

$$r_t = \left( \frac{M_{\text{BH}}}{n_*} \right)^{1/3} r_*$$