## Brown Dwạrf Formation from Early Ejection: Resultes from Recent SPH Simulations

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## Stellar Properties

- Distribution of stellar masses
- Observed to be relatively invariant, at least in our Galaxy (Kroupa 200I; Chabrier 2003)
- Star formation rate and efficiency
- Observed to be 3-6\% of gas mass per free-fall time (Evans et al. 2009)
- Fraction of binary and multiple stars
- Observed to be an increasing function of primary mass

- Separations, mass ratios, eccentricities
- High order systems (triples, quadruples)
- Protoplanetary discs
- Masses, sizes, density distributions

Bate 2009a: 500 Mo cloud with decaying turbulence, 35 million SPH particles Follows binaries to I AU, discs to ~10 AU
Forms I254 stars and brown dwarfs - best statistics to date from a single calculation

## Radial Distributions of Properties

- The calculation produces a very dense cluster
- Half-mass radius is just I0,000 AU (0.05 pc)
- No significant mass segregation in the cluster or halo
- Contrary to the usual picture of competitive accretion, perhaps due to the recent mergers of sub-clusters
- Binary fractions decrease \& velocity dispersion increases
- But only outside 3 half-mass radii
- Kohler et al. 2006 investigated ONC binaries at I-2 half-mass radii



| Quantity / Distance range | $<1000 \mathrm{AU}$ | $1000-3000 \mathrm{AU}$ | $3000-10^{4} \mathrm{AU}$ | $1-3 \times 10^{4} \mathrm{AU}$ | $3-10 \times 10^{4} \mathrm{AU}$ | $>1 \times 10^{5} \mathrm{AU}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Median mass $\left[\mathrm{M}_{\odot}\right]$ | 0.18 | 0.024 | 0.035 | 0.056 | 0.054 | 0.045 |
| Upper quartile mass $\left[\mathrm{M}_{\odot}\right]$ | 0.30 | 0.091 | 0.098 | 0.15 | 0.18 | 0.095 |
| Maximum mass $\left[\mathrm{M}_{\odot}\right]$ | 5.3 | 2.9 | 3.7 | 2.5 | 2.1 | 2.0 |
| Velocity dispersion $[\mathrm{km} / \mathrm{s}]$ | 6.1 | 4.0 | 4.2 | 4.3 | 8.2 | 13.8 |
| Number objects | 8 | 56 | 569 | 408 | 172 | 41 |
| Number binaries | 2 | 8 | 68 | 55 | 13 | 0 |
| Binary fraction | 0.33 | 0.167 | 0.136 | 0.156 | 0.082 | 0.0 |

## Velocity Dispersion

- No strong dependence of stellar velocities on stellar mass
- VLM objects have a smaller velocity dispersion than stars (80\%) (c.f. Joergens)
- Binaries have $\sim 60 \%$ of the velocity dispersion of single stars


Stellar Mass Distribution

- Competitive accretion/ejection gives
- Salpeter-type slope at high-mass end
- Low-mass turn over
- $\sim 4$ times as many brown dwarfs as a typical star-forming region
- Not due to sink particle approximation - results almost identical for different sink parameters



## IMF: Competitive Accretion and Ejection

- Stars and brown dwarfs
- Form with opacity limited masses, accrete to larger masses
- Final masses depend on how long they accrete
- Accretion typically terminated by ejection




Multiplicity as a Function of Primary Mas ${ }^{7^{2}}$

- Multiplicity fraction $=(\mathrm{B}+\mathrm{T}+\mathrm{Q}) /(\mathrm{S}+\mathrm{B}+\mathrm{T}+\mathrm{Q})$
- Observations: Close et al. 2003; Basri \& Reiners 2006; Fisher \& Marcy 1992; Duquennoy \& Mayor I991; Preibisch et al. I999; Mason et al. 1998



## Dependence of Multiplicity on Sink Particle Radius

- Decreasing the sink particle accretion radius slightly increases the VLM binary frequency

Accretion radius: 5 AU
Accretion Radius: 0.5 AU


## Star/VLM Object Separation Distributions

Stars: binary, triple, quad separations
Median separation: 26 AU

VLM objects: binaries, triples, quads
Median separation: IO AU


Solid line: Duquennoy \& Mayor I99|

## Star/VLM Object Separation Distributions

- Distributions depend on sink particle size
- Reducing sink particle size from 5 to 0.5 AU
- Produces log-normal stellar separation distribution
- Increases binary fraction for VLM objects
- Also separations ofVLM objects decrease with time






## Star/VLM Object Binary Mass Ratio Distributions

Stars: M>0.5 M๑
$59 \%$ have $\mathrm{q}>0.6$

Stars: $0.1<\mathrm{M}<0.5 \mathrm{M}_{\odot}$
$51 \%$ have $q>0.6$

VLM objects: $\mathrm{M}<0.1$ M○

71\% have $q>0.6$




## VLM Binary Eccentricity Distribution

- Trent Dupuy: presented first eccentricity distribution for VLM binaries
- Tend to have low eccentricities

Observations
Calculation (accretion radii 0.5 AU )



## VLM Companions to Stars

- Frequency of $\sim 10 \%$
- Independent of primary mass (from 0.I Mo up to solar masses)
- BUT, typical separation increases with primary mass
- 0.I-0.2 Mo: $3 / 14$ systems have separations $<30 \mathrm{AU}$
- 0.2-0.5 Mo: 3 at < $10 \mathrm{AU}, \quad \mathrm{I}$ at $50 \mathrm{AU}, 3$ at $>1000 \mathrm{AU}$
- 0.5-0.8 M○: 3 with separations 27-65 AU
- Solar type primaries: 2 cases, both with separations >1000 AU
- Impossible to examine increased frequency of binary VLM companions to stars with current statistics
- Stamatellos \& Whitworth 2009 type simulations


## Discs: Closest Encounter Distance

- Dense star cluster produces many close encounters, truncating discs
- All stars > \| Mo have had encounters closer than 2 AU
- Doesn't mean don't have discs - if not ejected, discs often re-form through accretion
- Brown dwarfs: encounter distances from < I AU to > 100 AU
- Those without close encounters may have large discs




## Hydrodynamical Star Formation

- Can now perform simulations that form large numbers of objects
- Statistical uncertainties are the same as from observations
- Comparison with observations shows what we get right and wrong
- Many properties and trends are in good agreement with observations
- General form of the IMF
- Multiplicity with primary mass
- Trends for separation and mass ratio distributions
- Orbital planes of triple systems
- Two glaring inconsistencies:
- Too many brown dwarfs
- To few wide, unequal mass solar-type binaries
- Need to move on with additional physics

Star Cluster Formation with Radiative Feedbaclere

- Repeat Bate, Bonnell \& Bromm 2003, Bate \& Bonnell 2005
- 50 Mo molecular clouds, Decaying `turbulence' $\mathrm{P}(\mathrm{k}) \propto \mathrm{k}^{-4}$
- Diameters 0.4 pc and 0.2 pc , Mean thermal Jeans masses I Mo and I/3 M๑
- 3,500,000 SPH particles
- Sink particles
- Radiative transfer calculations: Sink Radii 0.5 AU, no gravitational softening
- Radiative transfer
- Implicit, grey flux-limited diffusion
- Separate radiation and matter temperatures, but assumes gas = dust temperature
- See poster by Andrea Urban (S266)
- No feedback from protostars
- Intrinsic protostellar luminosity unimportant
- Accretion luminosity underestimated (energy liberated from 0.5 AU to stellar surface)
- Gives a lower limit on the effects of radiative feedback



## BBB2003:Typical cloud: Jeans mass I Mo, P(k) $\propto \mathrm{k}^{-4}$ <br> with Radiative Transfer



## Impact of Radiative Feedback

- Bate, Bonnell \& Bromm (2003)
- "Typical" density 50 Mo molecular cloud ( $\sim 10^{4} \mathrm{~cm}^{-3}$ )

|  | Stars | Brown Dwarfs | Total |
| :---: | :---: | :---: | :---: |
| Barotropic Equation of State | 23 | 27 | $50 \quad\left(1.40 \mathrm{t}_{\mathrm{f}}\right)$ |
| Radiative Transfer | 11 | 2 | 13 |
| $\left.1.40 \mathrm{t}_{\mathrm{f}}\right)$ |  |  |  |

- Bate \& Bonnell (2005)
- Denser 50 Mo cloud ( $\sim 10^{5} \mathrm{~cm}^{-3}$ )

|  | Stars | Brown Dwarfs | Total |
| :---: | :---: | :---: | :---: |
| Barotropic Equation of State | 19 | 60 | $79 \quad(1.40 \mathrm{tfif})$ |
| Radiative Transfer | 14 | 3 | $17 \quad\left(1.40 \mathrm{tff}_{\mathrm{f}}\right)$ |

## Radiative Feedback and the IMF

- Radiative feedback brings the star to brown dwarf ratio in line with observations
- Observations suggest a ratio of $5 \pm 2$
- Chabrier 2003; Greissl et al. 2007; Luhman 2007;Andersen et al. 2008
- Simulations: 25:5 ~ 5
- Bate 2009b
- Furthermore, dependence of the IMF cloud density is removed
- K-S test on the two IMFs with radiative shows them to be indistinguishable


Large-scale Simulations with Radiative Feedbaclere

- Currently re-running Bate (2009a) with radiative feedback
- 500 Mo cloud, using $35,000,000$ SPH particles
- Resolves opacity limit for fragmentation
- Follows:
- All binaries $(0.02 \mathrm{AU})$ and discs to $\sim \mathrm{I}$ AU radius
- Results so far
- Just reached I. 06 initial cloud free-fall times
- Formed 89 stars and brown dwarfs
- Including I binary brown dwarf system: I5 AU separation, 0.04 eccentricity
- Original calculation at the same time: $\sim 300$ stars and brown dwarfs




## Large-scale Simulations with Radiative Feedbaclere

- Comparison of the IMFs obtained without and with radiative feedback
- As expected, many fewer brown dwarfs
- Stars to brown dwarfs without radiative feedback: 74:154~I/2 vs with feedback 42:22 ~ 2
- Remains to be seen how other stellar properties compare


- The Future:
- Self-gravitating radiation magnetohydrodynamical simulations
- Statistics as good or better than observational surveys
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