

Gamma-ray emission from Crab pulsar and Nebula: paradigm shifts?

Maxim Lyutikov (Purdue U., CITA)

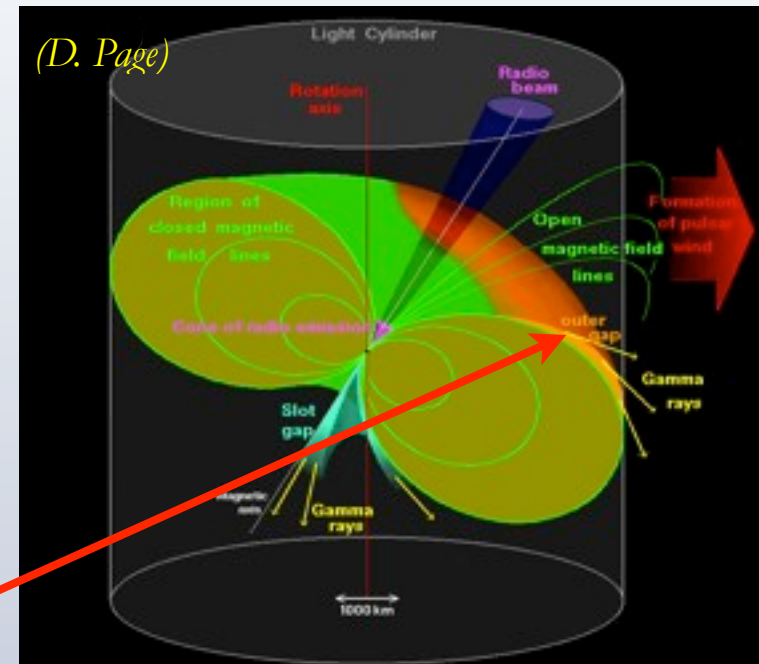
I. Gamma-ray emission from pulsars

Gamma-rays: Outer/slot gaps: messy physics, good fits geometrical

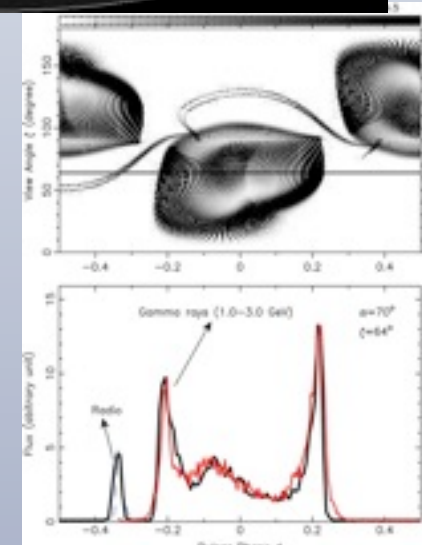
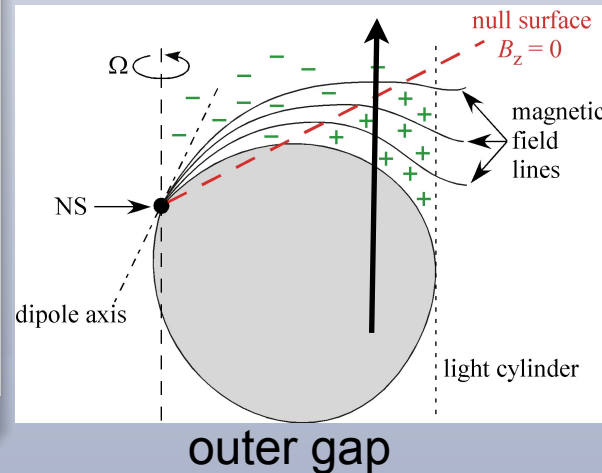
Chen & Rudernman 86

- vacuum dipole (Romani +)
- force-free models (Spitkovsky)
- caustics: dipole + sweep-back + magnetospheric currents + aberration + time of flight

production of gamma-rays
(Chen & Ruderman 1986)



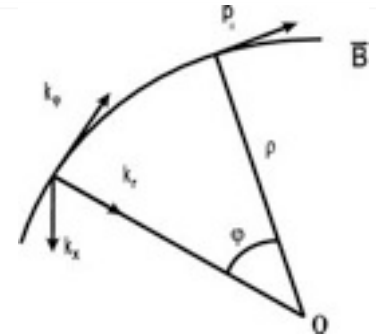
- Rotation induces charge density in the magnetosphere
- $E_{||}$ accelerates particles which emit



Emit what?

- Curvature emission (Chen & Ruderman 1986)

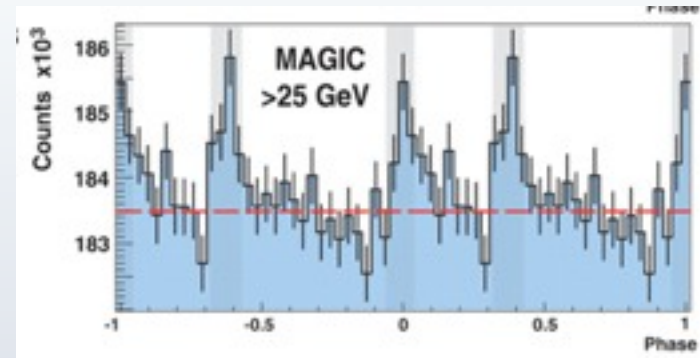
$$\epsilon_{ph} = \frac{\hbar \gamma^3 c}{R_C}$$



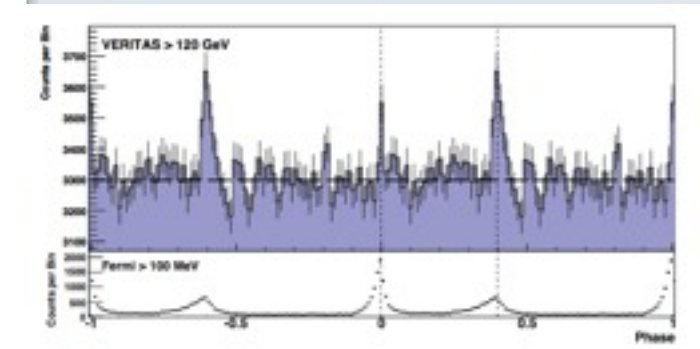
- Hard to solve the full electrodynamic picture: **there is no kinetic model of pulsar magnetosphere**
- $E_{||}$ accelerates particles, produce pairs and currents, pairs screen $E_{||}$, currents distort B-field, changing $E_{||}$, non-local radiative transfer.
- Typically $E_{||} \sim 10^{-2}-10^{-1}$ B
- Maximal $\gamma \geq 10^7$ for primary beam is needed for Crab
- **Clear prediction: above the break the spectrum must be exponentially suppressed**

Crab at VHE

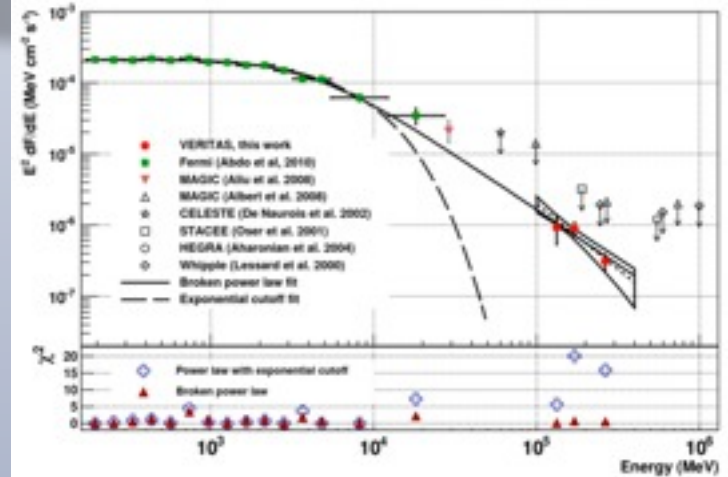
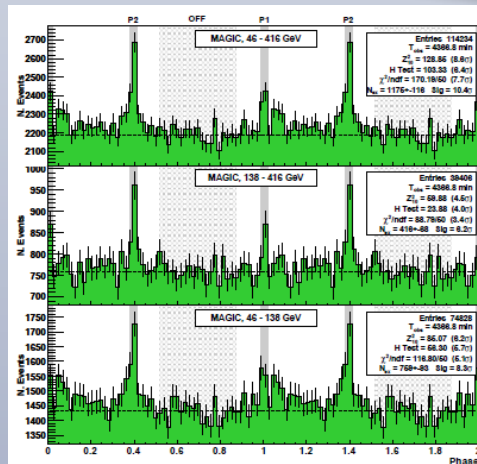
- MAGIC sees Crab at 25 GeV
- Not enough by factor ~ few



- VERITAS sees Crab at > 150 GeV!
- Cut-off is non-exponential(!): Power-law
- IP is brighter than MP



MAGIC:
Crab at 500GeV



Curvature emission near light cylinder is excluded

Lyutikov + 2012

- Astrophysical E-fields < B-field
- Equate acceleration by $E_{\parallel} = \eta (r/R_{LC}) B$ to curvature losses in $R_C = \xi R_{LC}$

Maximum possible energy break due to curvature emission

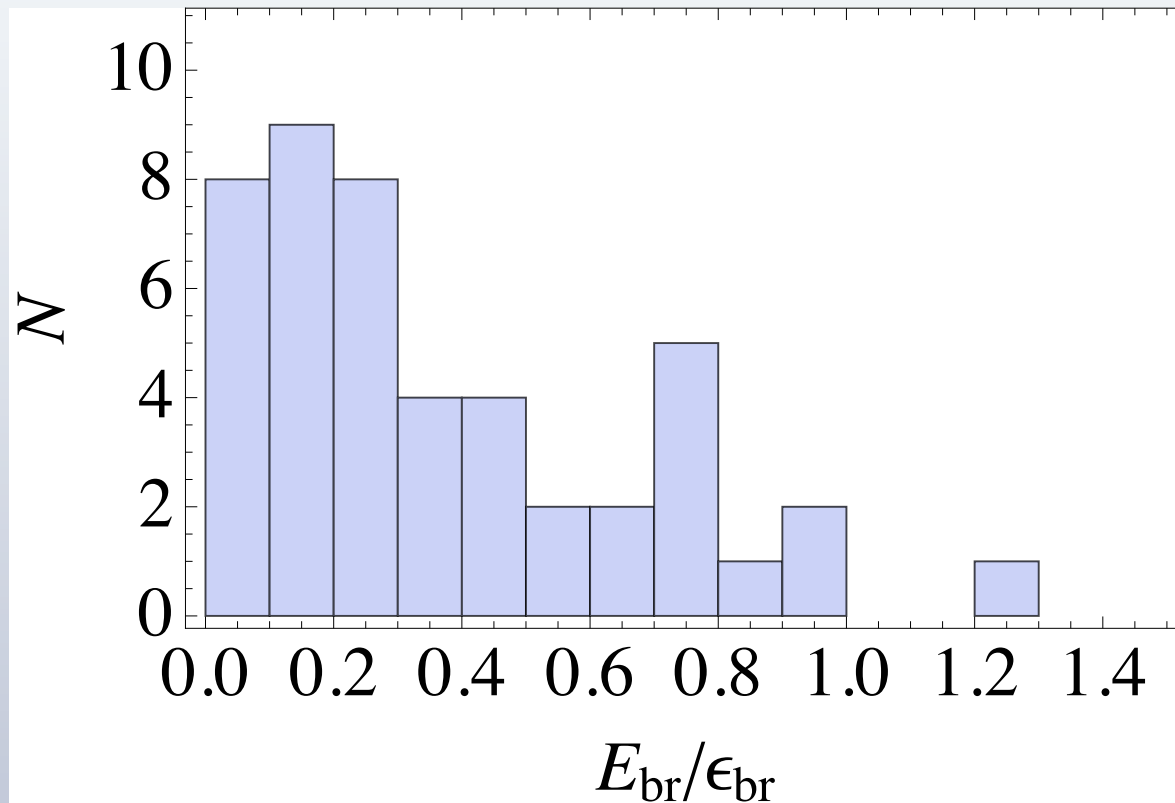
$$\epsilon_{br} = (3\pi)^{7/4} \frac{\hbar}{(ce)^{3/4}} \eta^{3/4} \sqrt{\xi} \frac{B_{NS}^{3/4} R_{NS}^{9/4}}{P^{7/4}} \left(\frac{r_{em}}{R_{LC}} \right)^{-1}$$

For Crab, assuming E=B

$$\approx 150 \text{ GeV}$$

- Detection of Crab above 150 GeV (with non-exponential cut-off) exclude curvature emission as the main emission mechanism (Lyutikov et al. 2011)

Other pulsars: maximal curvature energy at light cylinder



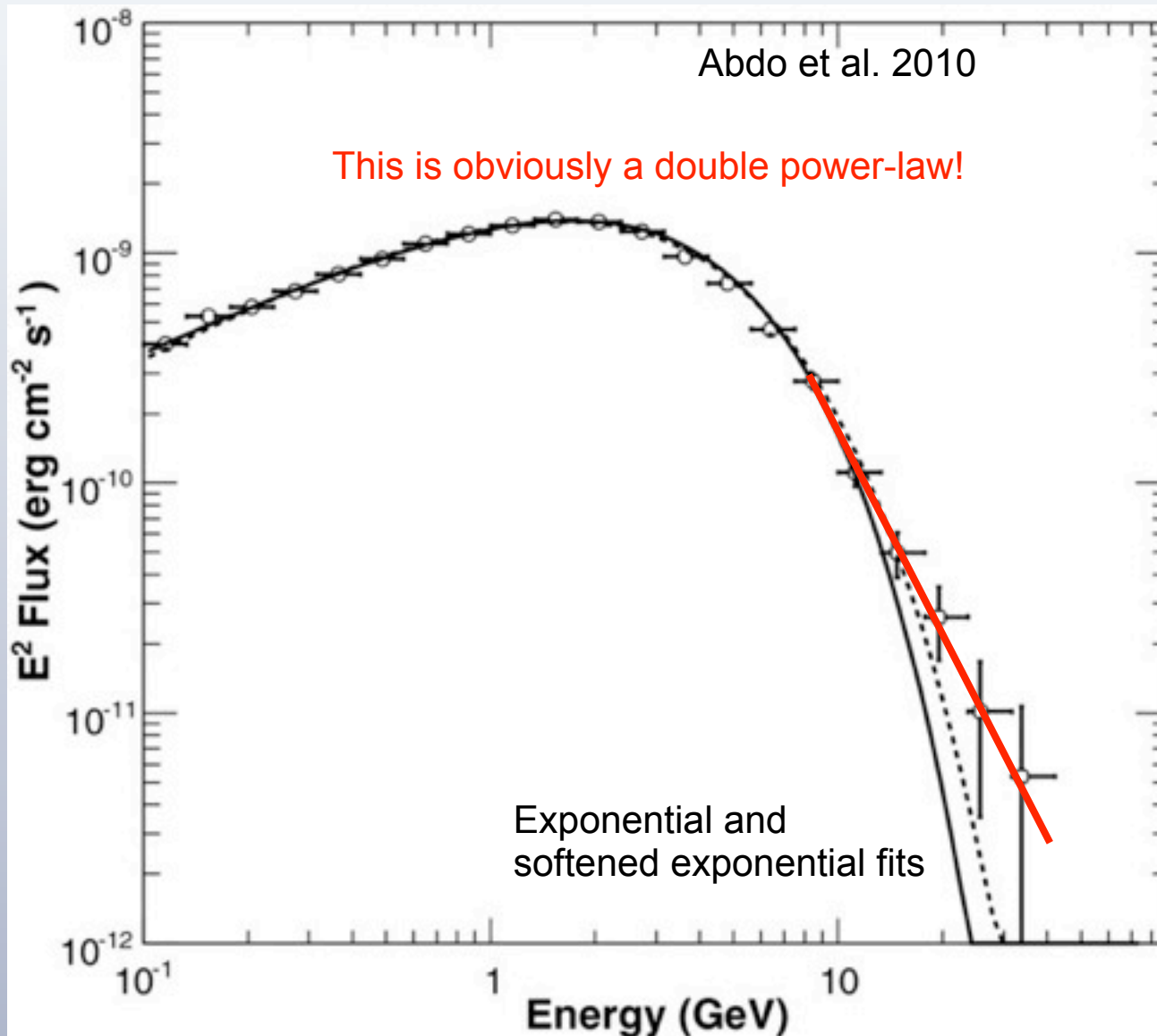
- Ratio of the observed break energies E_{br} for 46 pulsars to the maximum predicted for curvature radiation ϵ_{br}
- For Crab $E_{br}/\epsilon_{br} \sim 0.05$ seemed OK, but not OK \rightarrow Lower limits

Implications of Crab detection by VERITAS:

- **Spectral break in Crab is not due to curvature emission of the maximal energy of particles**
- **Alternative possibility: IC scattering**
- **Break due to the details of particle distribution and scattering cross-section (in the KN regime)**

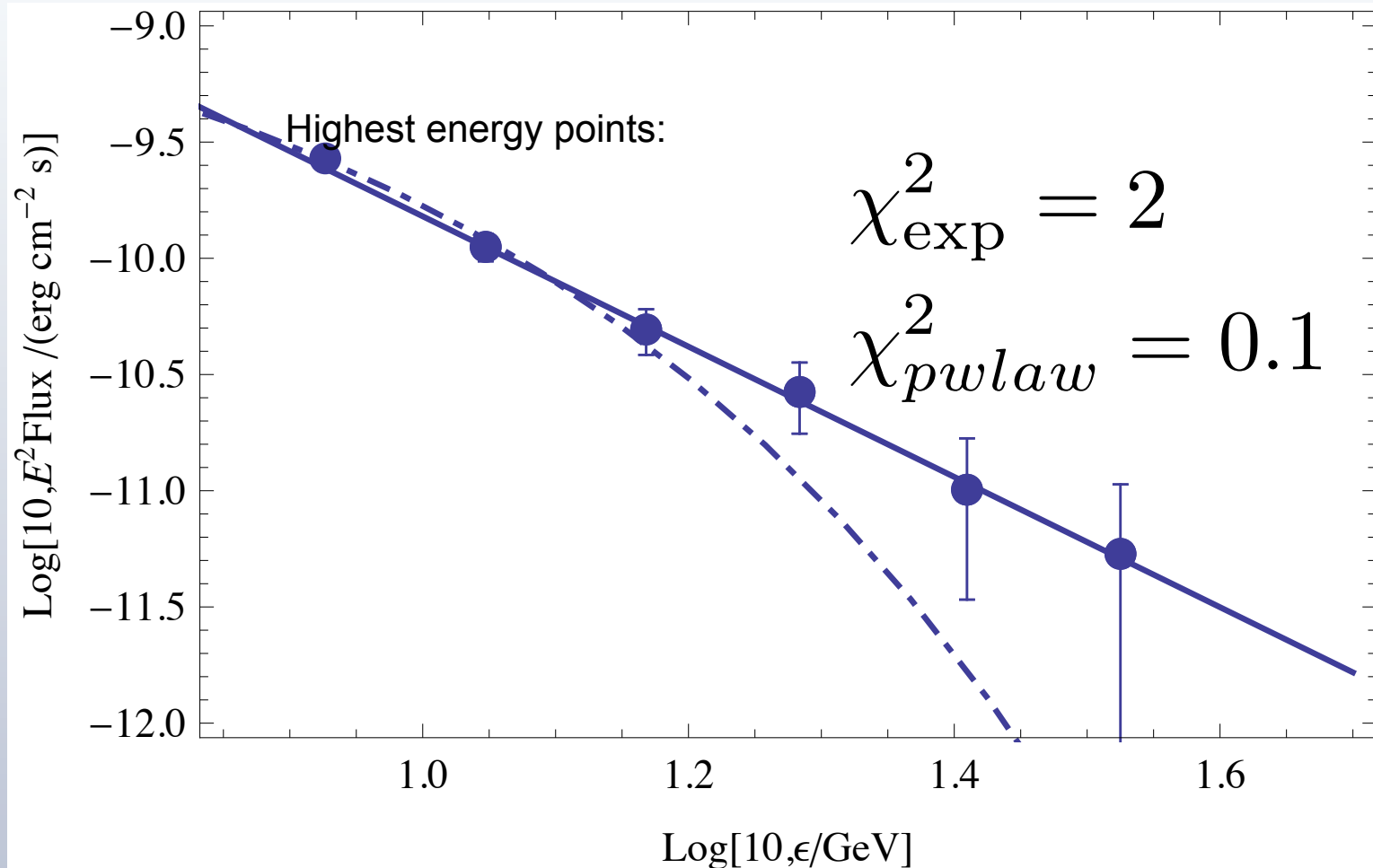
- Is Crab special (e.g. high level of soft photons)?
- What about other pulsars?
 - Vela
 - Geminga

Fermi spectrum of Geminga



Geminga: fits

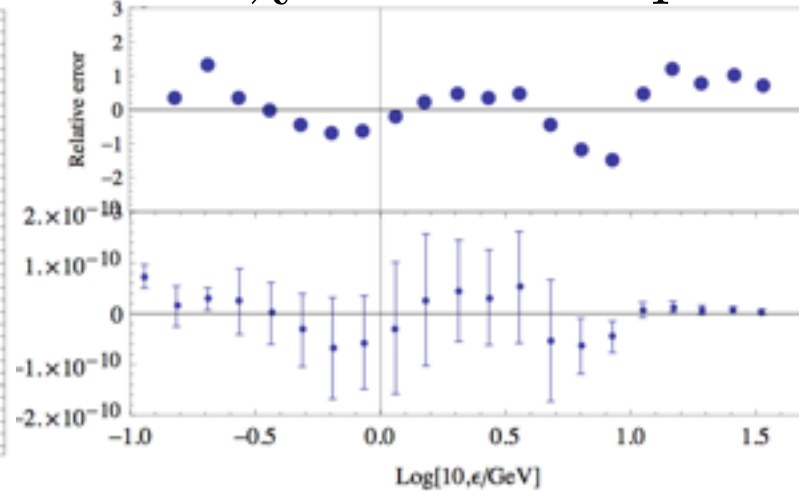
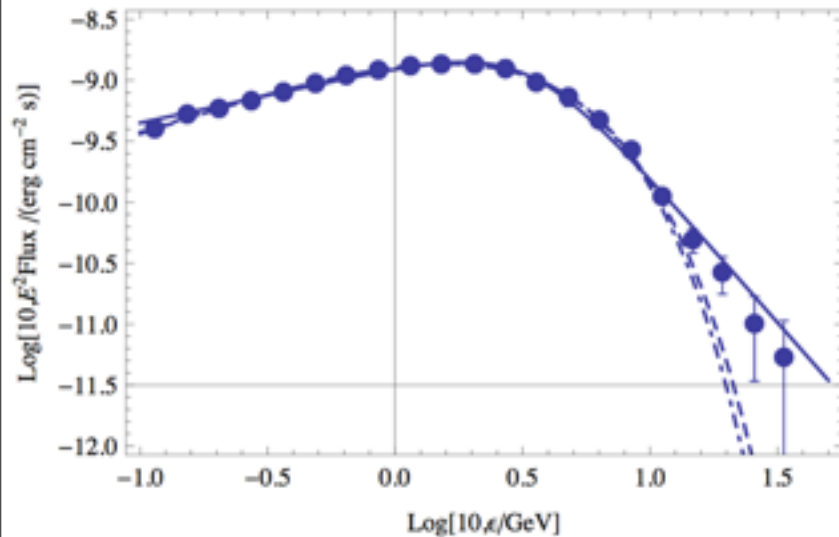
Lyutikov 2012



- The highest energy data points actually have the **smallest** error bars.
- Too broad energy bins?
- Geminga is not intrinsically bright - “garden variety”

Geminga: broad band fits

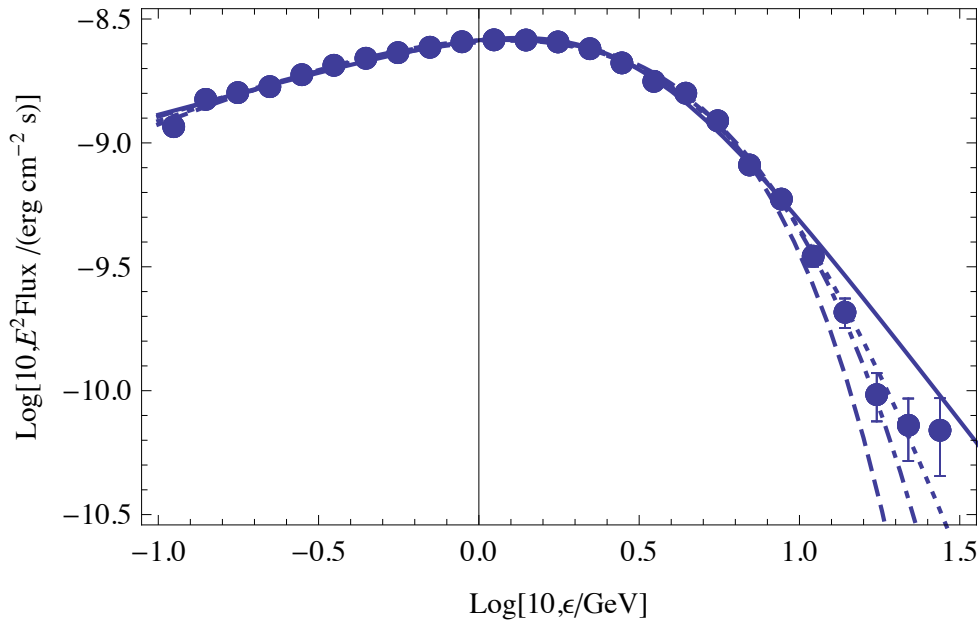
errors χ^2 for double pwlaw



model	Fit function	α	β	ϵ_{br}	reduced, unweighted χ^2	b	dof
a	$\left(\left(\frac{\epsilon}{\epsilon_{br}} \right)^\alpha + \left(\frac{\epsilon}{\epsilon_{br}} \right)^{-\beta} \right)^{-1}$	2.38	0.45	3.32	1.26	—	17
b	$\epsilon^\beta e^{-\frac{\epsilon}{\epsilon_{br}}}$	—	.70	2.35	1.13	—	18
c	$\epsilon^\beta e^{-\left(\frac{\epsilon}{\epsilon_{br}} \right)^b}$	—	0.75	1.98	0.83	0.91	17

- The errors are not random
- **Most of the χ^2 is accumulated near the break energy due to the ARBITRARY parametrization of the spectral roll-off**
- Similar results for phase-resolved spectra

Vela



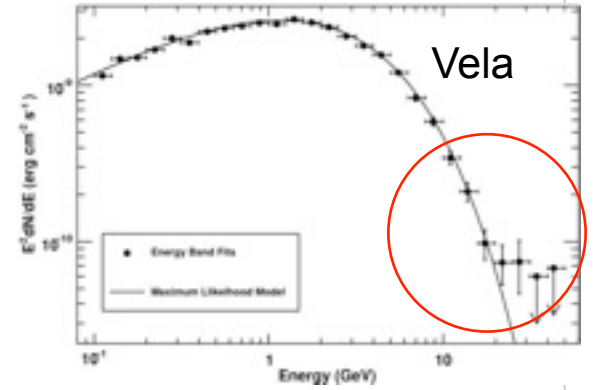
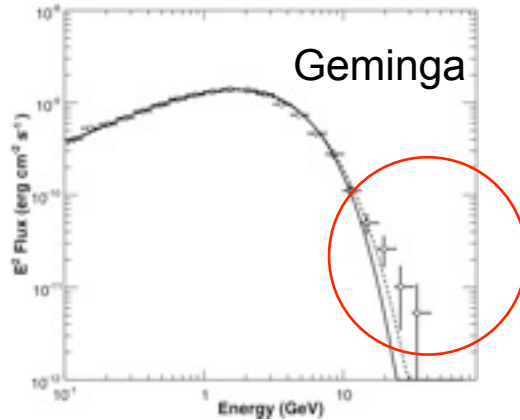
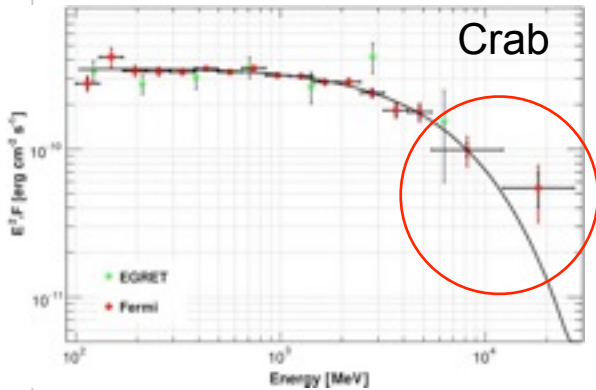
- Double power-law fits are as good as exp.
- Various parametrizations of roll-offs reduce χ^2

model	Fit function	α	β	ϵ_{br}	reduced χ^2	b	dof
<i>a</i>	$\left(\left(\frac{\epsilon}{\epsilon_{br}} \right)^\alpha + \left(\frac{\epsilon}{\epsilon_{br}} \right)^{-\beta} \right)^{-1}$	1.68	0.34	2.91	2.2	—	21
<i>b</i>	$\left(\left(\frac{\epsilon}{\epsilon_{br}} \right) + \left(\frac{\epsilon}{\epsilon_{br}} \right)^{-\beta} \right)^{-\alpha}$	4.11	0.11	8.8	1.3	—	21
<i>c</i>	$\epsilon^\beta e^{-\frac{\epsilon}{\epsilon_{br}}}$	—	.42	3.1	2.0	—	22
<i>d</i>	$\epsilon^\beta e^{-\left(\frac{\epsilon}{\epsilon_{br}} \right)^b}$	—	0.59	1.58	1.4	0.73	21

Of the three brightest pulsars, two are inconsistent with exp cut-off, third is consistent with double power law

More hints: spectra

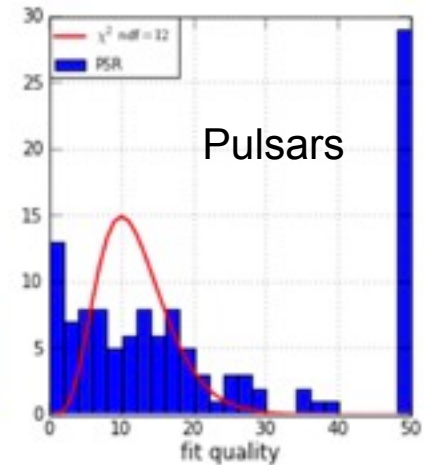
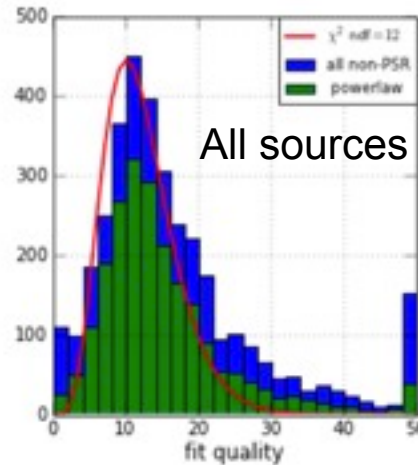
- Most young pulsars and some MSPs have hard excess with respect to models



Paul Ray

Maxim Lyutikov and Alice Harding shake on a bet over whether the gamma-ray spectrum of the Vela Pulsar is power-law rather than exponentially cutoff above 10 GeV. — at [Aspen Center for Physics](#).

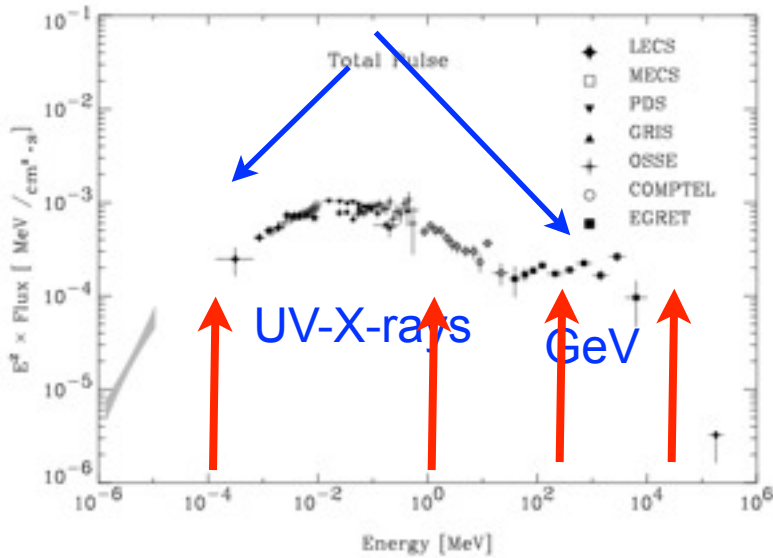
Fermi fit quality



T. Burnett, priv. comm.

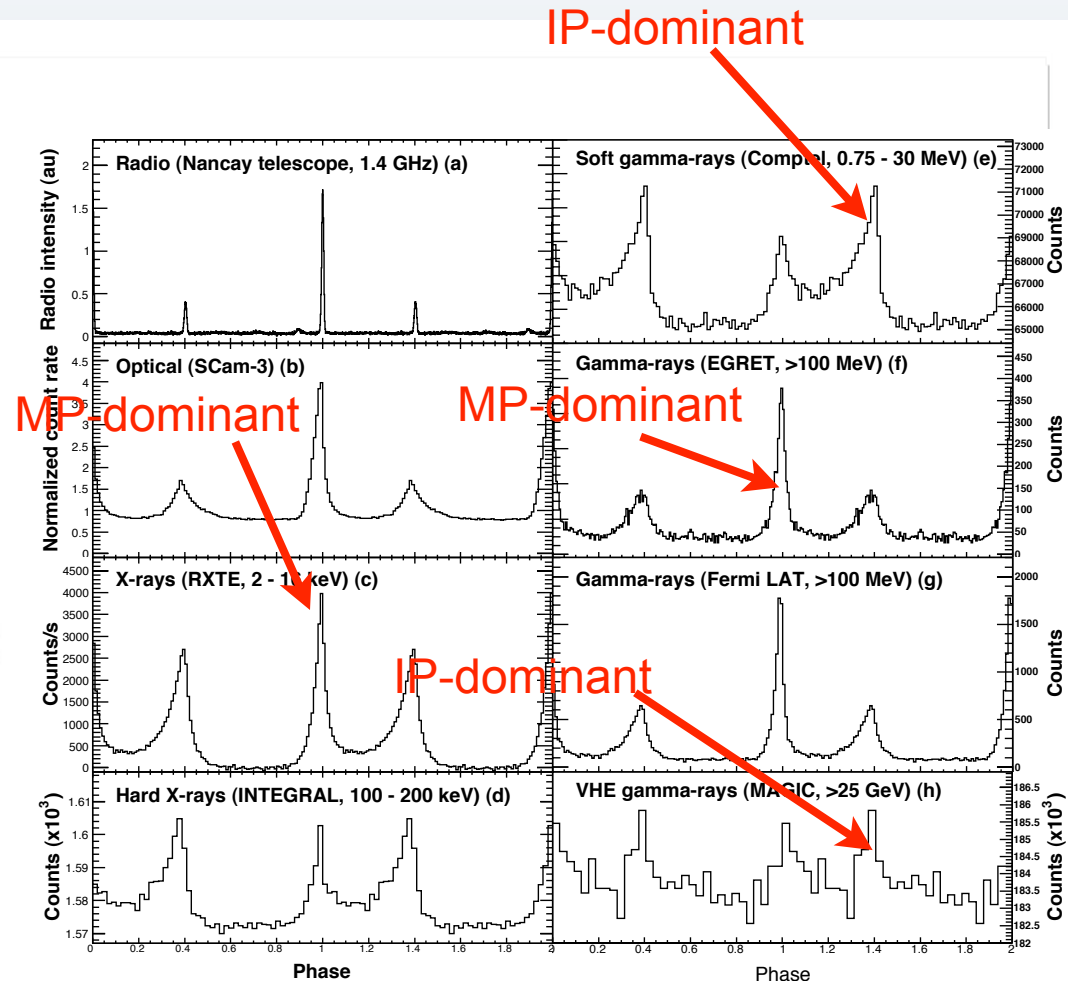
More hints: Crab spectrum & profiles

Two bumps



-MP/IP pattern is repeated
in the two spectral bumps
-Consistent with IC model

Detection of Geminga or Vela by VERITAS/HESS would be a killer
for the curvature model

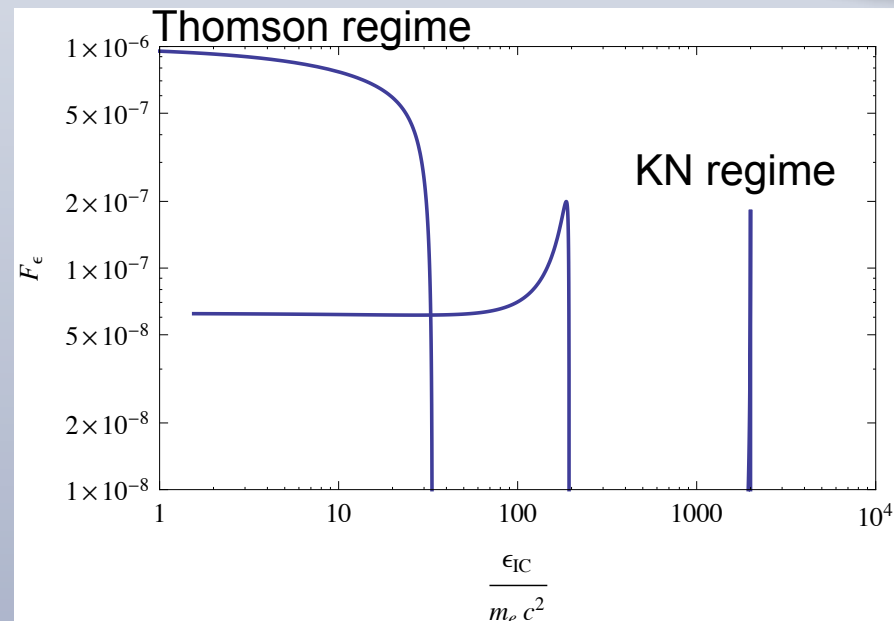
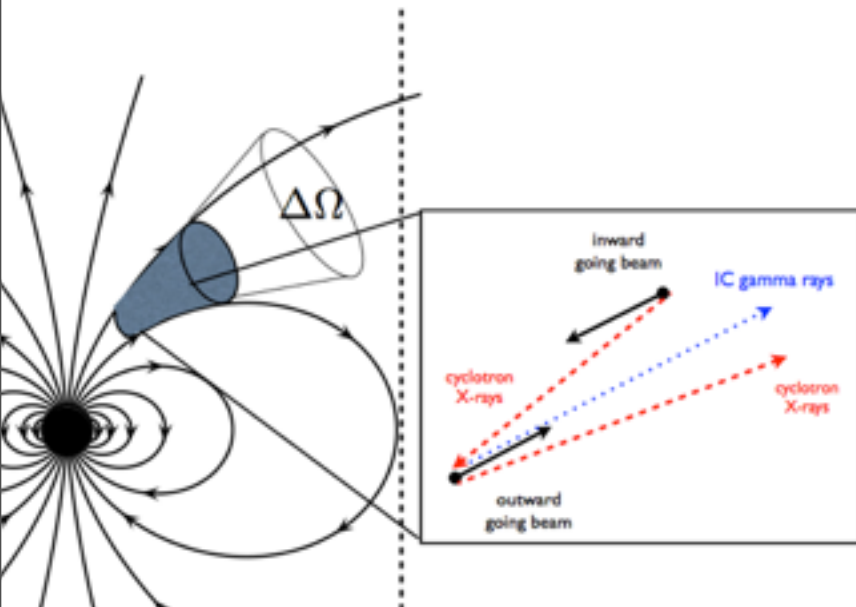


IC model

Lyutikov 2013

- `Off-the shelf'' SSC models not applicable
 - Random B-field of a given value
 - Isotropic particle distribution
 - single value for bulk motion
- Regular B-field, changing sharply
- Strong radiative damping: non-isotropic distribution
- Continuous v_{II}

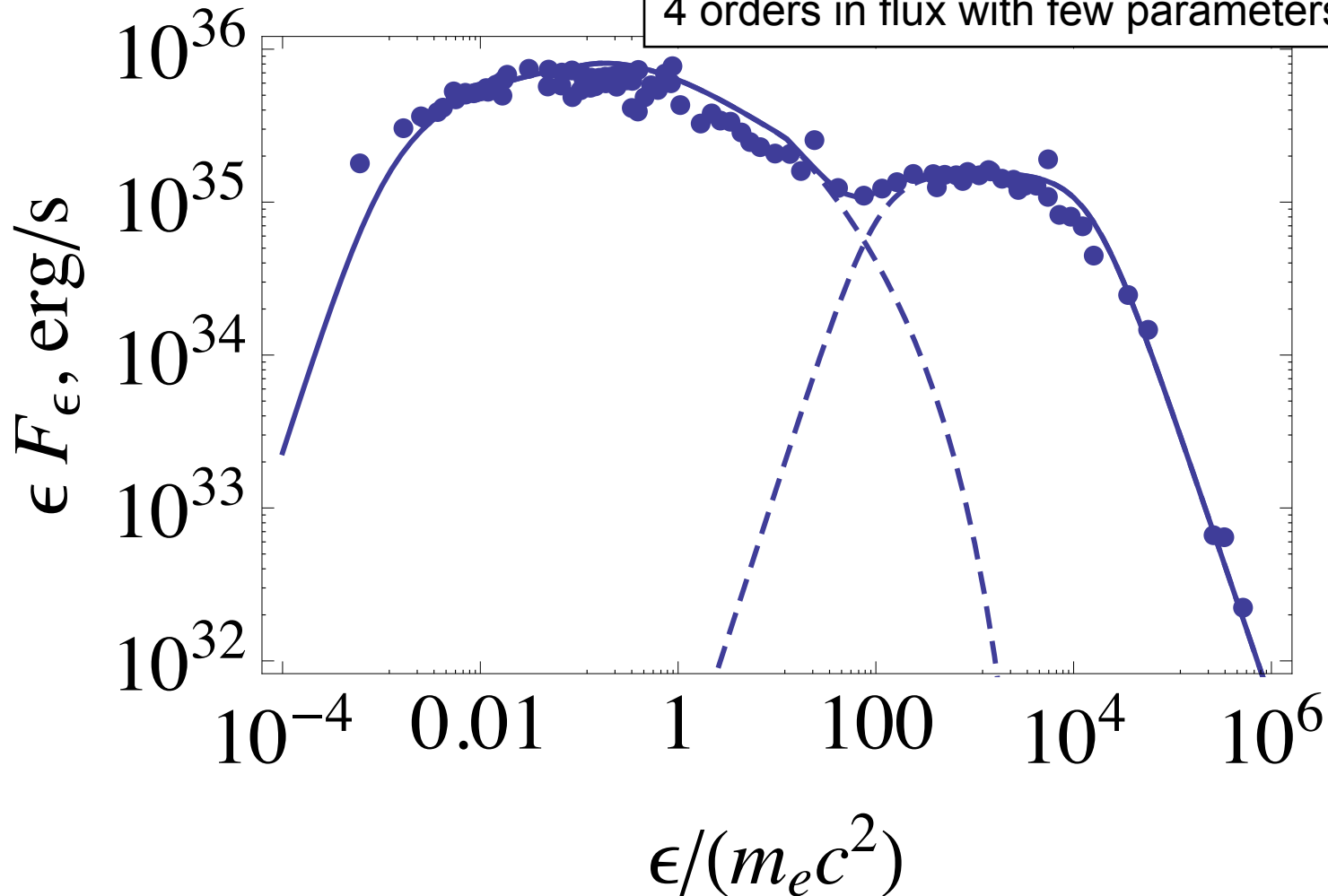
- Do not model acceleration - infer distribution from observations
- 1D model: Two counter-streaming components:
 - optical-X-ray: boosted cyclotron
 - gamma rays: IC scattering of the inward cyclotron photons by the outward going particles
- Deep in KN regime: **IC bump is a direct measure of $f(p_{II})$**



Data fit: 10 orders in energy

Data: Kuiper +, 2001, Fermi, VERITAS

Highly constrained fit, ten orders in energy,
4 orders in flux with few parameters



Details of the fit

- 4 parameters (R_{em} , γ , $v_{gyration}$, multiplicity), 4 measurables (energies and fluxes of two bumps).
- Kinematics: cyclotron peak at ~ 100 keV, IC peak at \sim GeV:
- L_X , L_{γ} :

$$\frac{R_{em}}{R_{NS}} \sim 15$$

$$\gamma \sim 2000$$

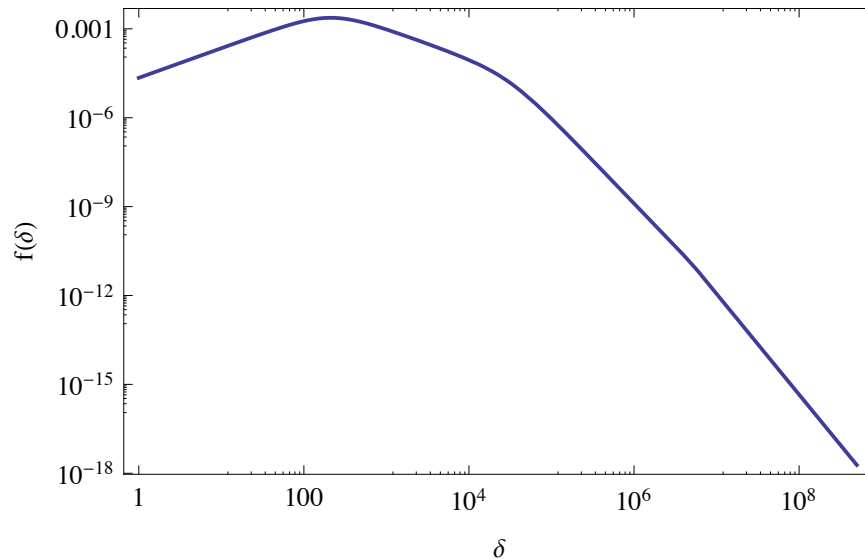
$$\lambda = \frac{8\pi}{b_{NS}} \tilde{\epsilon}_s^2 \frac{\lambda_C}{r_E} \frac{1}{\eta_\Omega} \frac{L_{IC}}{L_X} \left(\ln \left(\frac{\tilde{\epsilon}_{max}}{\tilde{\epsilon}_{min}} \right) \right)^{-1} \approx 10^5$$

$$\beta_0 = \frac{2\sqrt{r_E} \lambda_C \sqrt{\ln \frac{\tilde{\epsilon}_{max}}{\tilde{\epsilon}_{min}}}}{\sqrt{\pi m_e c^3 \Delta\Omega} \tilde{\epsilon}^2 L_{IC}^{1/2}} \approx 4 \times 10^{-5} \Delta\Omega_{-2}^{1/2}$$

cyclotron emission

Measured distribution function $f(p_{II})$

- Deep in KN regime: **IC component traces particle distribution**

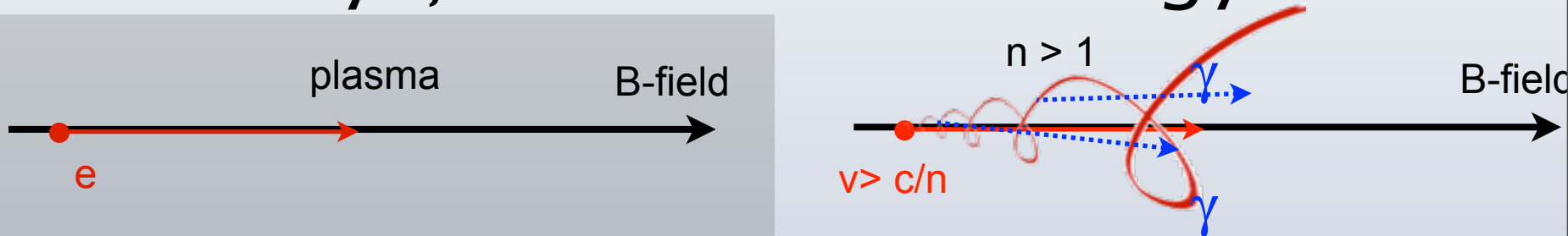


$$f(\delta) \propto \begin{cases} \delta^m, & m \approx 1, \text{ for } \delta_0 < \delta < \delta_1 \\ \delta^n, & n \approx -1, \text{ for } \delta_1 < \delta < \delta_2 \\ \delta^l, & l \approx -3, \text{ for } \delta_2 < \delta < \delta_3 \\ \exp^{-\delta/\delta_3}, & \text{for } \delta_3 < \delta \end{cases}$$

$$\delta_0 \approx 10, \delta_1 \approx 10^4, \delta_2 \approx 10^6, \delta_3 \geq 10^8$$

- plus counter-streaming. **Typical gamma $\sim 10^3$** (very reasonable)
- **multiplicity: $10^6 - 10^7$** - highish, but still reasonable, consistent with average $\sim 10^6$ need for the nebula
- $\beta_0 \propto (r - R_{NS})^3$ - came from spectral fit. Why gyration?

Relating all pulsar non-thermal emission, from radio to VHE gamma rays, 18 orders in energy

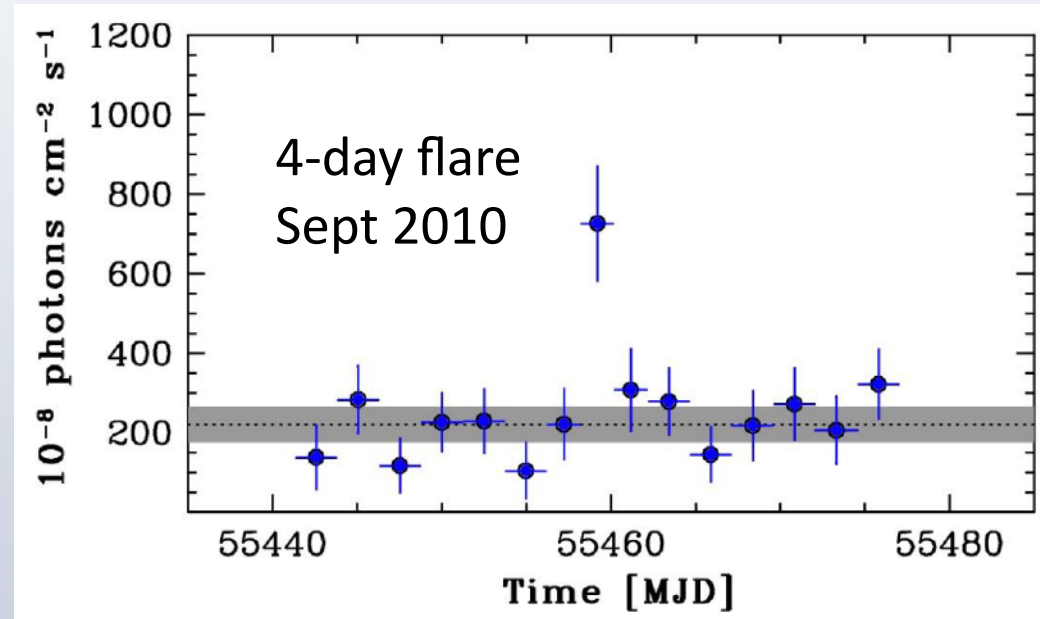


- gyration is excited at anomalous cyclotron resonance (Kazbegi + 91, Lyutikov + 98)
- Relativistic plasma streaming along B-field excites EM waves at the anomalous cyclotron resonance $\omega - k_{\parallel} v_{\parallel} = \ominus \omega_B / \gamma$
- Particle goes **up** in Landau levels **and** emits a photon (of negative energy in the center of gyration frame) $\beta_0 \propto (r - R_{NS})^3$
- Alignment of radio and gamma (?).
- **Radio and gamma are intrinsically related!**

Implications:

- Spectral breaks are not due to curvature emission of the maximal energy particles
- Alternative possibility: IC scattering, break due to the details of particle distribution and scattering cross-section (in the KN regime)
- typical gamma $\sim 10^3$ - very reasonable
- high multiplicity, $\sim 10^6$ - 10^7 , but Crab nebula needs 10^6 on average.
- Pair production in the outer gaps
- $\beta_0 \propto (r - R_{NS})^3$ - follows from the theory of radio emission: radio and VHE gamma are related! (18 orders)
- Critique: where are soft photons in non-Crab pulsars? - IC scattering in KN is highly energy dependent, favors UV

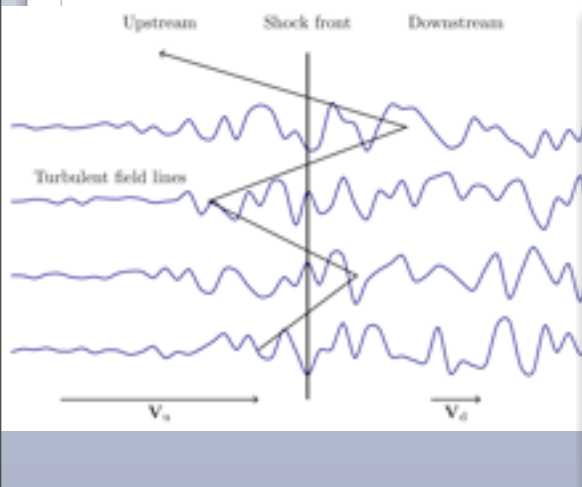
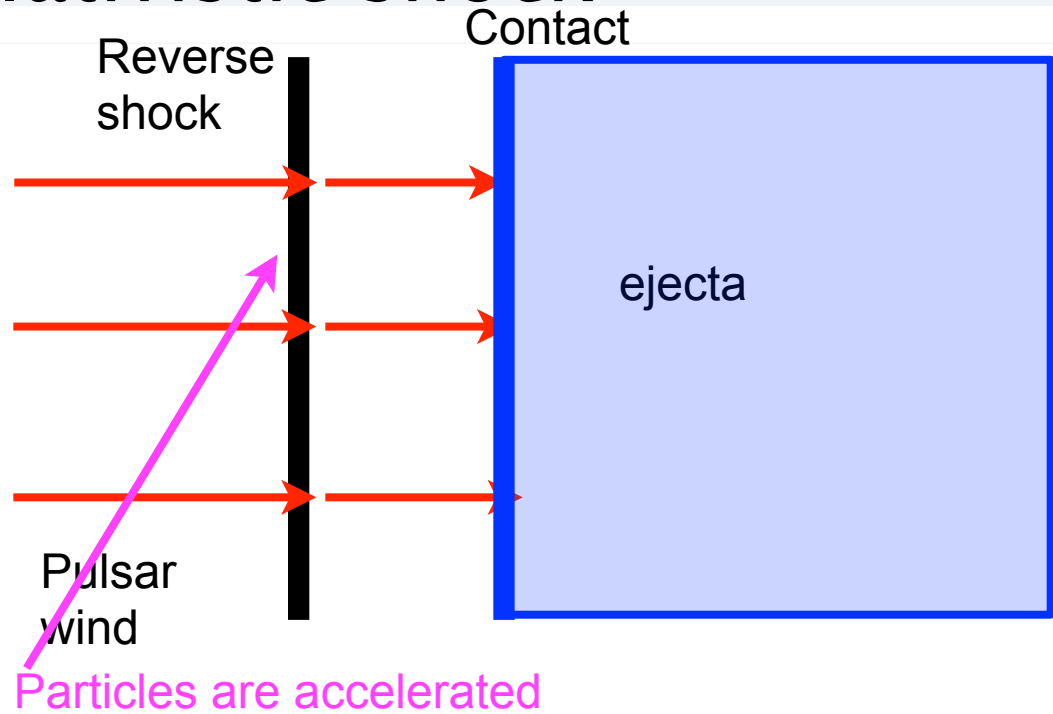
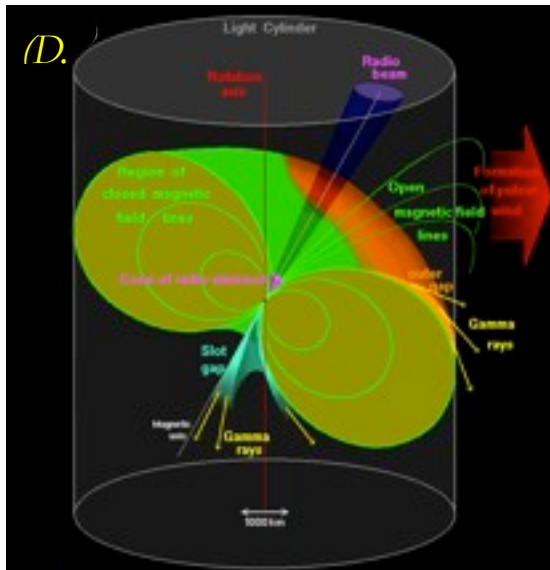
II. Crab nebula flares: evidence for reconnection



Tavani et al. 2011

- ~ few days increase in 100 MeV-1 GeV flux, factor of few-tens
- about once per year
- Nothing at other energies or the pulsar
- Time scales \ll dynamical time for inner rings (months) ->
Localized intermittent events - what events?

Current models of pulsar wind: relativistic shock



- How much energy is carried by particles, and how much by B-field?
- Models of pulsar magnetospheres: $\sigma \gg 1$
- Models of the nebular: $\sigma \ll 1$
- Small σ : strong shocks, acceleration by Fermi
- **Acceleration is slow, on time-scale \gg gyration**

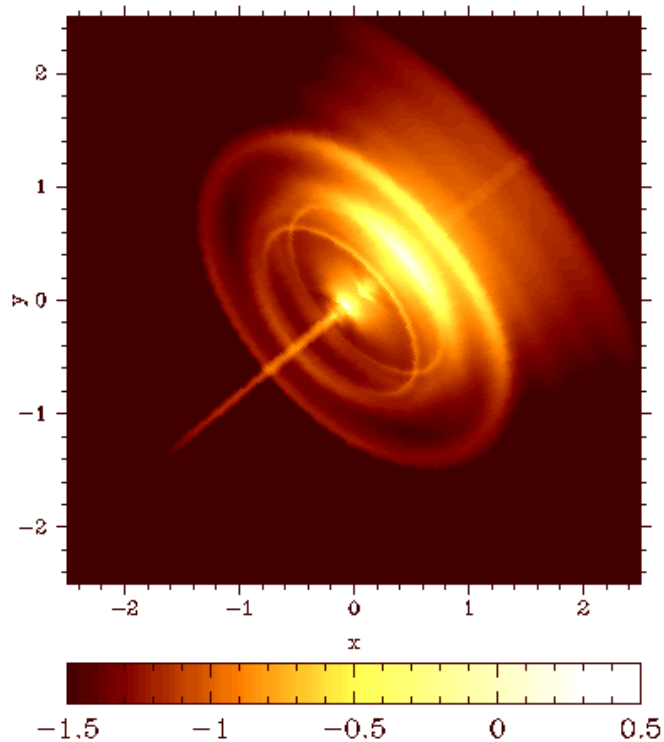
$$\sigma = \frac{B^2}{4\pi\gamma\rho c^2}$$

We have a problem...

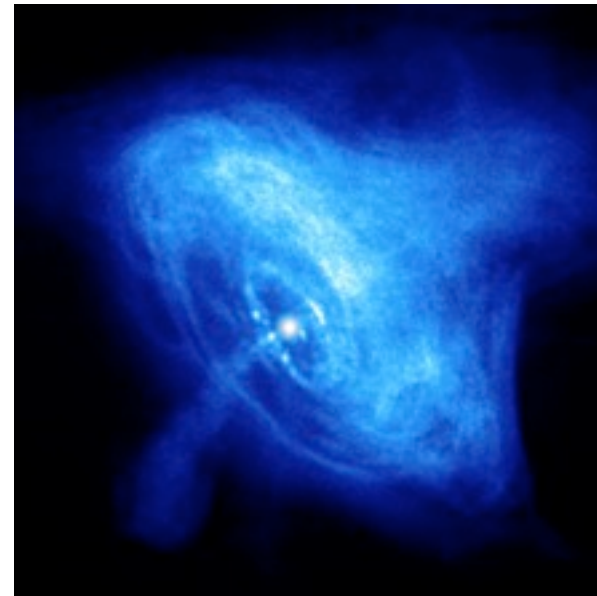
PWN morphology is well reproduced with low magnetized wind

Komissaov & Lyubarski,
Del Zanna et al., Bucciantini

Synchrotron Emission



Chandra image of Crab

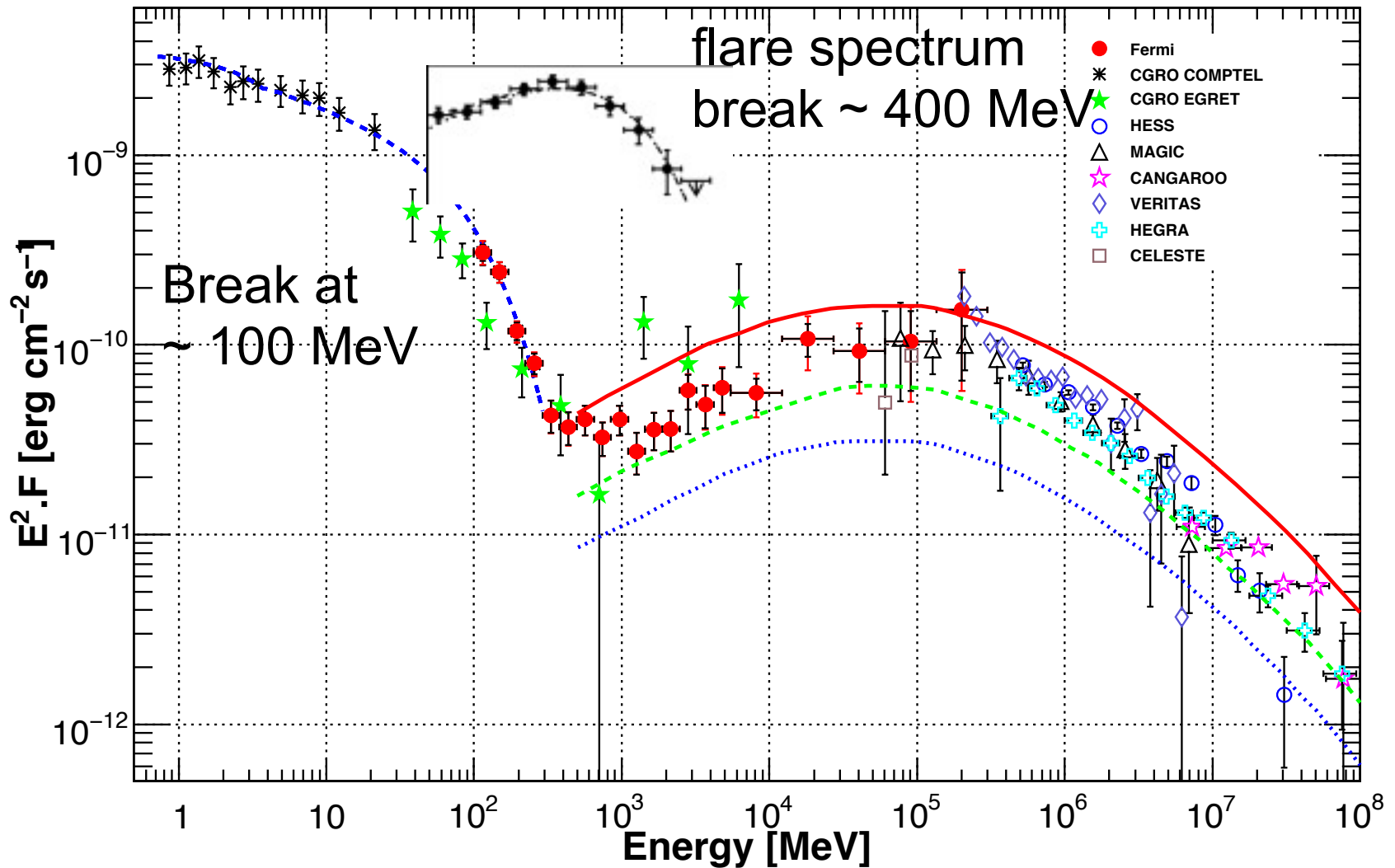


Need low magnetized wind, sigma ~ 0.001

$$\sigma = \frac{B^2}{4\pi\gamma\rho c^2}$$

But: spectrum of Crab nebula

Tavani et al. 2010
Beuhler et al., 2011



Upper limit to synchrotron frequency

Accelerating E-field < B-field

$$eEc = \eta eBc = \frac{4e^4}{9m^2c^3} B^2 \gamma^2$$
$$E_p = \frac{27}{16\pi} \eta \frac{mhc^3}{e^2} = 236 \eta \text{ MeV.}$$

Lyutikov '10,
Komissarov & Lyutikov '11
de Jager '98 (for shocks)

- Same as Fermi acceleration on inverse gyroscale
(requires very efficient scattering, stochastic
acceleration: $\eta \ll 1$)

- **Typically $\eta < 10^{-2}$ for stochastic shock acceleration:
this excludes stochastic acceleration schemes even for
“normal” PWN emission**

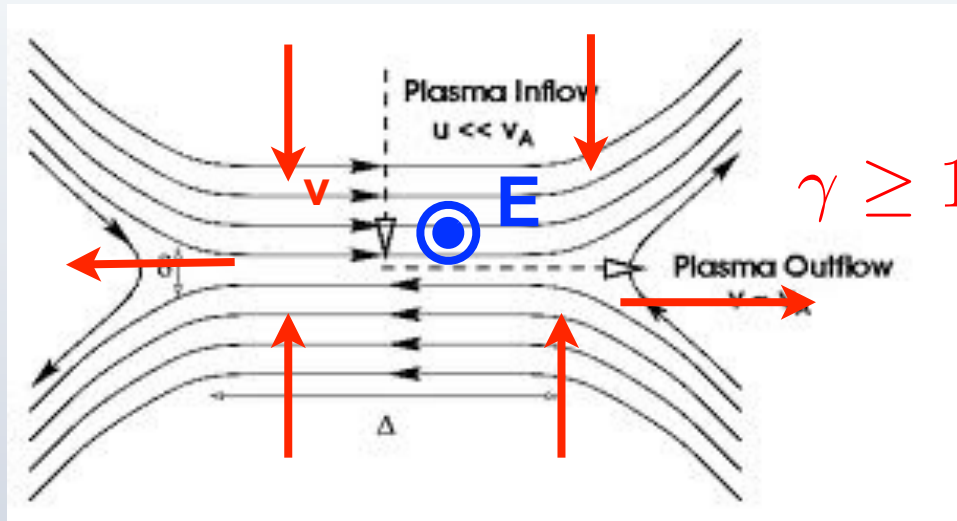
Contradiction: low magnetized pulsar wind can reproduce Nebula
morphology, but not the spectrum

Particle acceleration?...

- Highly magnetized, $\sigma \gg 1$, shocks are weak, not likely to be efficient accelerators.
- All the energy in the B-field: accelerate particles directly via **reconnection**.

Paradigm change (?): some (most?) particles are accelerated by magnetic reconnection (and not shocks)

Reconnection: efficient, non-stationary



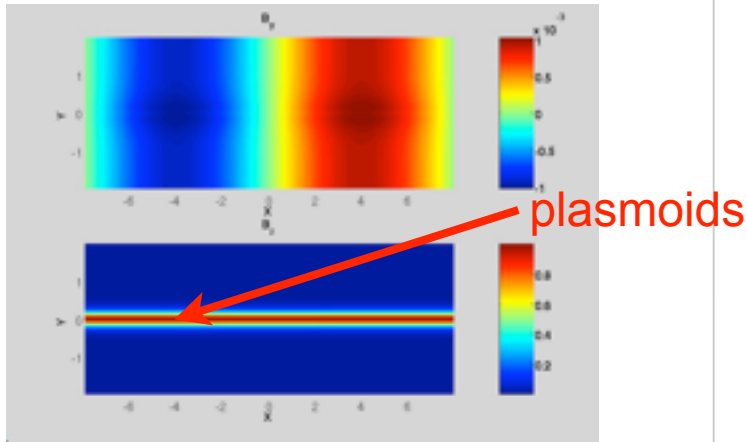
Reconnection in $\sigma \gg 1$ plasma: outflow can be relativistic (Lyutikov & Uzdensky 2002, others)

New plasma physics regime: $\sigma \gg 1$ plasma.

- **What are dynamic and dissipative properties of such plasmas? - very different from laboratory and space plasmas.**
- Pulsar winds, AGN & GRB jets and magnetospheres of BHs
- Alfvén velocity is highly relativistic
 - E-field is dynamically important
 - charge density is important

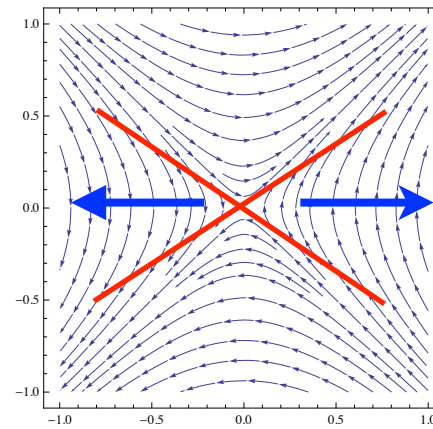
Physical model: collapse of magnetic X-point in force-free plasma

- Current sheet can be unstable to tearing

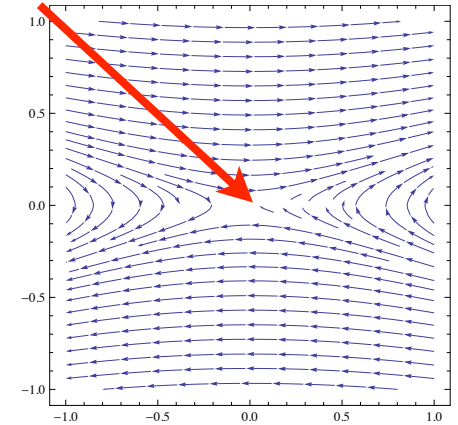


Lyutikov 2003, Komissarov+ 2007

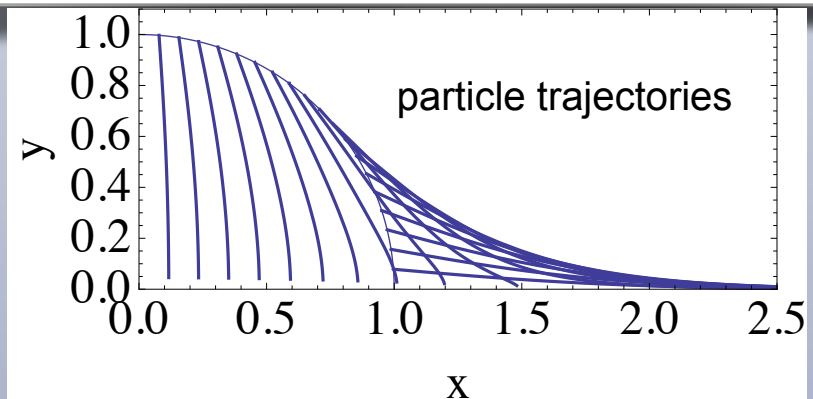
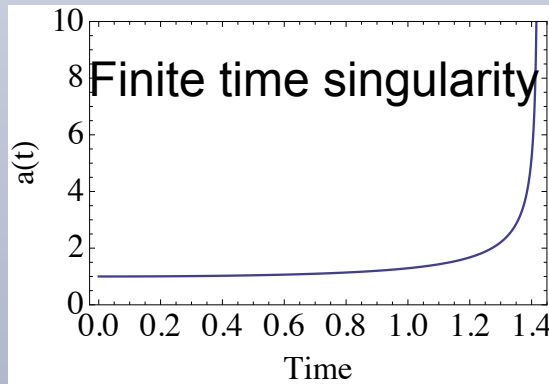
X-point collapse:



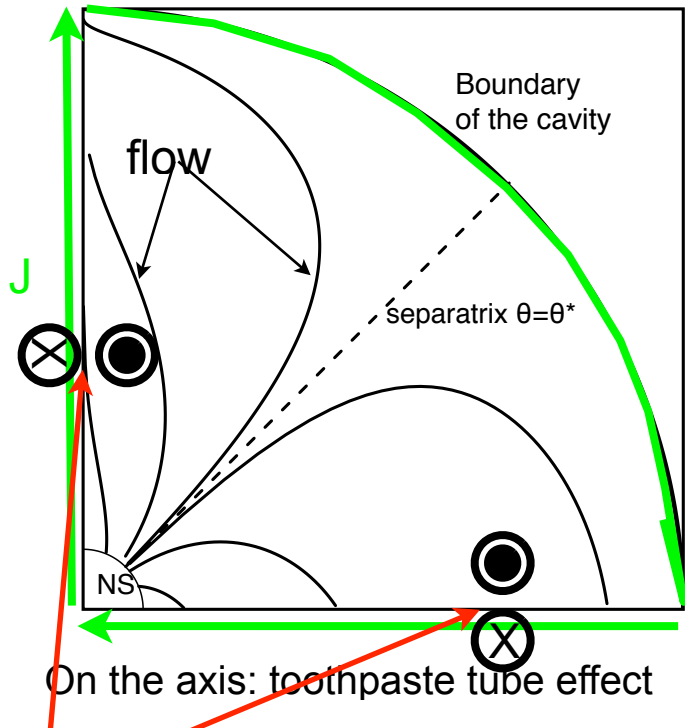
current sheet formation



- **explosive** dynamics on Alfvén (light) time
- Starting with smooth conditions
- $E \sim B_0$ (field outside), $E > B$ with resistivity
- Particles drift towards null line



High sigma model of pulsar wind nebulae *(Lyutikov 2010)*



- Lyutikov (2010): 100 MeV is still too much.
- Ideal flow in the bulk, dissipation on boundary
- "We propose that [...] the excessive magnetic flux is destroyed in a reconnection-like process"

High sigma model of PWNe

- No shocks! (Acceleration in reconnection)
- Relativistic bulk motion of emitting plasma

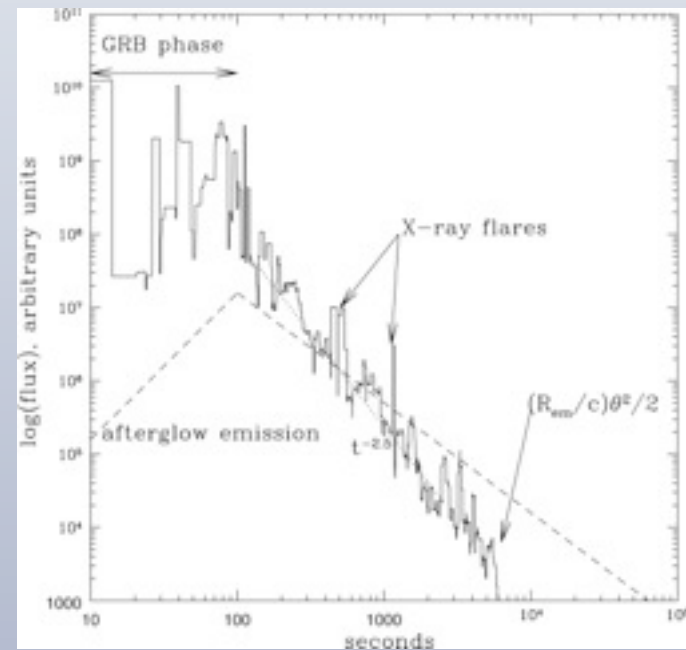
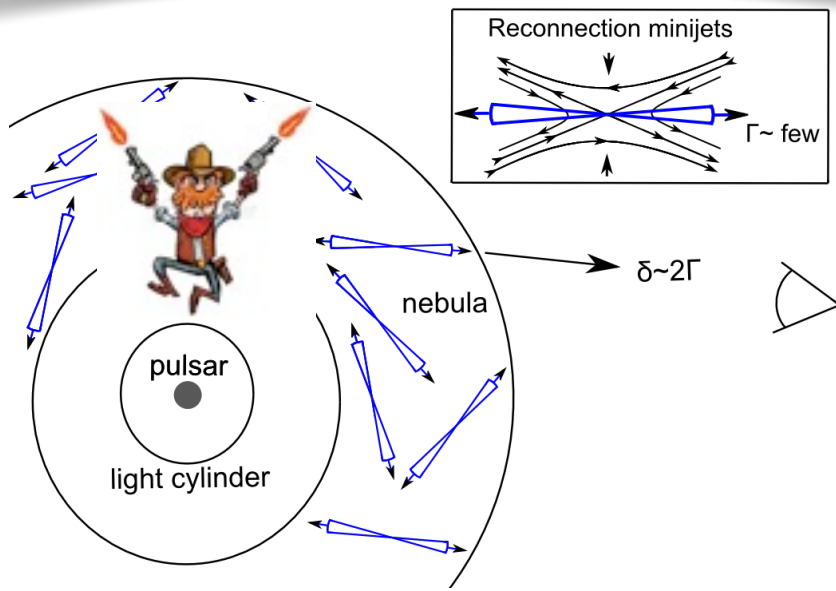
Two possible reconnection sites

Statistical model: Nebula emission originates in spontaneous relativistic reconnection outflows

- Relativistic reconnection: Lyutikov & Uzdensky, Lyubarsky, Hoshino
- $E \sim (v_{in}/c) B \sim B$
- outflow gamma $\gg 1$
- Can be non-stationary (tearing instability)

Clausen-Brown, Lyutikov 2012

GRBs: Prompt emission produced by emitters moving randomly in the bulk frame (Lyutikov 2006).



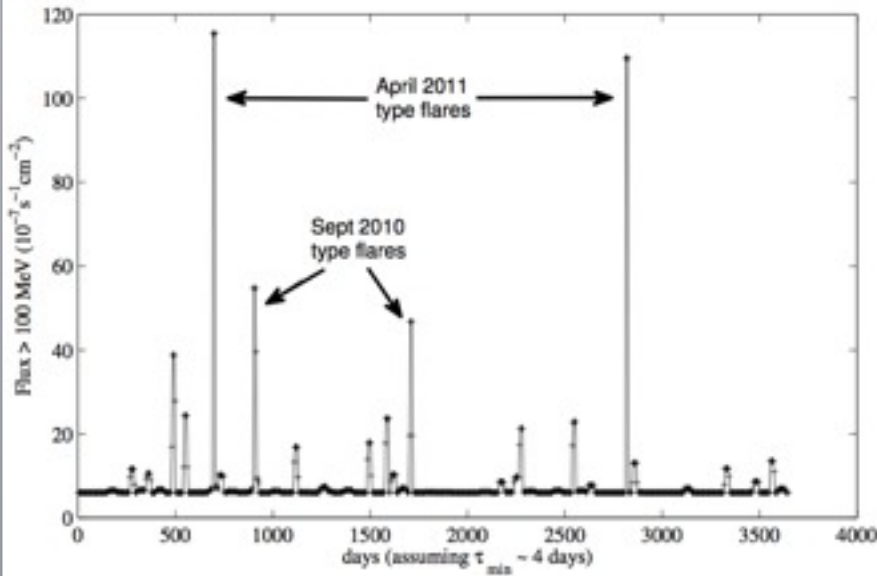
Also can be important for AGNs

Flare statistics: isotropic flares

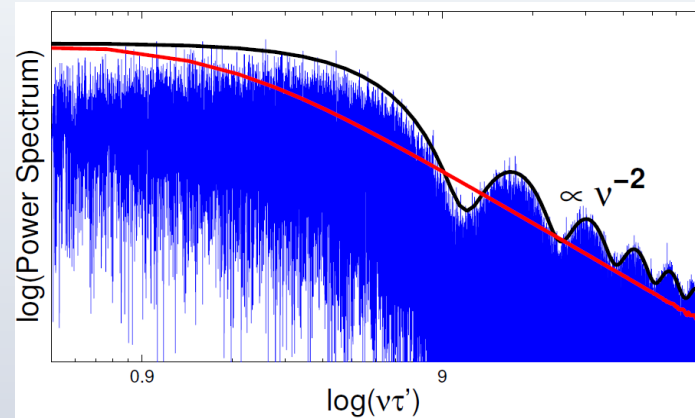
- probability of flare flux

$$\rho(F)dF \propto F^{-\frac{q+1}{q}} dF \approx \frac{1}{F} dF$$

- average flare flux is dominated by bright rare flares.



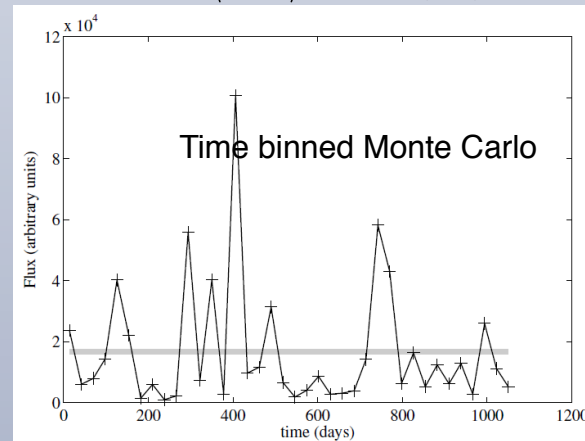
Power-law from shot noise!



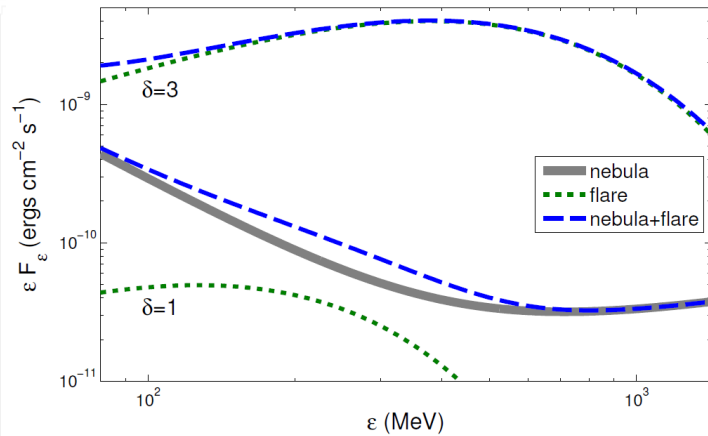
time average

$$\langle F(t) \rangle \approx n\tau' (2\Gamma)^{2+\alpha} F'$$

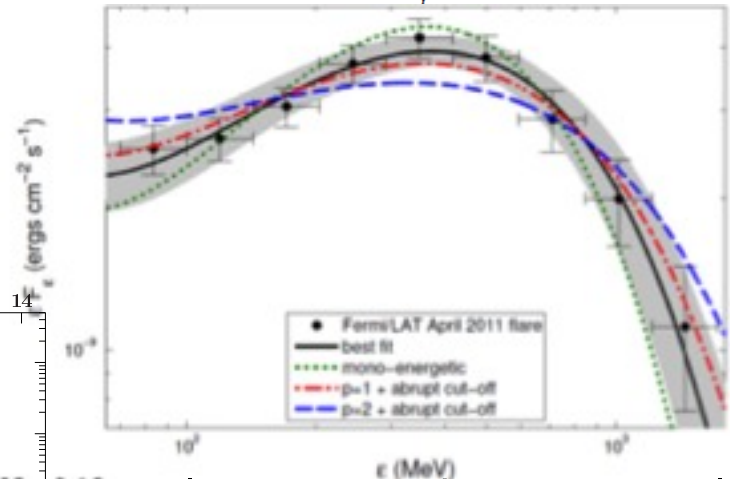
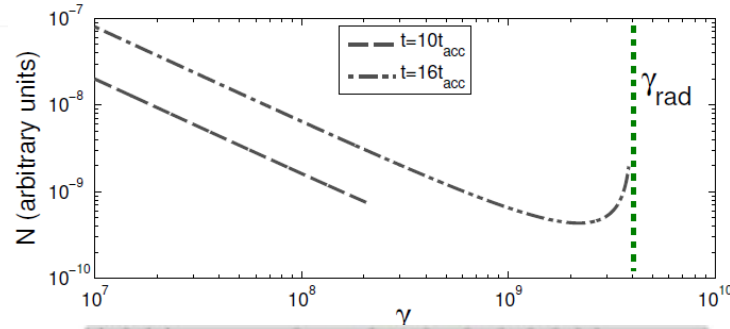
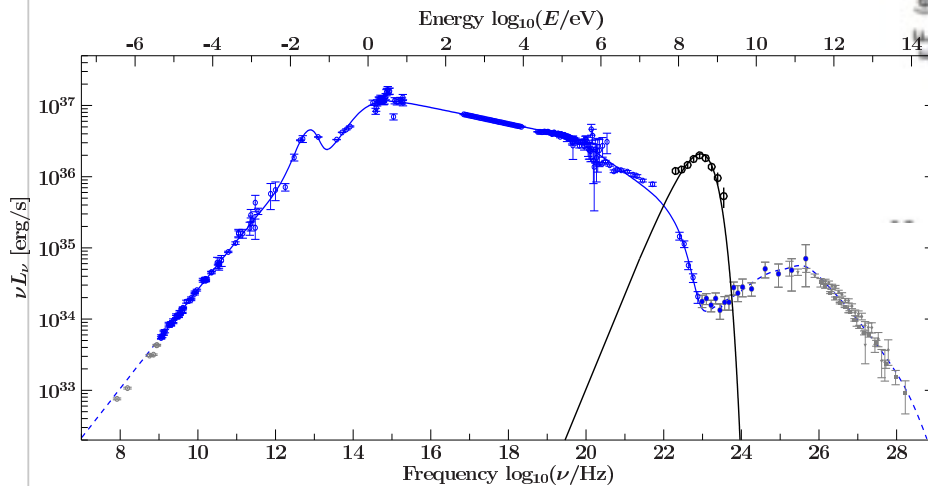
std. dev. $\rightarrow \frac{\sigma}{\langle F(t) \rangle} \approx \gamma_1 \approx \frac{\Gamma^{3/2}}{(n\tau')^{1/2}}$



$\Gamma \sim$ few increases flux and peak energy, nearly mono-energetic spectrum



mild boost - huge increase in flux

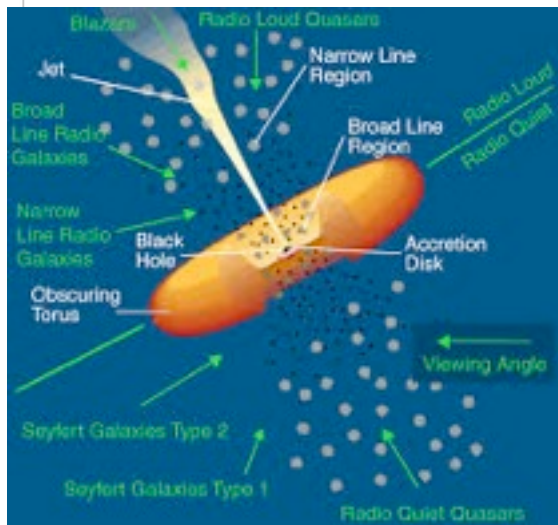
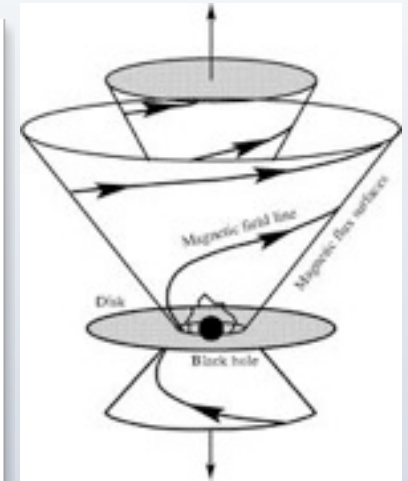


- Flare spectrum: nearly mono-energetic
- Flares are not seen at lower energies

Consistent with observations (Clausen-Brown & Lyutikov 2012)

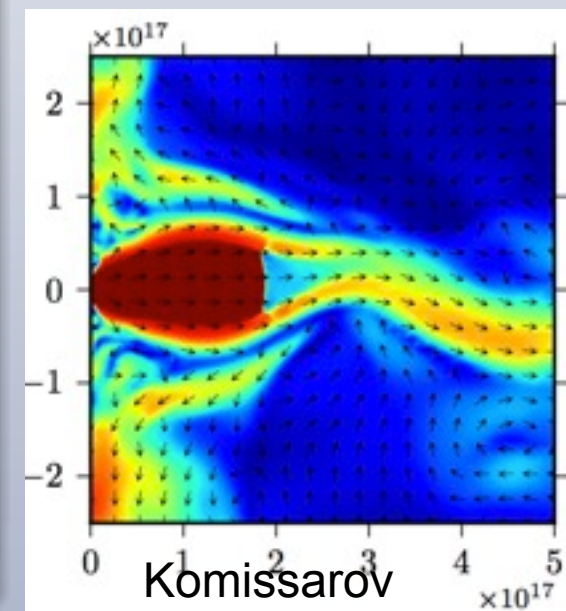
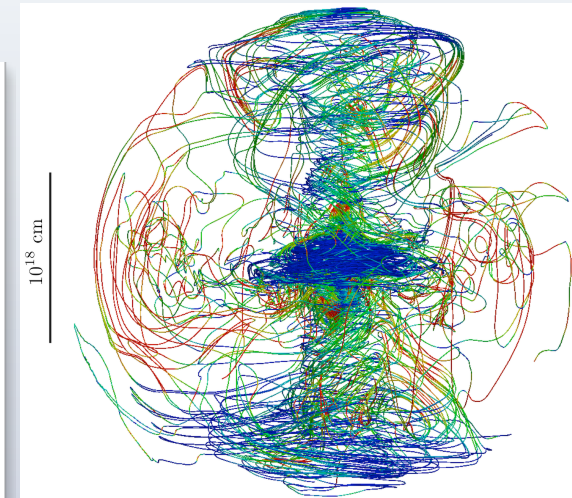
Relevance to other sources: AGNs, GRBs

- BHs in AGNs and GRBs work similar to pulsar: rotating, magnetized central object produces relativistic magnetized wind
- What is the particle acceleration mechanism in the jets?



What causes flares? - Current-driven instabilities in highly magnetized plasma

- Plasma with B-field is a non-linear anisotropic system, can slowly reach a threshold, then evolve explosively
- Flares are slowly externally-driven, suddenly “self-produced”, not like shocks
 - c.f., Solar flares
- DC-type acceleration in inductive-resistive E-field
- Need acceleration on scale of \sim light day, about 1 degree in polar angle (relativistic motion will help a bit)



Conclusion: paradigm changes (?)

- **Inverse Compton emission may be the dominant high energy emission mechanism in the majority of pulsars**
- **Reconnection is an important, perhaps dominant, mechanism of particle acceleration in PWNe and possibly in other high energy sources.**