

$$U(r) = c_1 \frac{GM_{\text{BH}}}{r} - \frac{(1 - c_1)GM_{\text{BH}}}{r - c_2 r_{\text{g}}} - \frac{c_3 GM_{\text{BH}}}{r} \frac{r_{\text{g}}}{r}$$