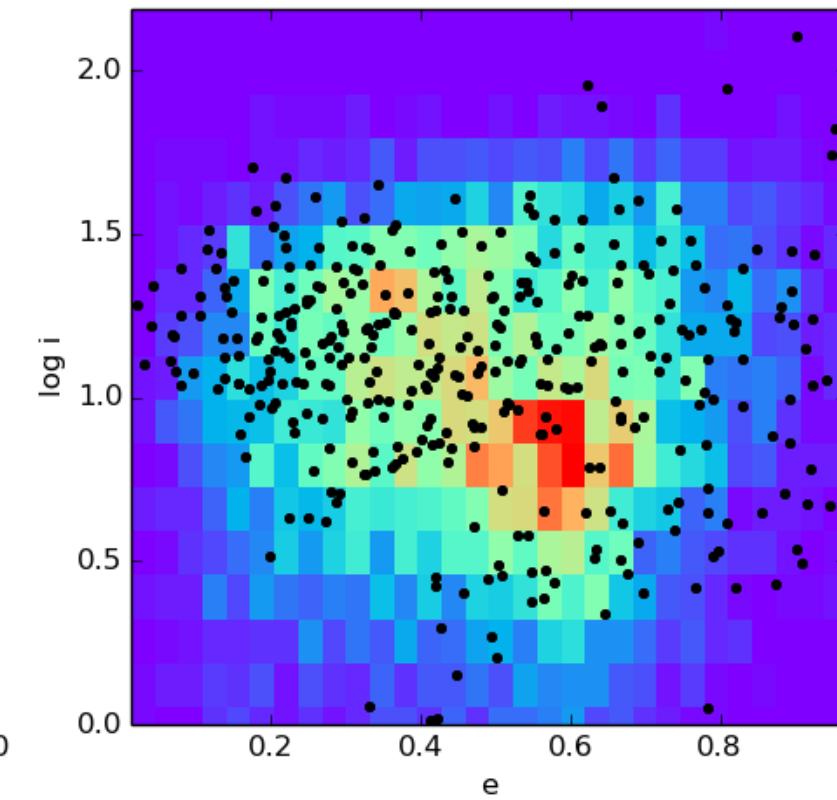
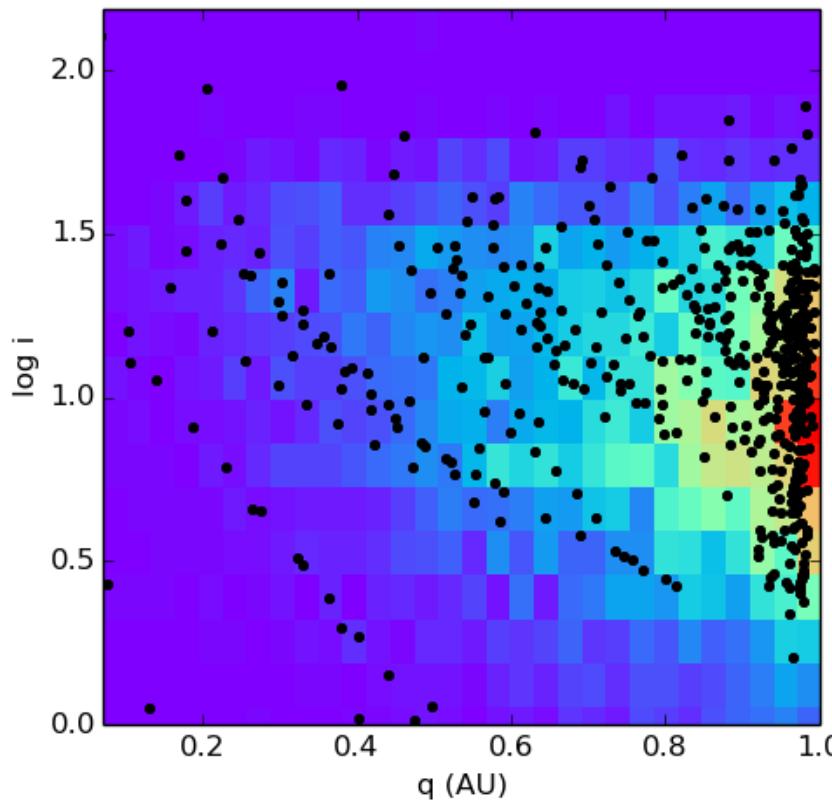


GRT: Preliminary results

15 February 2013, 03:20 UTC



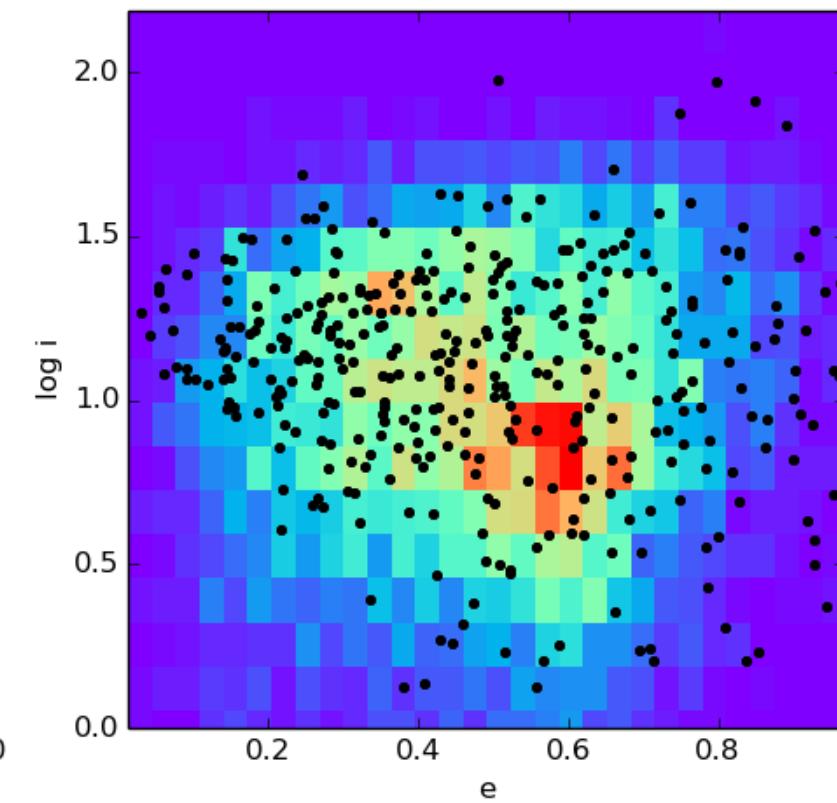
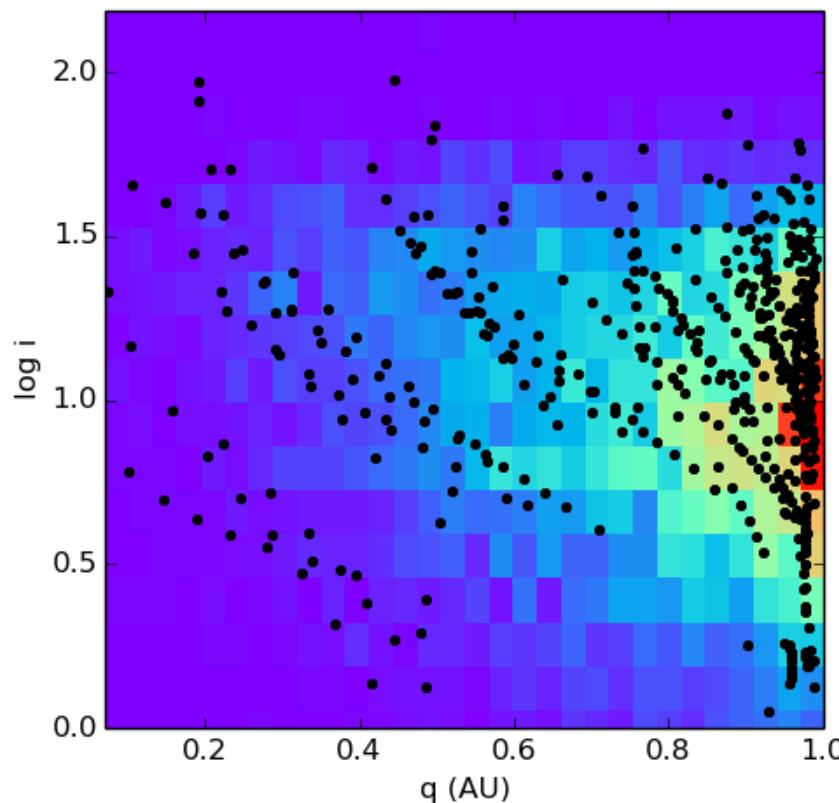
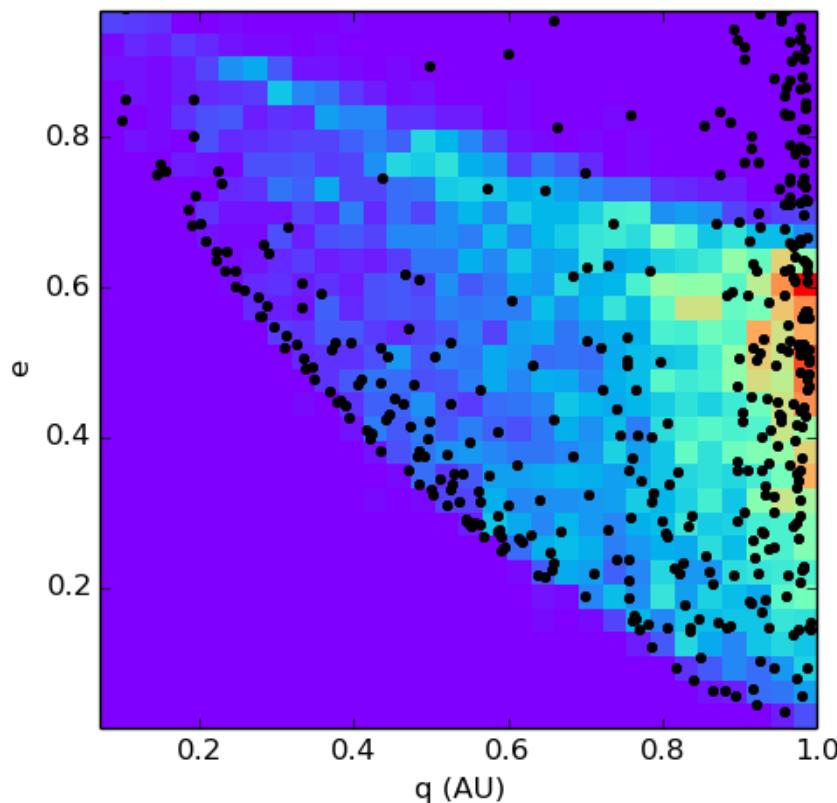
Source distribution for 'medellin'



GRT: Preliminary results

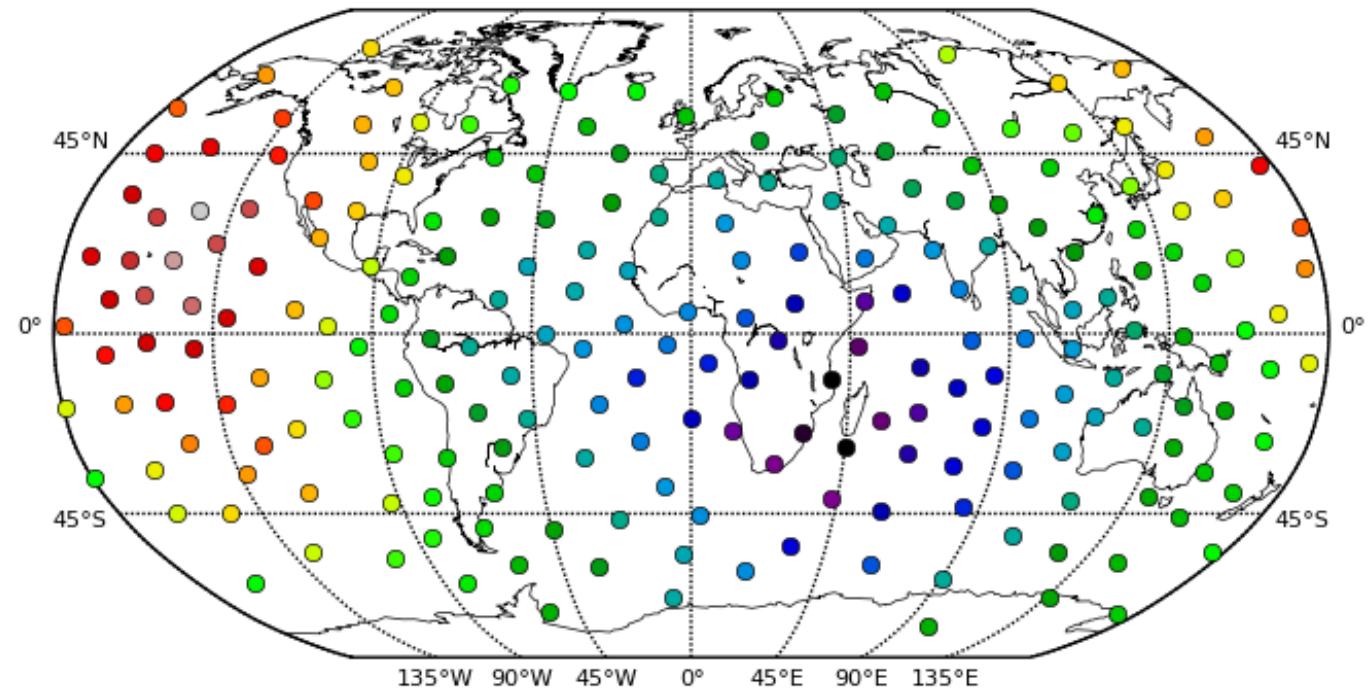
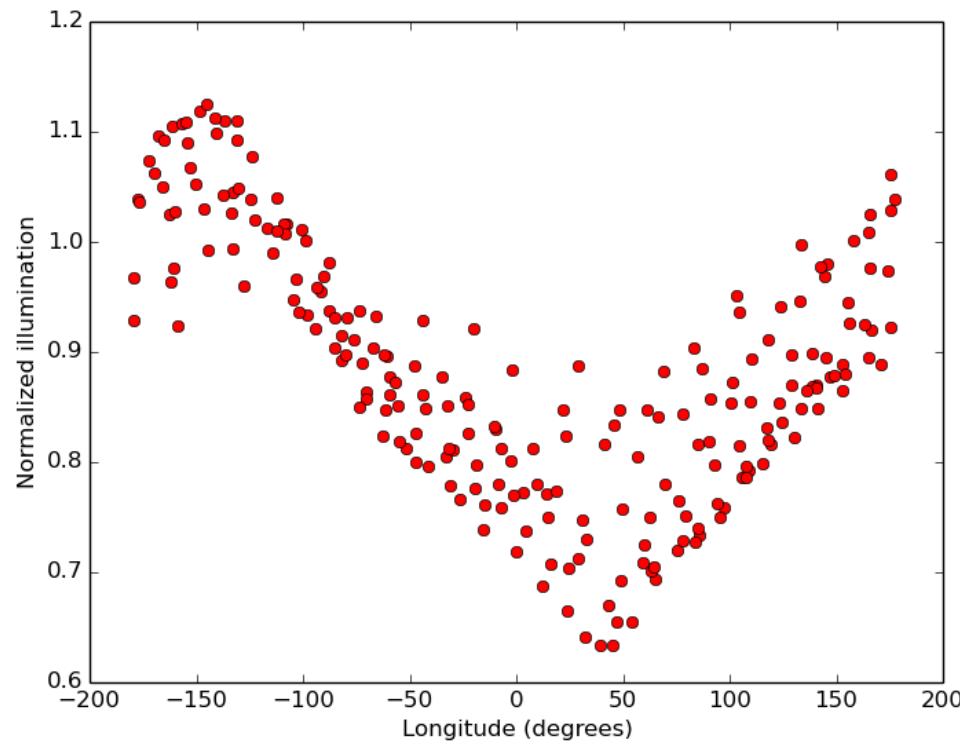
15 December 2013, 03:20 UTC

Source distribution for 'medellin-december'



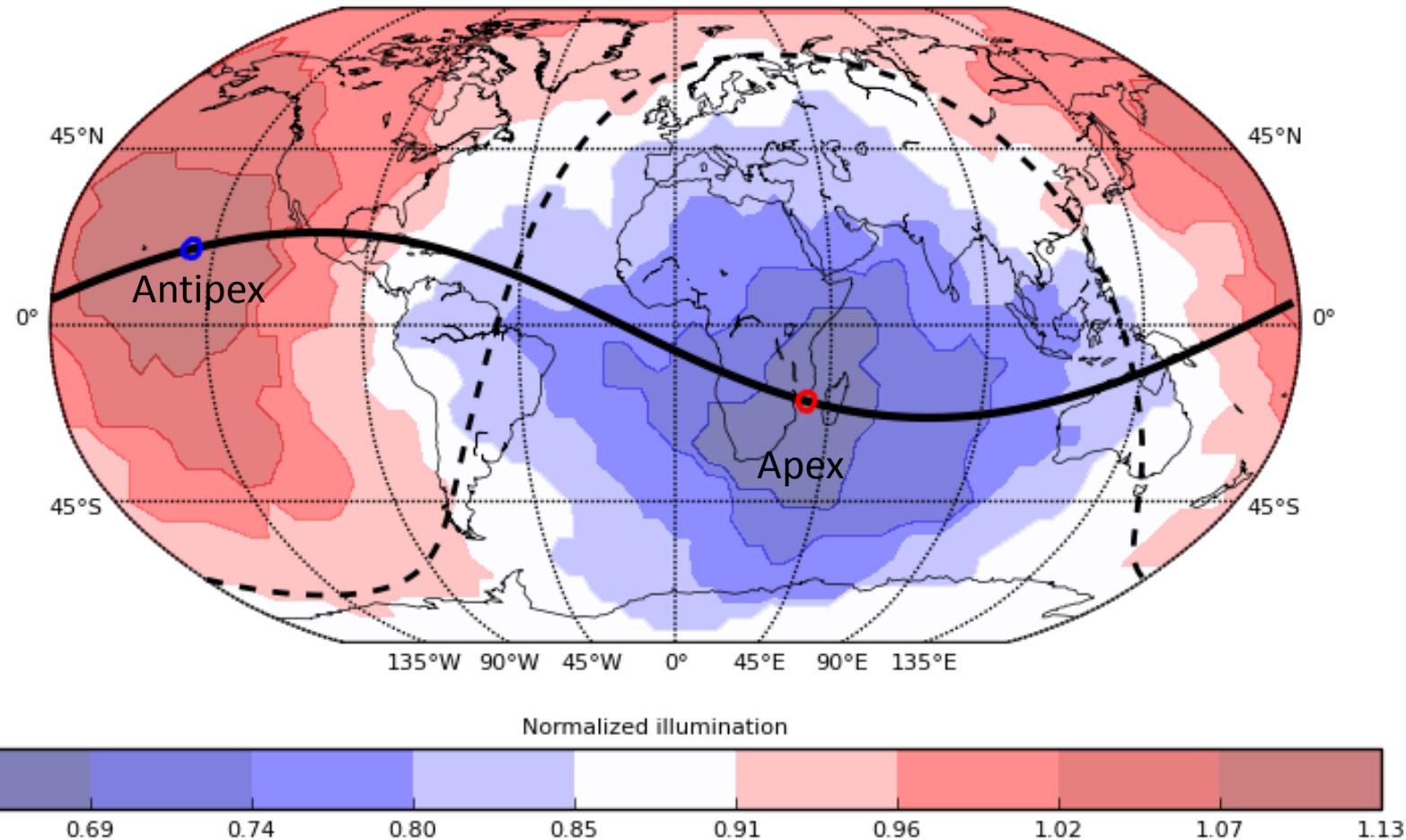
GRT: Preliminary results

15 February 2013, 03:20 UTC



GRT: Preliminary Results

data/ensamble-20130215032034



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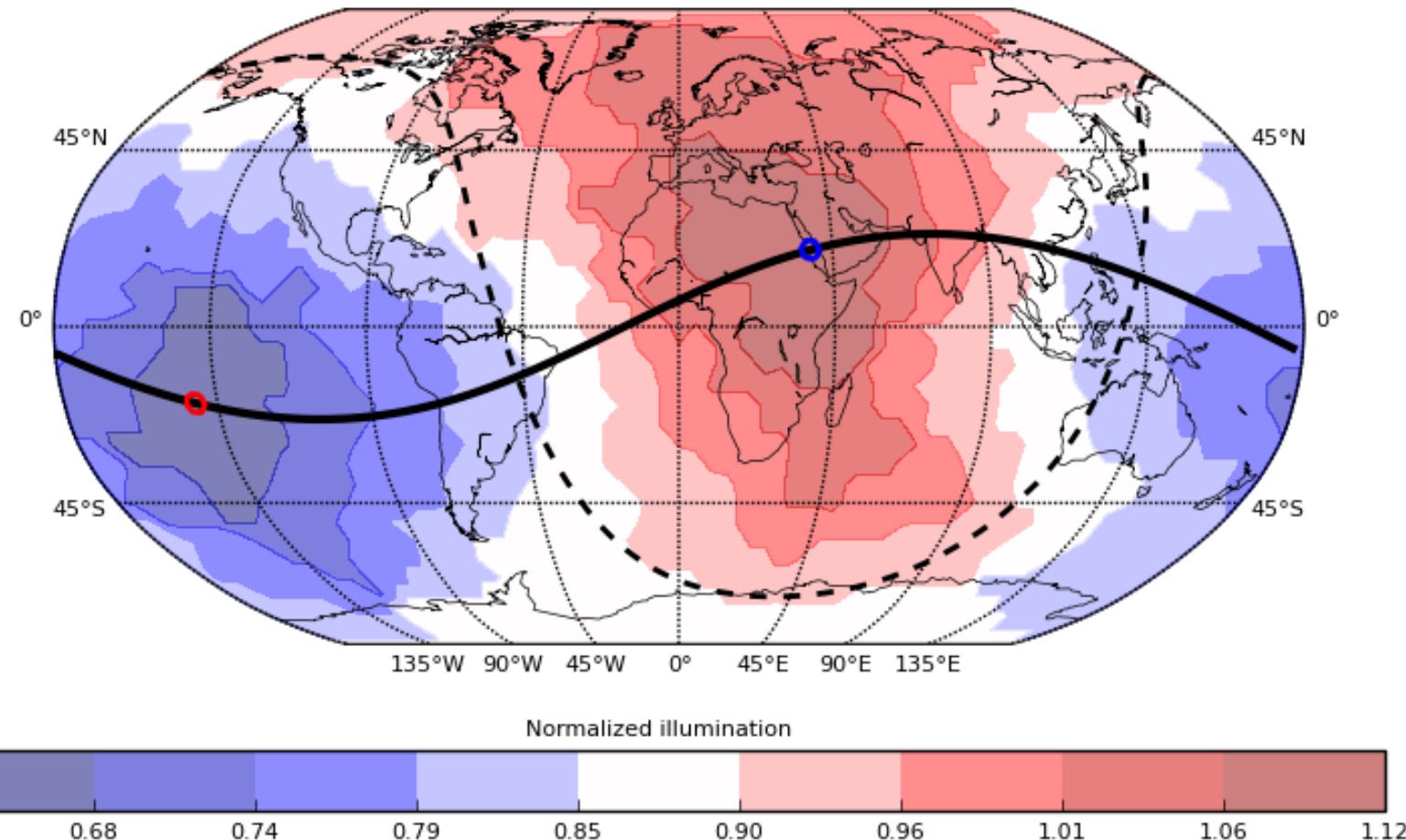
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Zuluaga & Sucerquia, jorge.zuluaga@udea.edu.co
Meteoroids 2016



GRT: Preliminary Results

data/ensamble-20130215152034



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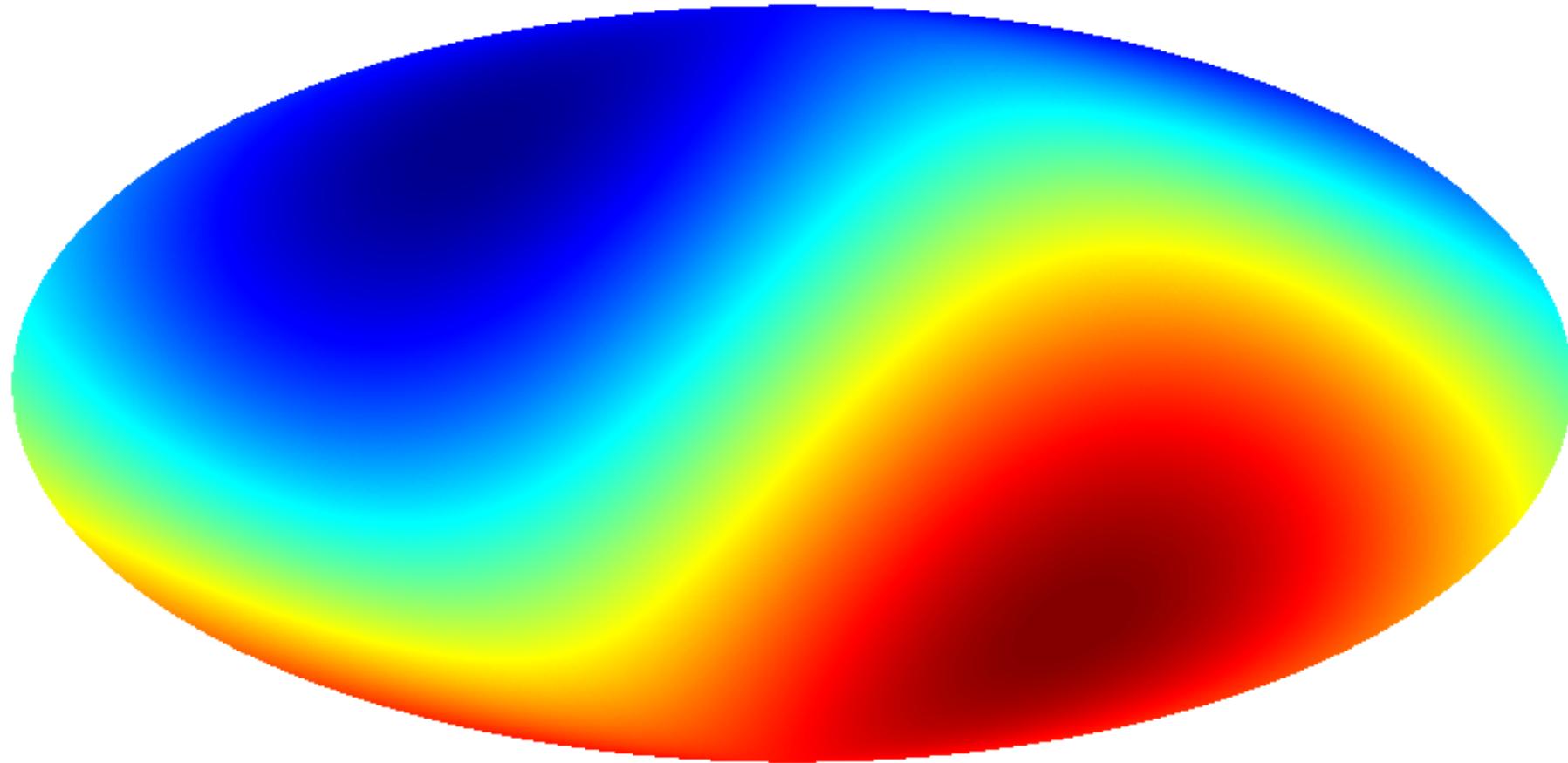


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GRT: Preliminary Results

*An analogy (with cosmology)
The Dipole component of the CMBR*



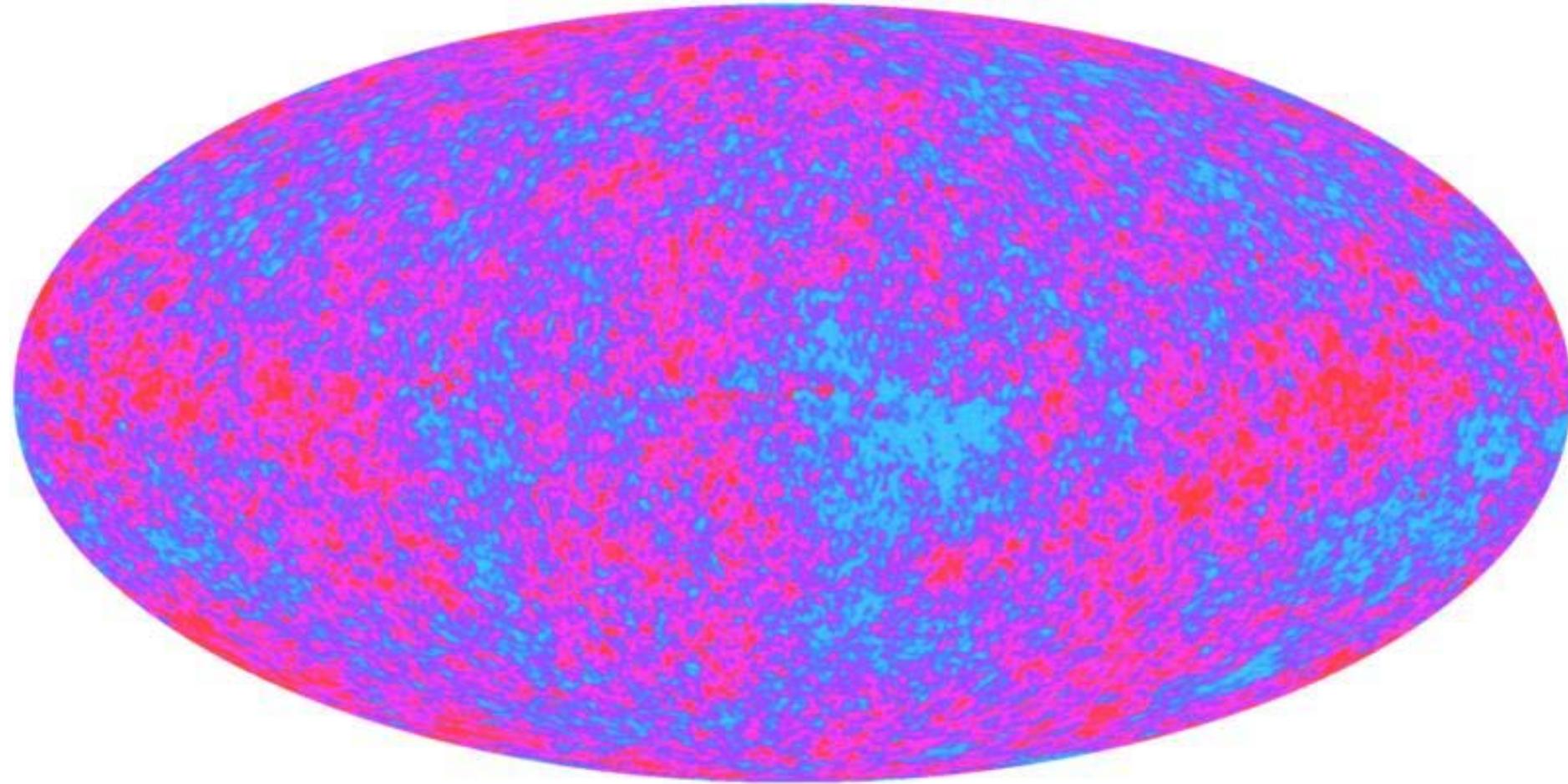
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GRT: Preliminary Results

*An analogy (with cosmology)
We don't want a trivial dipole, we want a signal!*



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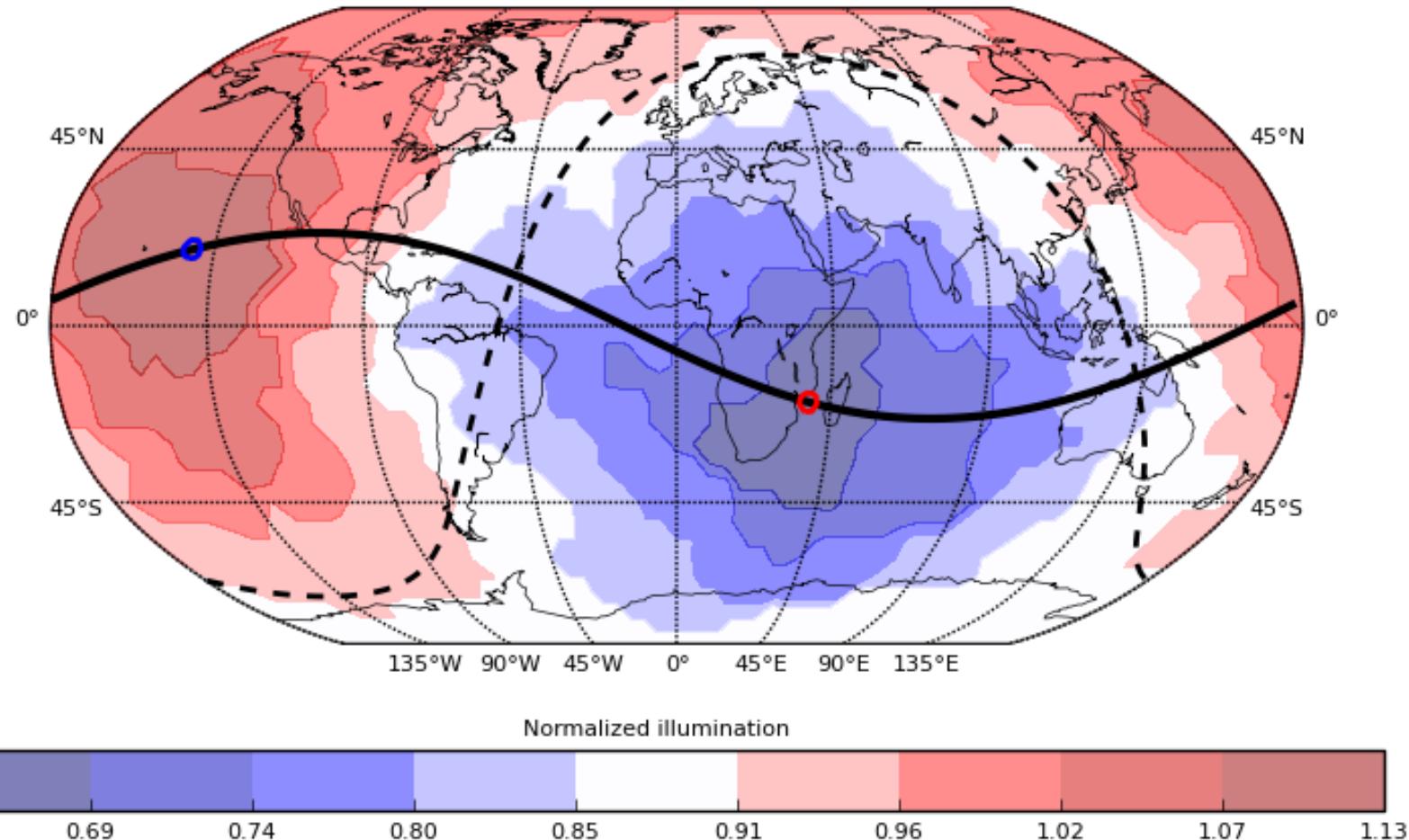


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GRT: Preliminary Results

data/ensamble-20130215032034



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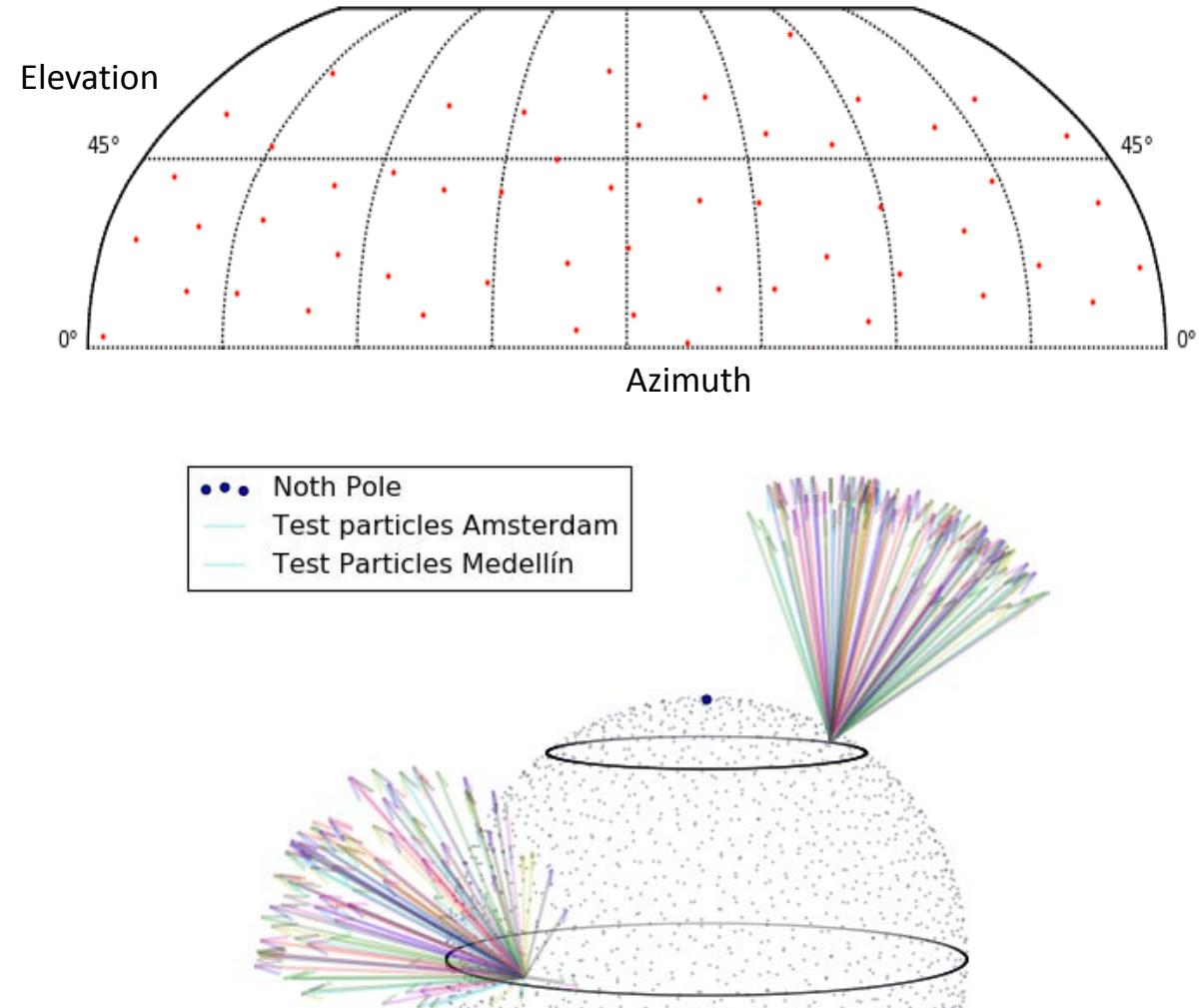
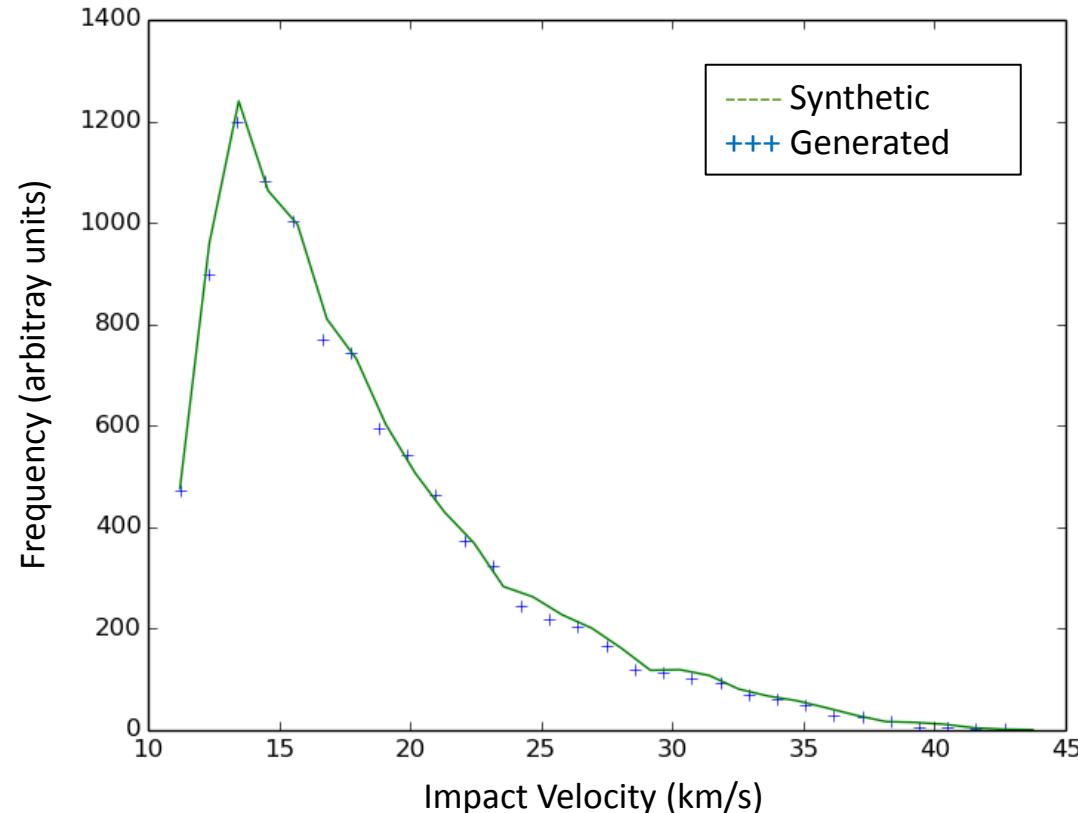


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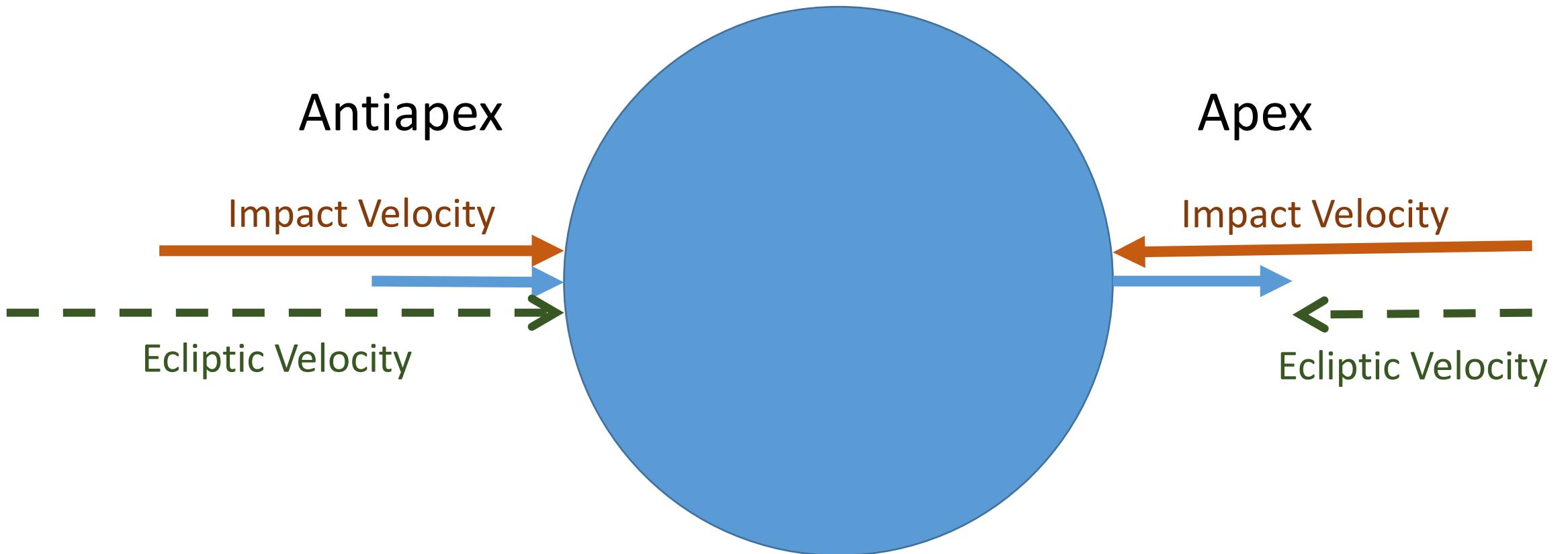


GRT: Initial conditions



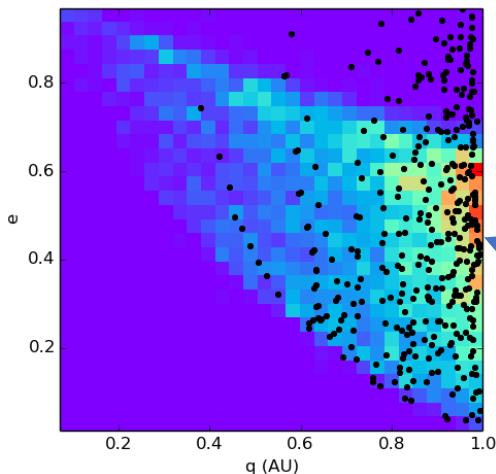
We generate local configuration: Azimuth (A), elevation (a), impact velocity (v)

GRT: Preliminary Results

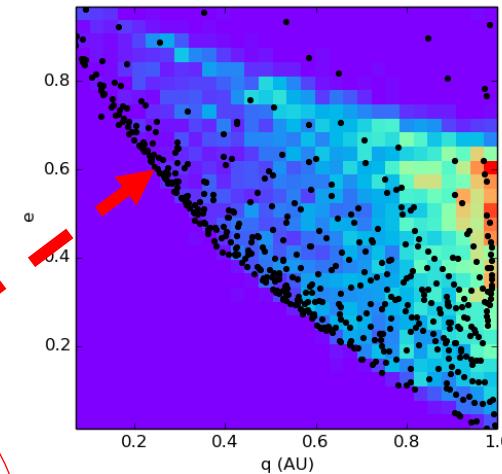


GRT: Preliminary Results

Antiapex Ray

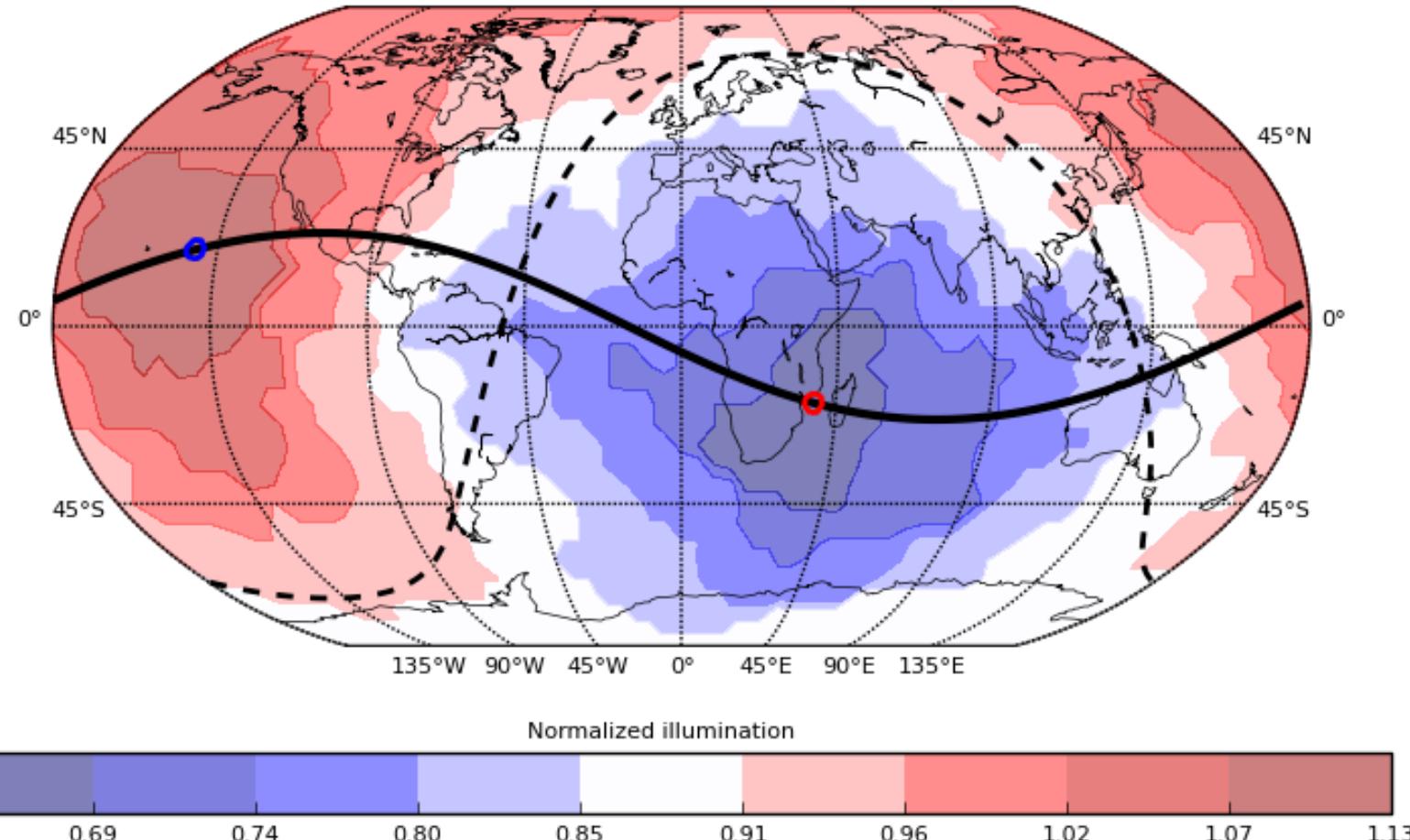


Apex Ray



GRT: Preliminary Results

data/ensamble-20130215032034



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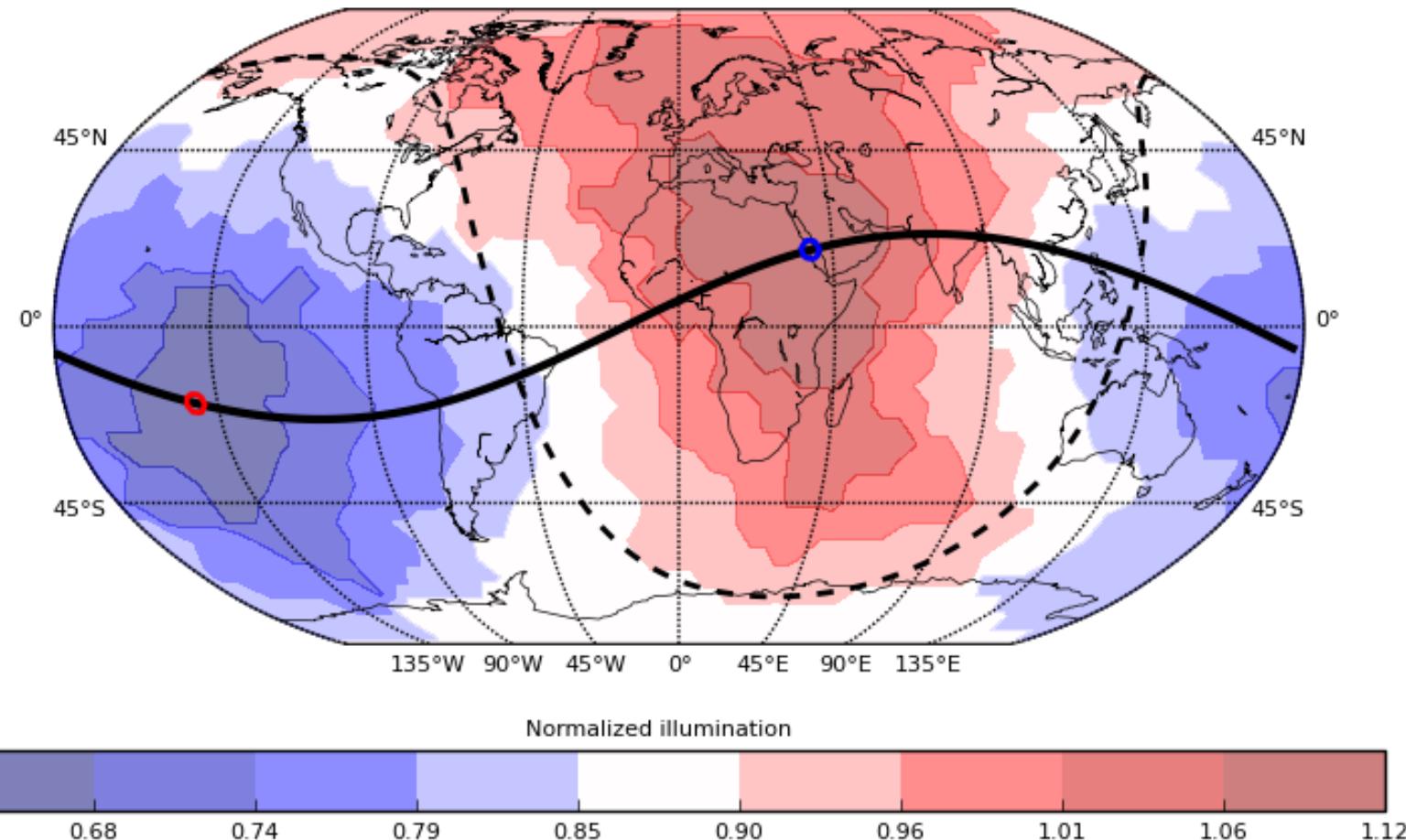


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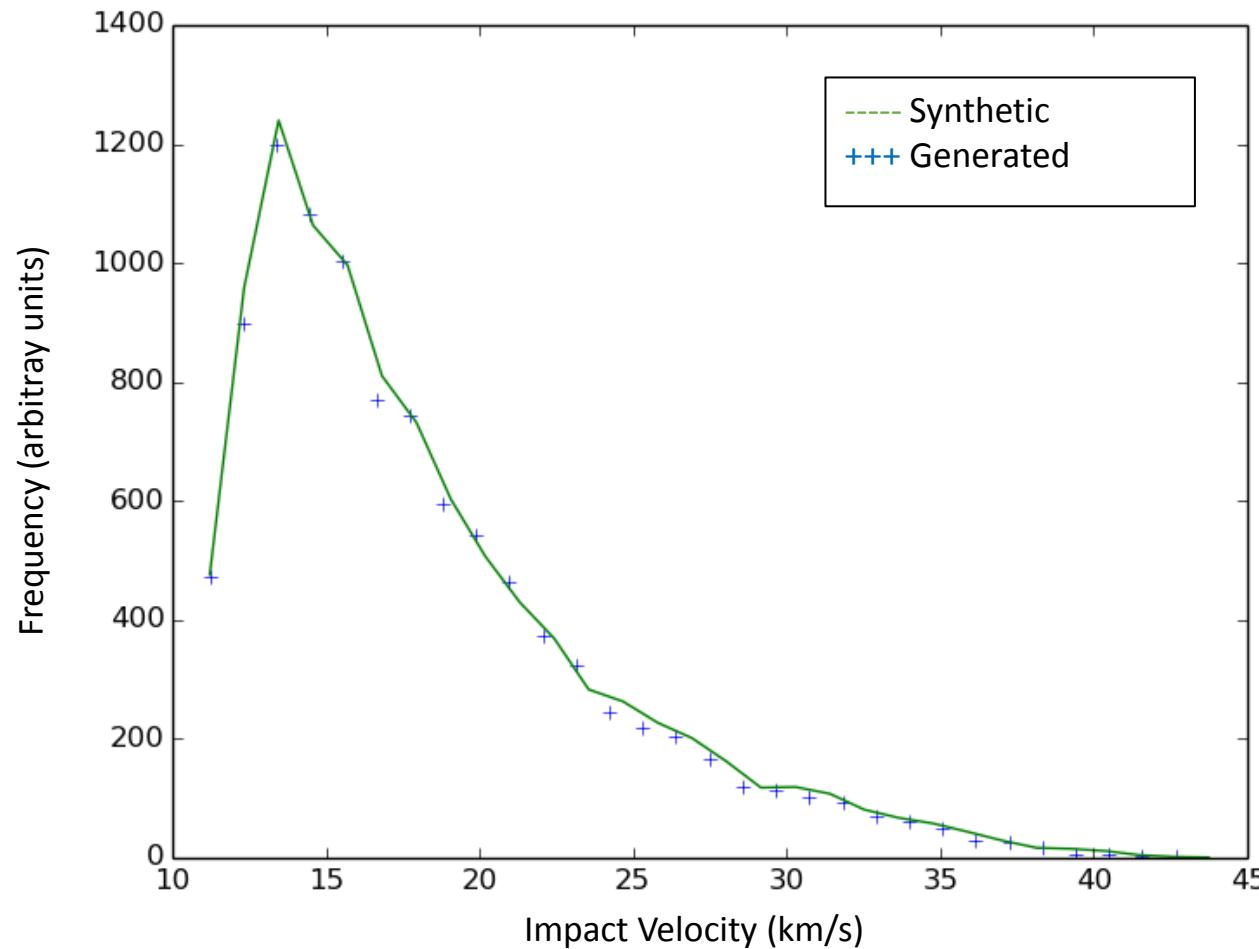


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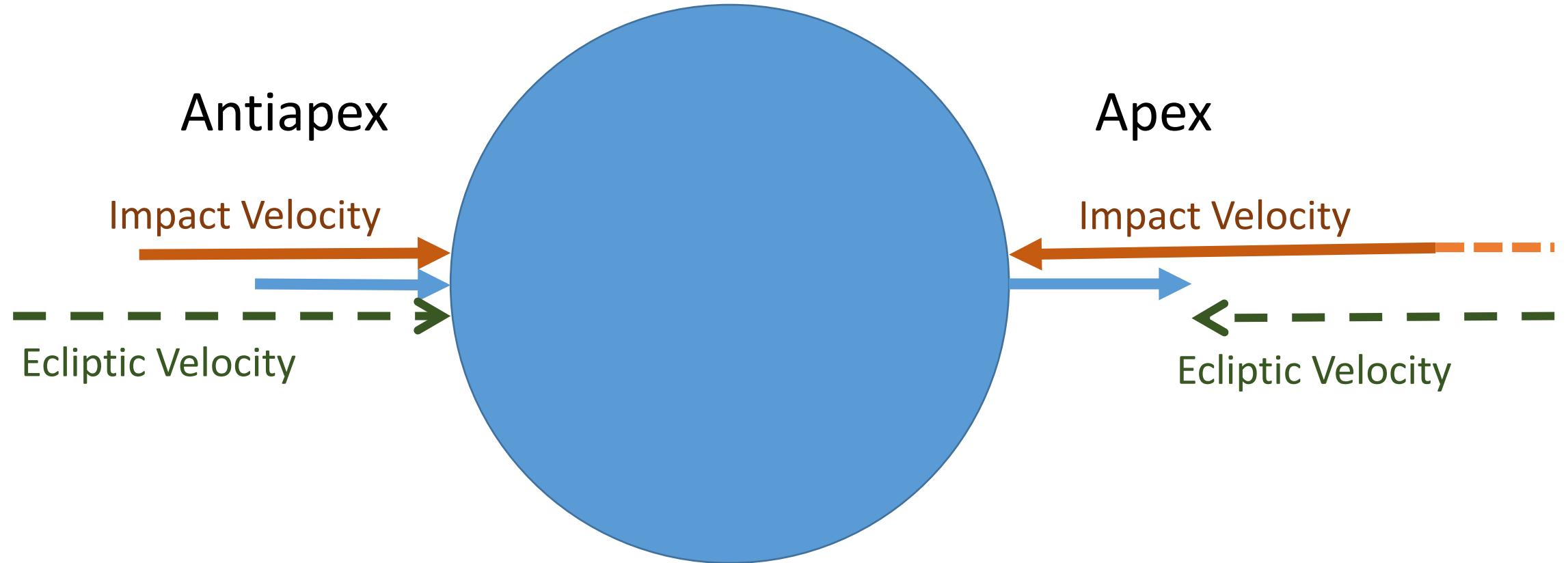
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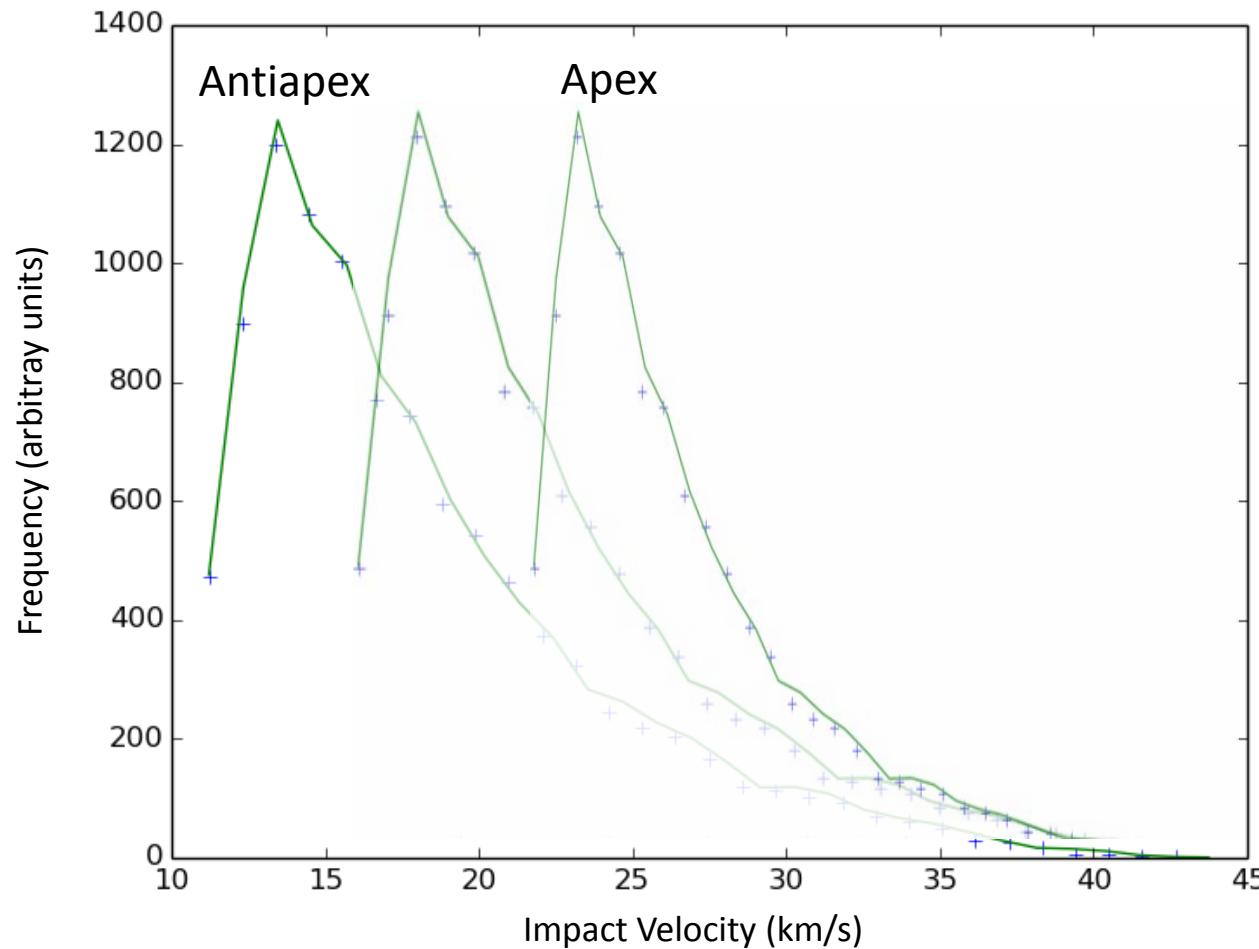


This is the average speed distribution

GRT: Preliminary Results



GRT: Preliminary Results



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Summary and Conclusions

- We [adapted, reinvented, coined the name] of a (new) method to calculate the spatial/temporal distribution of impacts on Earth

Gravitational Ray Tracing

- **Pros:** Complex gravitational settings, efficiency.
- **Contras:** Computationally intensive.
- Range of problems where it can be applied: lunar impacts, rate and differential flux of cratering, Jupiter impacts, temporarily captured objects
- Stay tunned!: <http://github.com/seap-udea>

Questions?



jorge.zuluaga@udea.edu.co

Don't forget to cite us: Zuluaga & Sucerquia (2016)