

Planet formation and (orbital) Evolution

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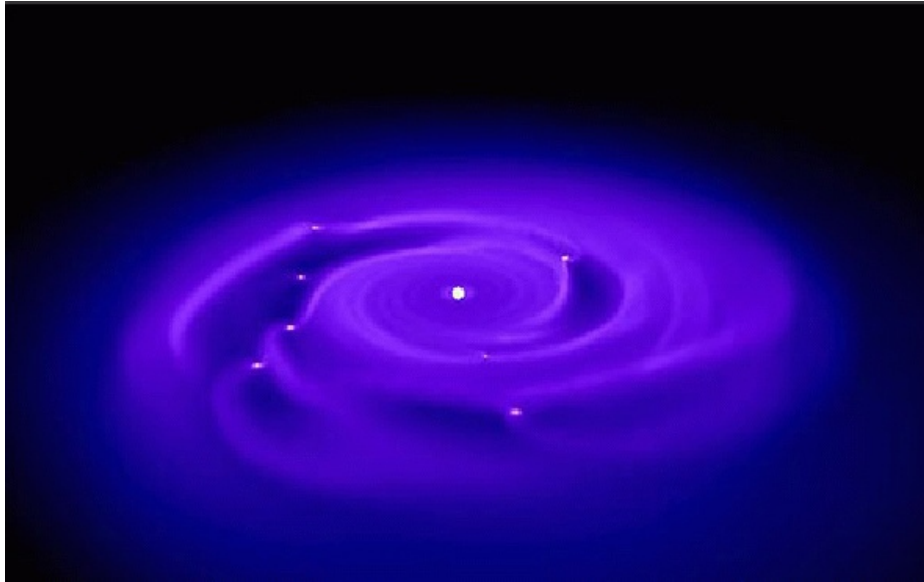


- Formation
- Planet-Disk Interaction
- Migration
- Circumbinary Planets
- Summary

(A. Crida)



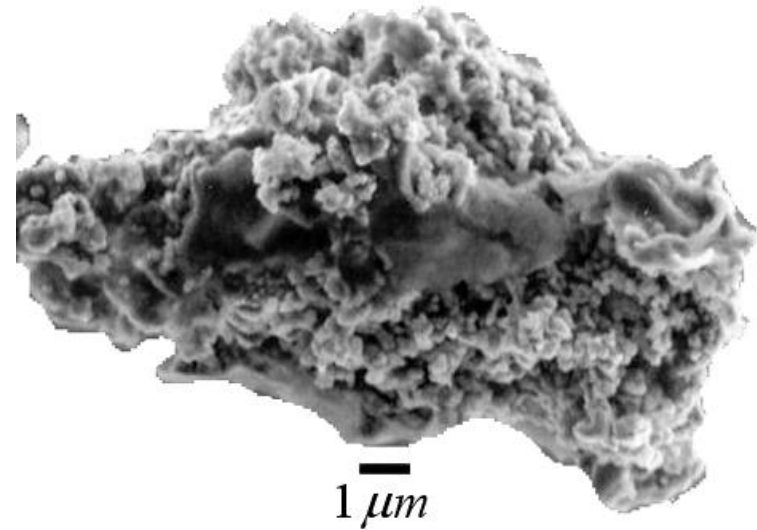
Gravitational-Instability (top-down)



(L. Mayer)

Self-gravitating disk
 Density-Fluctuations grow
 Spiral arms \Rightarrow planets
 Fast formation (10^3 years)
Core Formation ?
 (possibly for distant planets)

Sequential Accretion (bottom-up)

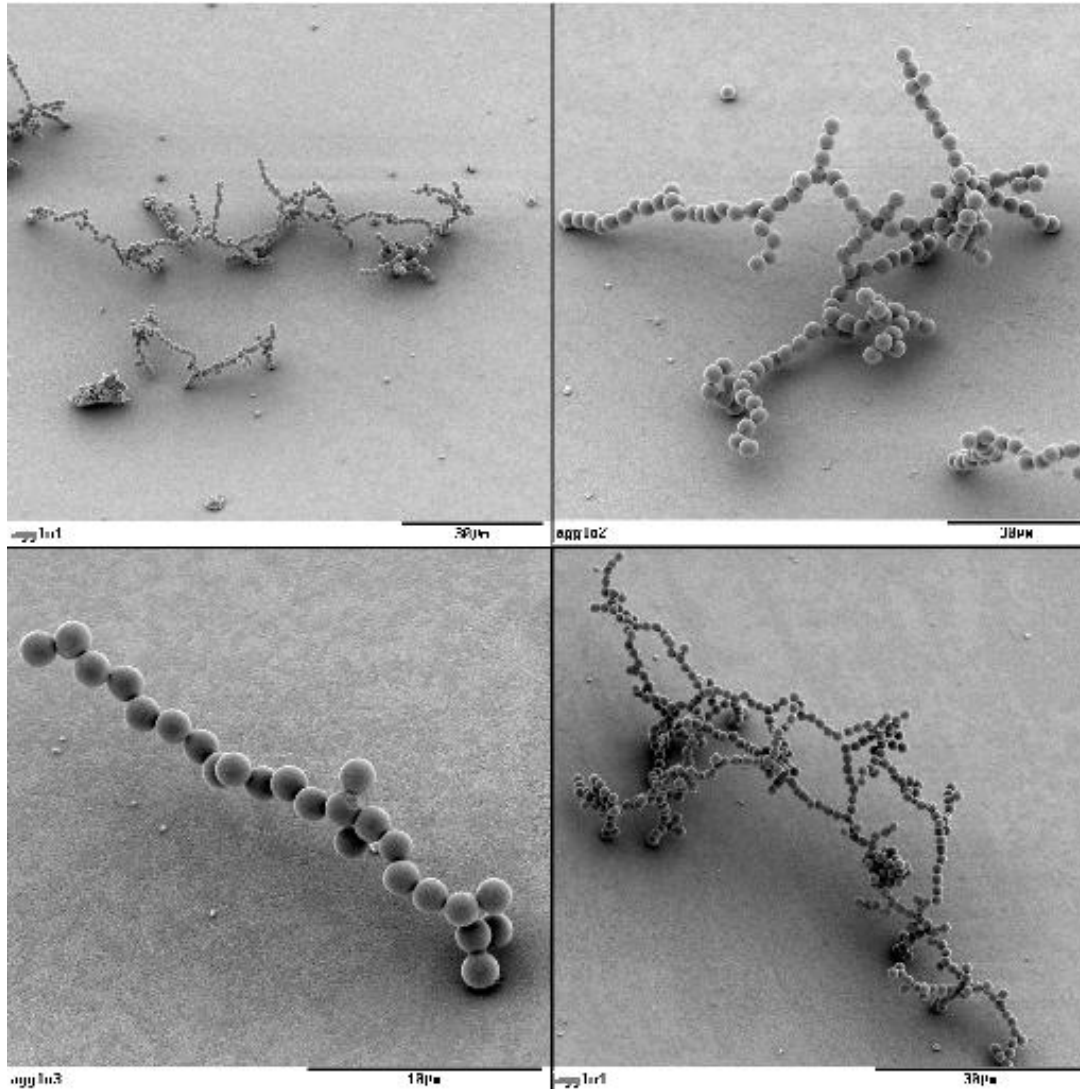


(NASA, U2)

From small to large particles
 Slow formation (10^6 Years)
 Need: High sticking probability
(Comets, asteroids, solid planets, cores of planets)
 (Preferred for Solar System)



Laboratory-Experiments μm -sized particles

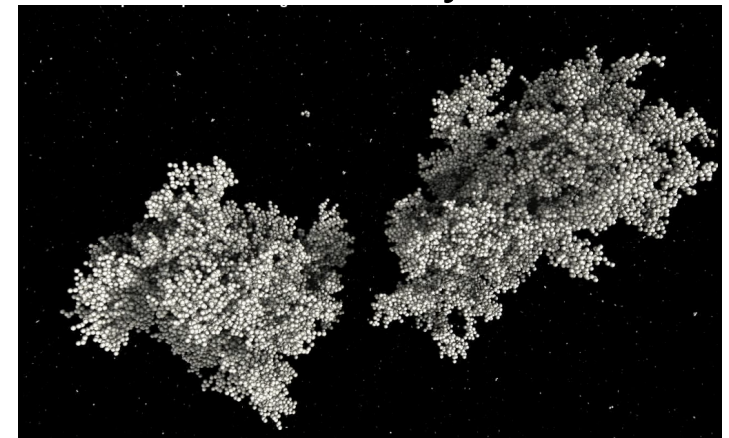


(J. Blum, Braunschweig)

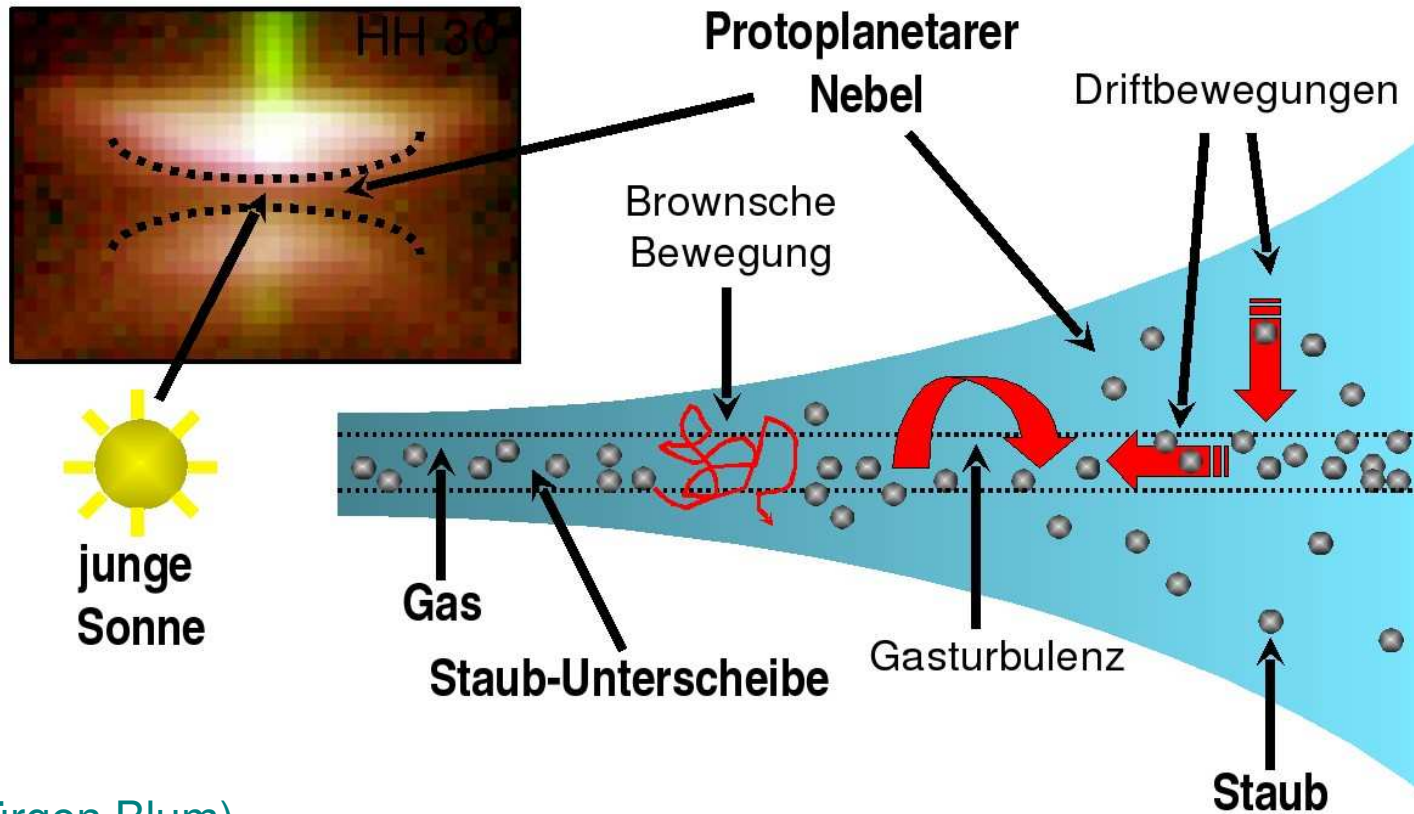
Sticking through:
Van der Waals forces
Fractal Growth:
works up to cm-sizes
for ices much larger
followed by compaction

Numerical Simulations

Here: Molecular dynamics



(Alexander Seizinger, Tübingen)



(Jürgen Blum)

Particles have relative velocity with respect to the gas \Rightarrow frictional forces

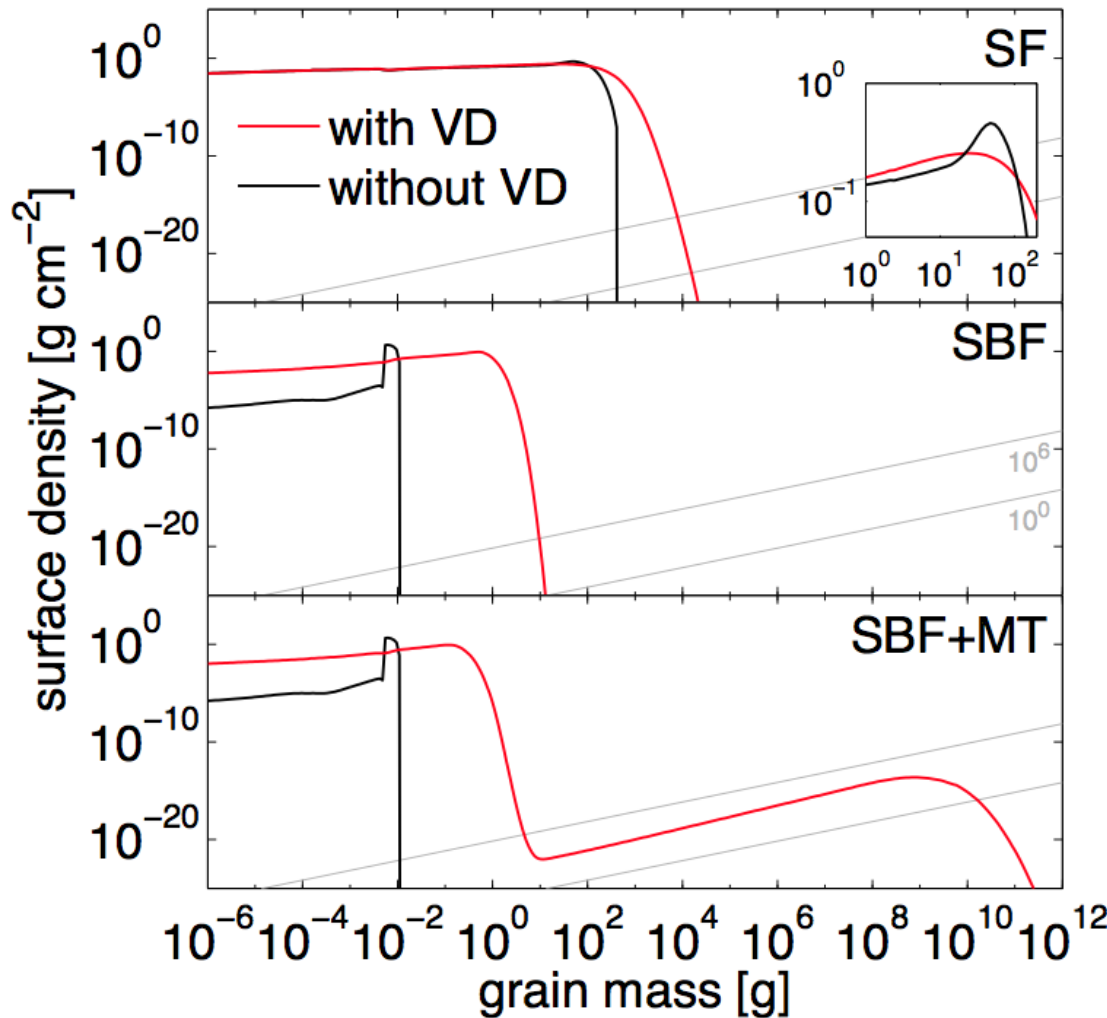
Problem I: Fast radial drift towards star (for 1m Size: 1 AU / 100 Years)

Problem II: Destructive Collisions (Bouncing)

Note: Disk is hotter near central star, better condensation beyond iceline



Enhanced Growth via a velocity distribution



SF:

Sticking + Fragmentation

SBF:

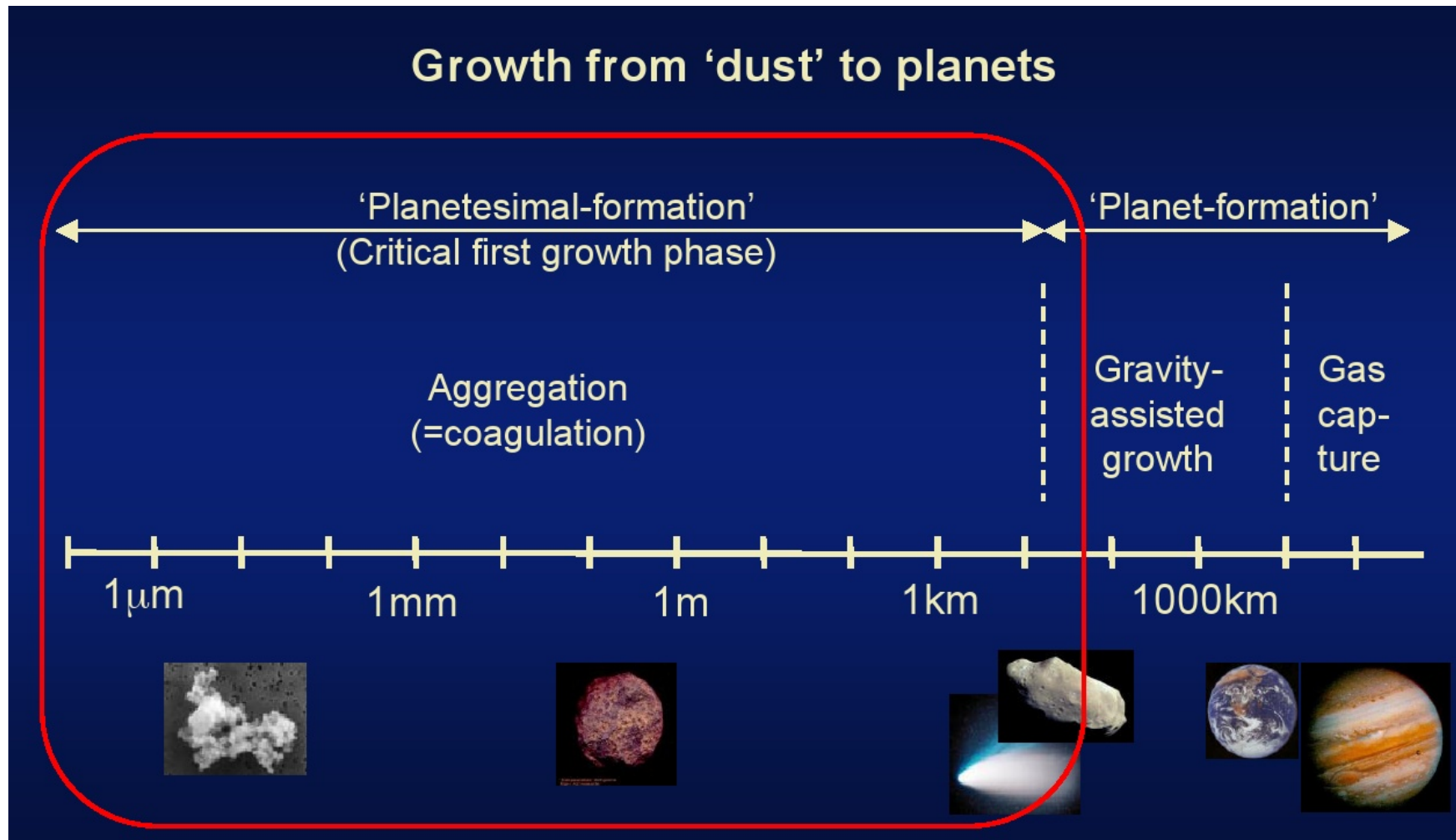
Sticking, Bouncing & Fragmentation

SBF+MT:

mass transfer added

(Fredrick Windmark)

Other options: Dust in inhomogeneities (turbulence, vortices, pressure jumps)



(C. Dullemond)

Dust \Rightarrow Planetesimals ($\mu\text{m} \Rightarrow 1\text{-}10\text{km}$, through Collisions)

Mass rich planets: Gravitation & Gas Accretion

Timescale problem for massive planets



- Not possible to form hot Jupiters in situ
 - disk too hot for material to condense
 - not enough material
- Difficult to form massive planets
 - gap formation
- Eccentric and inclined orbits
 - planets form in flat disks (on circular orbits)

But planets grow in disks:

⇒ Have a closer look at planet-disk interaction

Have two contributions: Spiral arms & Corotation effects

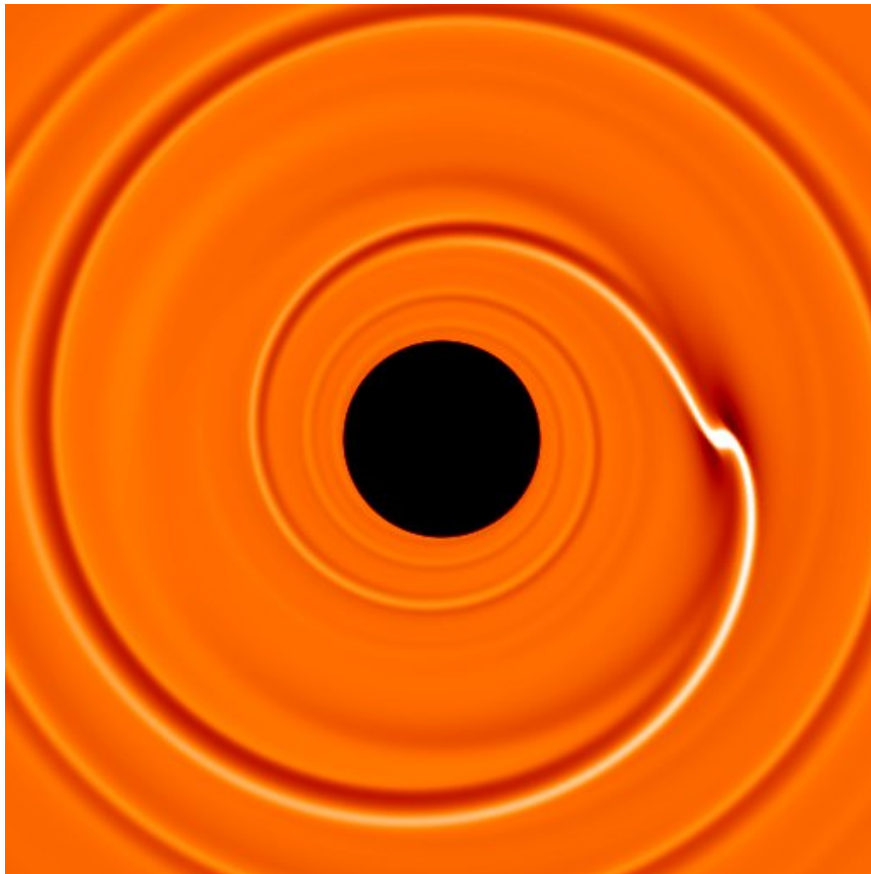
(more details: [Annual Review article by Kley & Nelson, ARAA, 50, 2012](#))



Young planets are embedded in gaseous disk

Creation of **spiral arms**:

- stationary in planet frame
- Linear analysis,
- Hydro simulations



Inner Spiral

- pulls planet forward:
- positive torque

Outer Spiral

- pulls planet backward:
- negative torque

→ Net Torque

⇒ Migration

Most important:

Strength & Direction ?

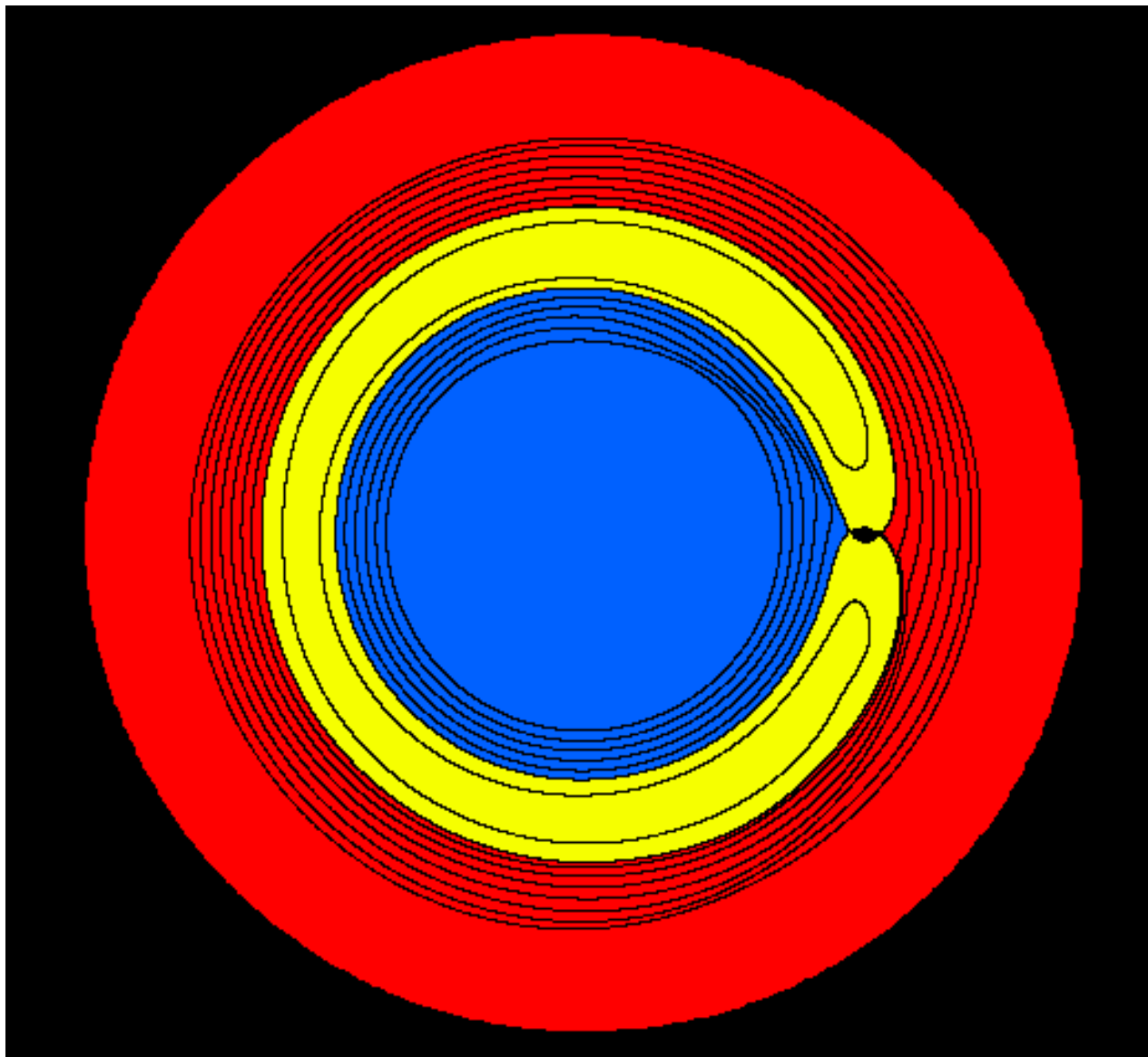
Typically: Outer spiral wins

⇒ Inward Migration

Explains Hot Jupiters

But: Too rapid !

(Masset, 2001)



3 Regions

Outer disk (spiral)

Inner disk (spiral)

⇒ Lindblad torques

Horseshoe (coorbital)

⇒ Corotation Torques
(Horseshoe drag)

Scaling with:

- Vortensity gradient
(Vorticity/density)

Positive or negative

Counterbalances
Lindblad Torques

(F. Masset)



Torque **on** the planet:

$$\Gamma_{\text{tot}} = - \int_{\text{disk}} \Sigma(\vec{r}_p \times \vec{F}) df = \int_{\text{disk}} \Sigma(\vec{r}_p \times \nabla \psi_p) df = \int_{\text{disk}} \Sigma \frac{\partial \psi_p}{\partial \varphi} df \quad (1)$$

3D analytical (Tanaka et al. 2002) and numerical (D'Angelo & Lubow, 2010)

$$\Gamma_{\text{tot}} = -(1.36 + 0.62\beta_{\Sigma} + 0.43\beta_T) \Gamma_0. \quad (2)$$

where

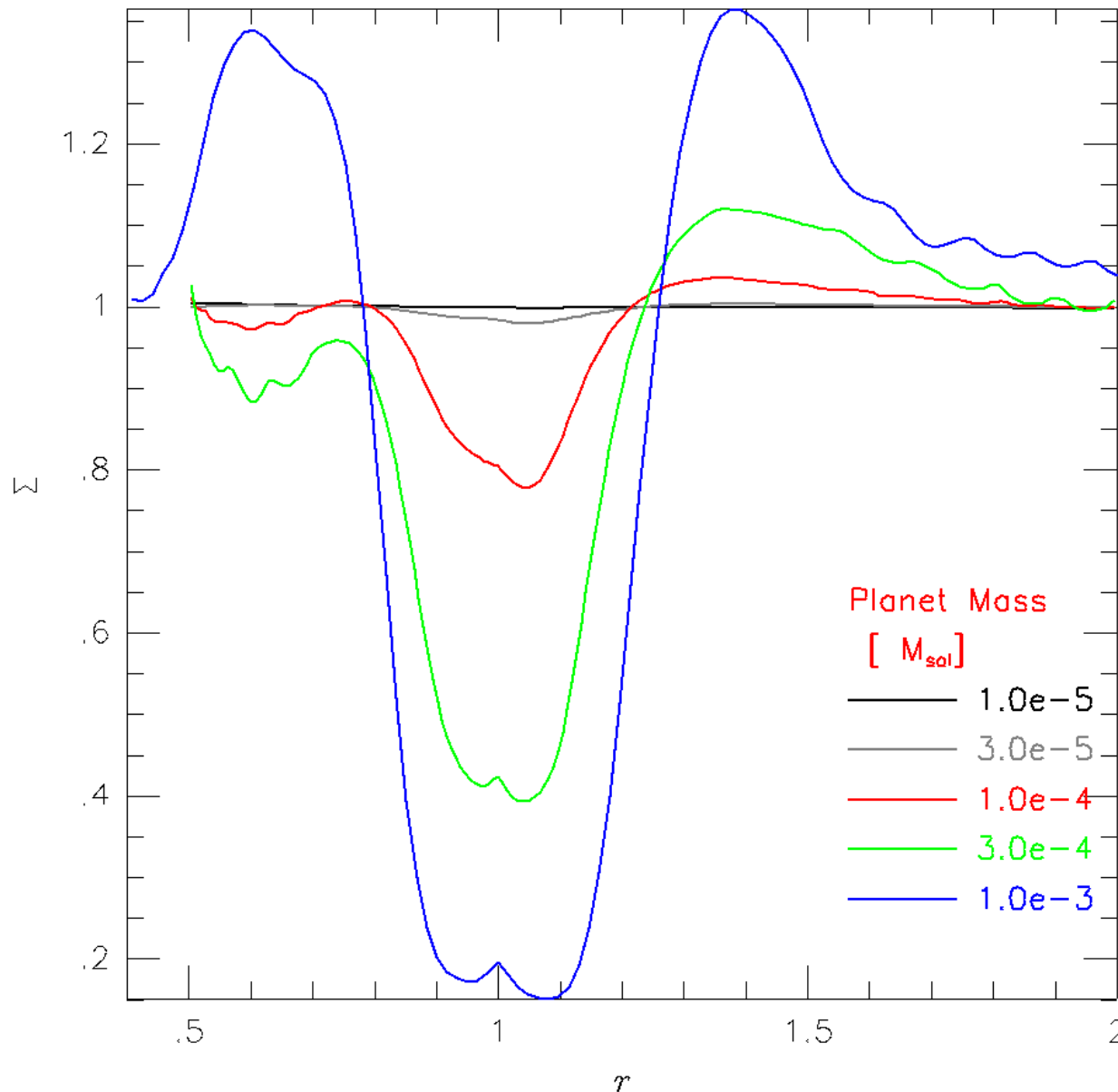
$$\Sigma(r) = \Sigma_0 r^{-\beta_{\Sigma}} \quad \text{and} \quad T(r) = T_0 r^{-\beta_T} \quad (3)$$

and normalisation

$$\Gamma_0 = \left(\frac{m_p}{M_*} \right)^2 \left(\frac{H}{r_p} \right)^{-2} (\Sigma_p r_p^2) r_p^2 \Omega_p^2, \quad (4)$$

$$\Rightarrow \text{Migration} \quad \dot{J}_p = \Gamma_{\text{tot}} \quad \Rightarrow \quad \frac{\dot{a}_p}{a_p} = 2 \frac{\Gamma_{\text{tot}}}{J_p} \quad (5)$$

Low Planet Mass (Type I): Typically Negative & fast



$$M_p = 0.01 M_{\text{Jup}}$$

$$M_p = 0.03 M_{\text{Jup}}$$

$$M_p = 0.1 M_{\text{Jup}}$$

$$M_p = 0.3 M_{\text{Jup}}$$

$$M_p = 1.0 M_{\text{Jup}}$$

Depth depends on:

- M_p
- Viscosity
- Temperature

Torques reduced:

Migration slows

Type I \Rightarrow Type II

linear \Rightarrow non-linear

Planet moves with
(viscous) disk



2D hydro-simulations:

- small mass
- inviscid

Note:

for barotropic and inviscid flows:

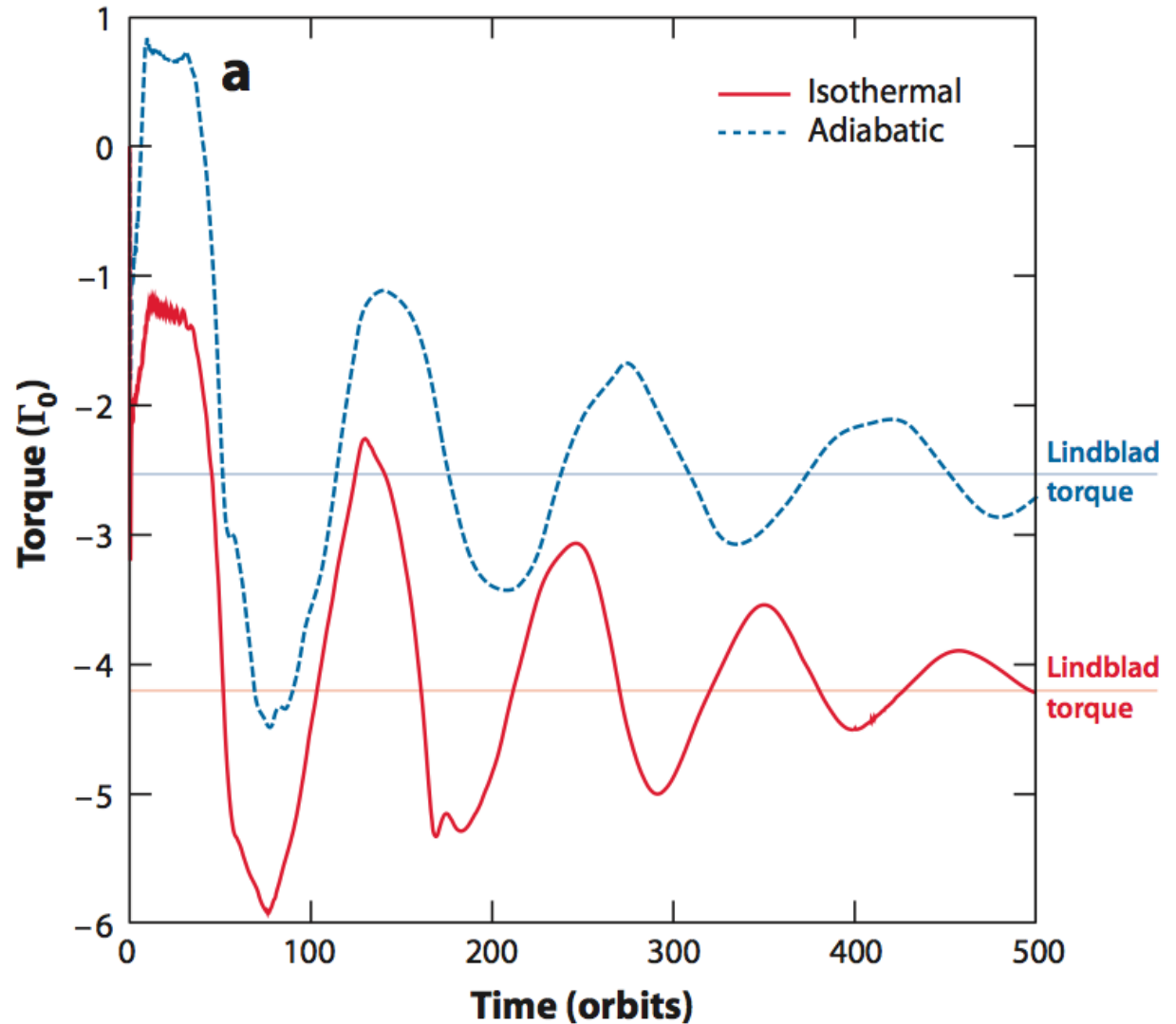
$$\frac{d}{dt} \left(\frac{\omega_z}{\Sigma} \right) = 0$$

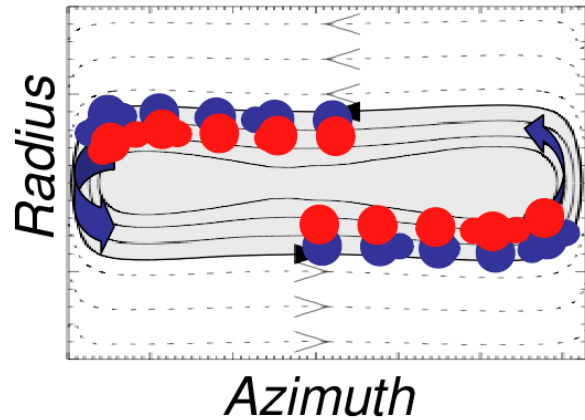
$$\frac{dS}{dt} = 0$$

Torque depends on:
 Gradients of ω_z/Σ , S
 ω_z Vorticity
 S Entropy

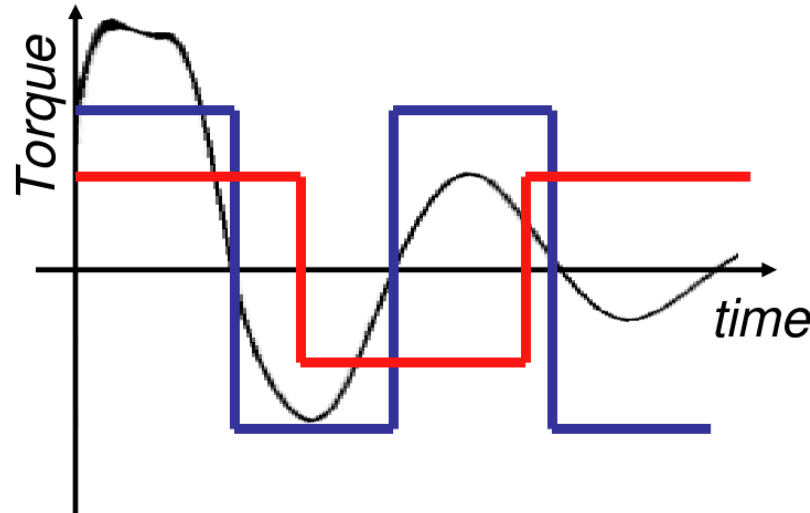
Gradients are wiped out in the corotation region

Total torque vs. time - isothermal - adiabatic



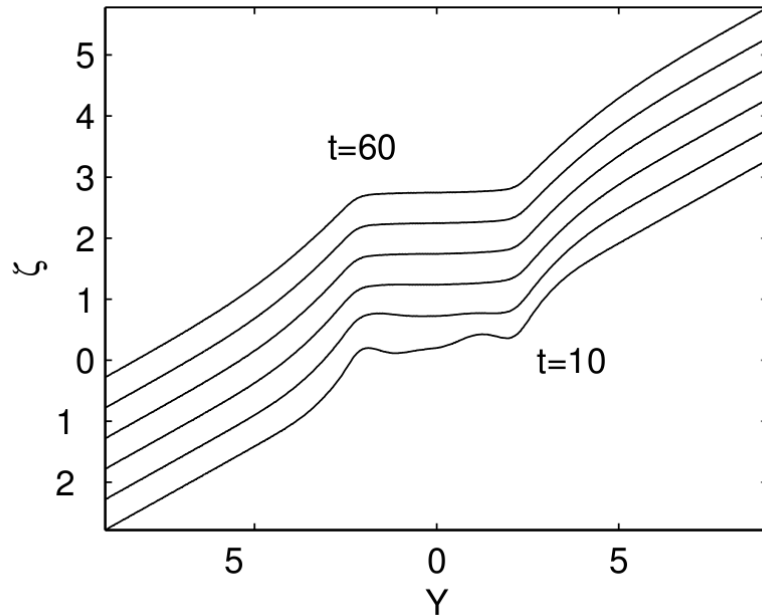


(F. Masset)

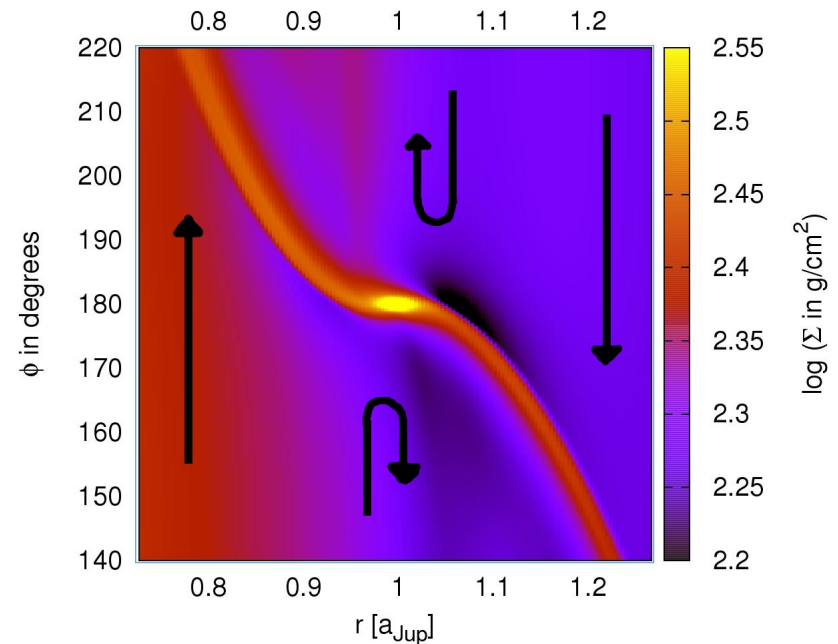


Red and Blue
Orbits have
different periods
⇒ Phase mixing

(a) Mean vorticity



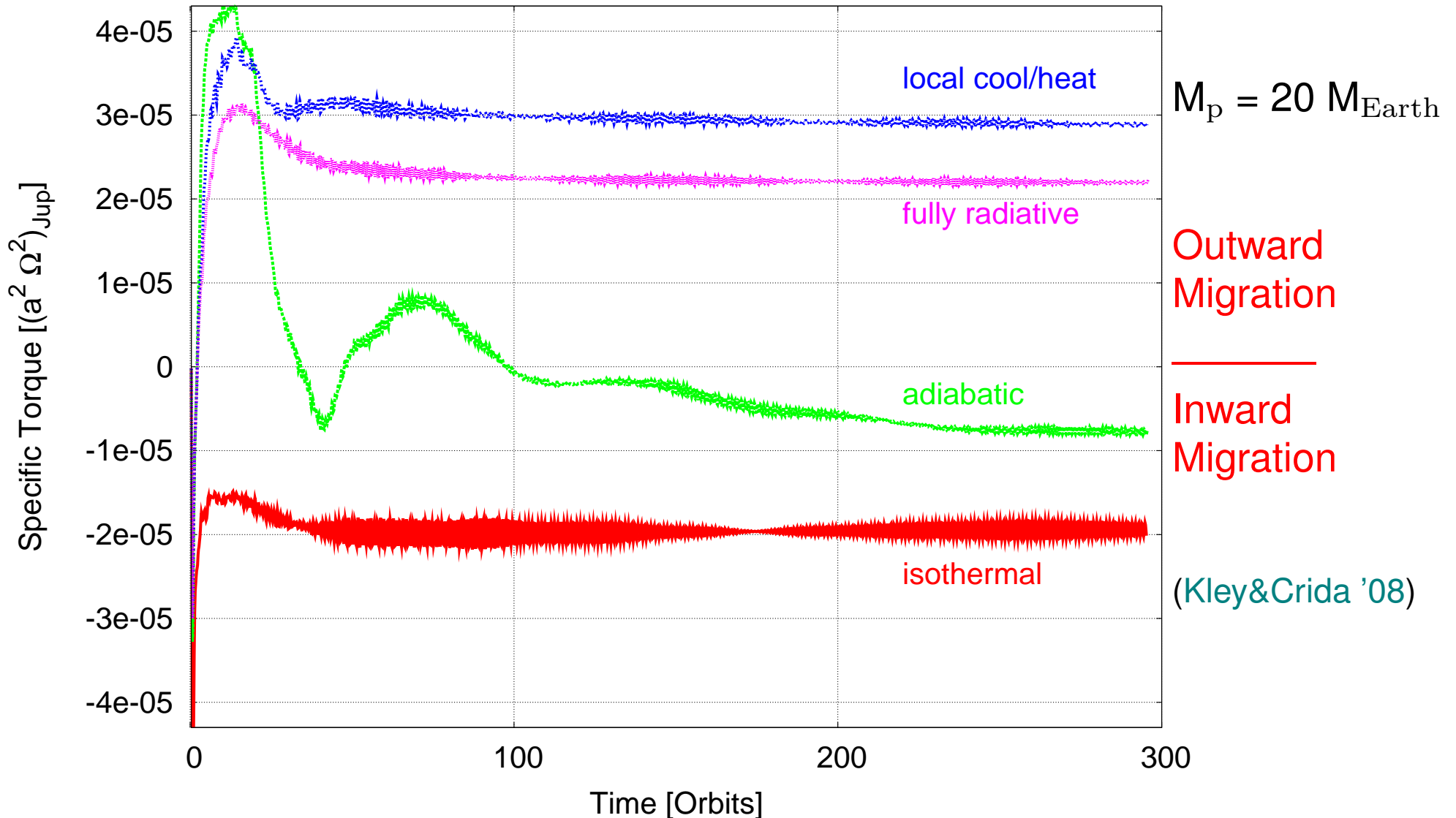
(Balmforth & Korycanski)



3D radiative disk (B. Bitsch)



$$\frac{\partial \Sigma c_v T}{\partial t} + \nabla \cdot (\Sigma c_v T \mathbf{u}) = -p \nabla \cdot \mathbf{u} + D - Q - 2H \nabla \cdot \vec{F}$$





Total torque
vs. viscosity:

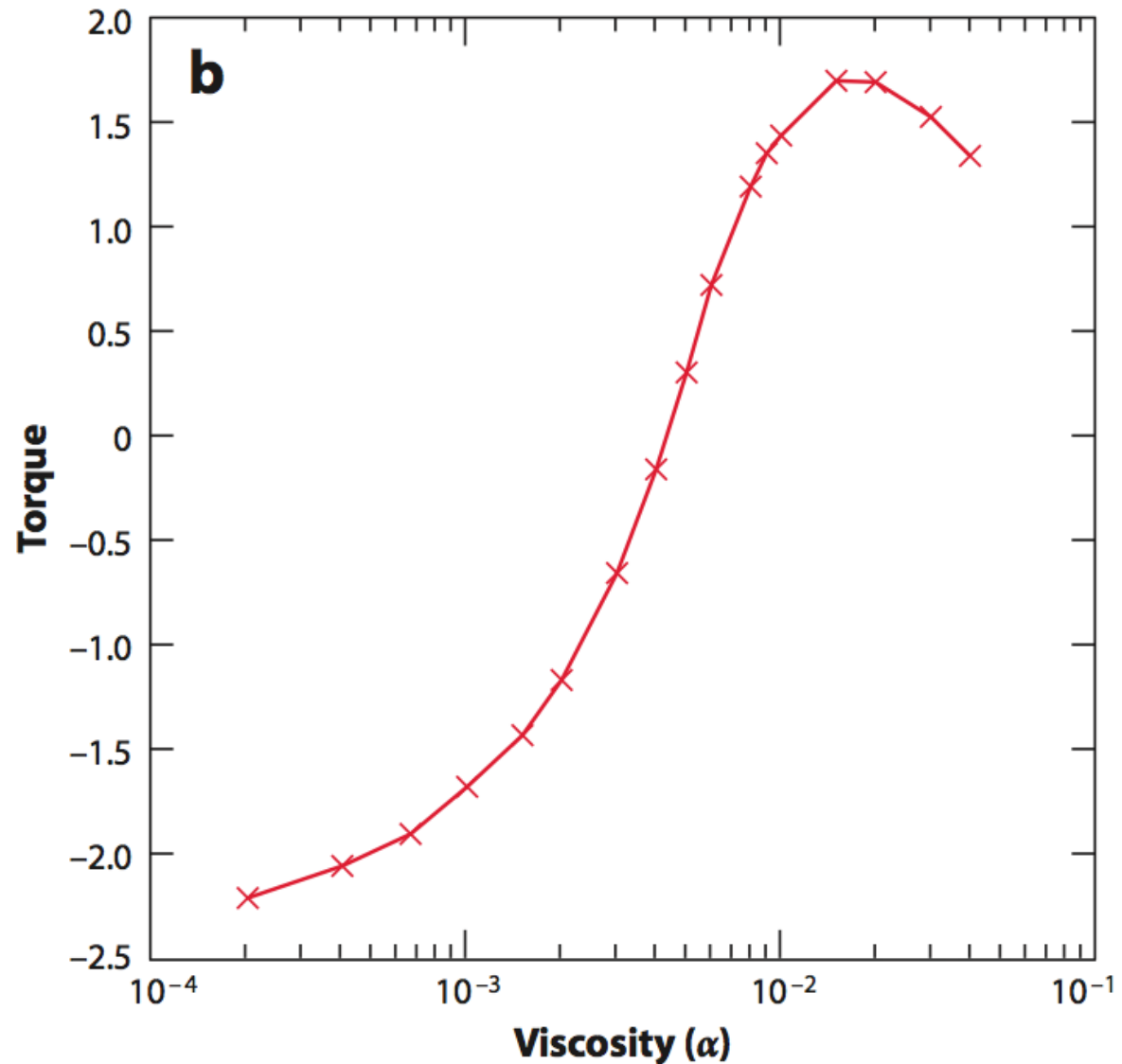
in **viscous** α -disk
2D **radiative** model
- in equilibrium

Efficiency depends
of ratio of timescales

$$\frac{\tau_{\text{visc}}}{\tau_{\text{librat}}}$$

$$\frac{\tau_{\text{rad}}}{\tau_{\text{librat}}}$$

Local disk properties
matter

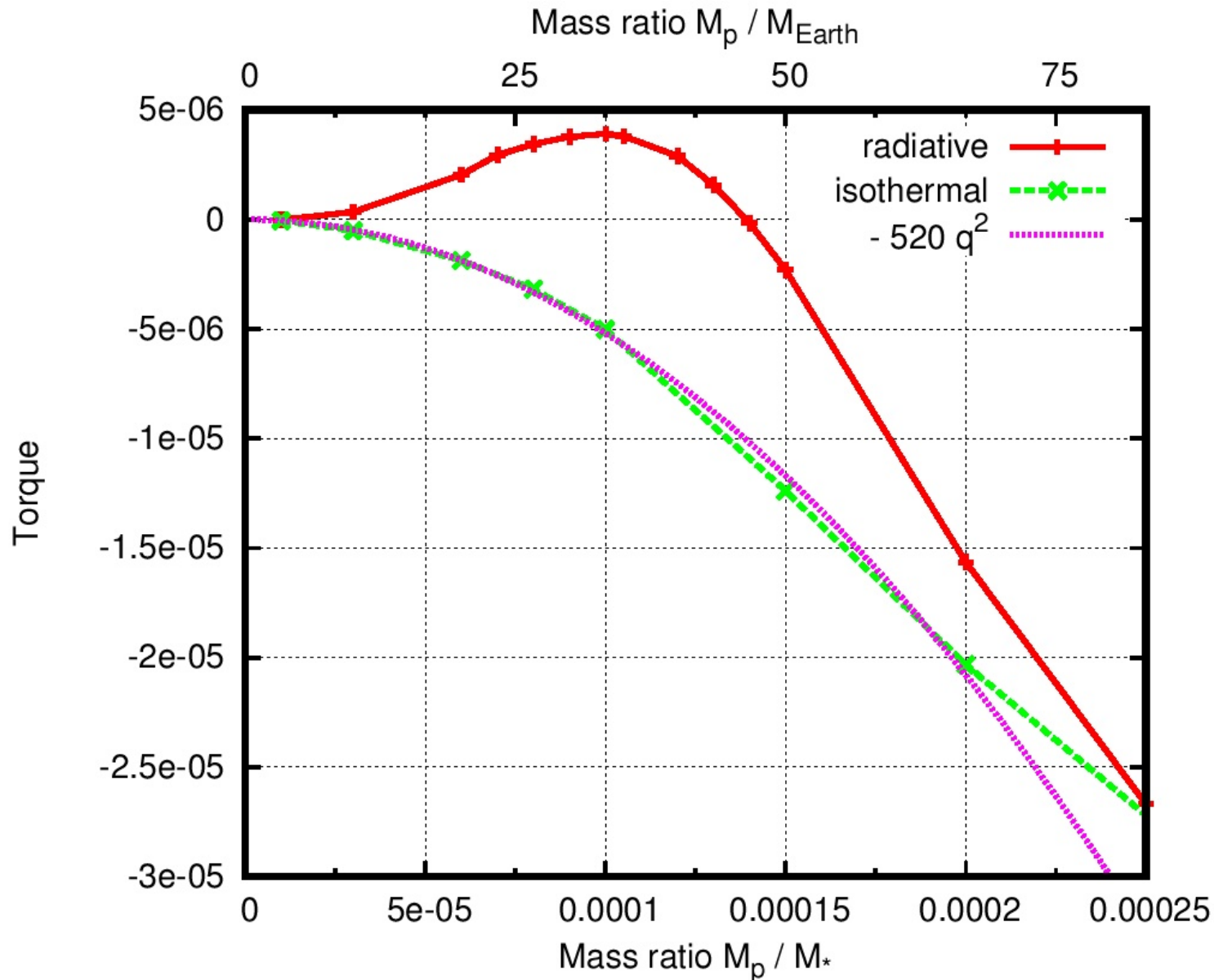


(Kley & Nelson 2012)

\Rightarrow Need viscosity to prevent saturation !



Isothermal and radiative models. Outward migration for $M_p \leq 40 M_{\text{Earth}}$



Vary M_p
(Kley & Crida 2008)

In full 3D
(Kley ea 2009)

With irradiation:
Bitsch ea. (2012)

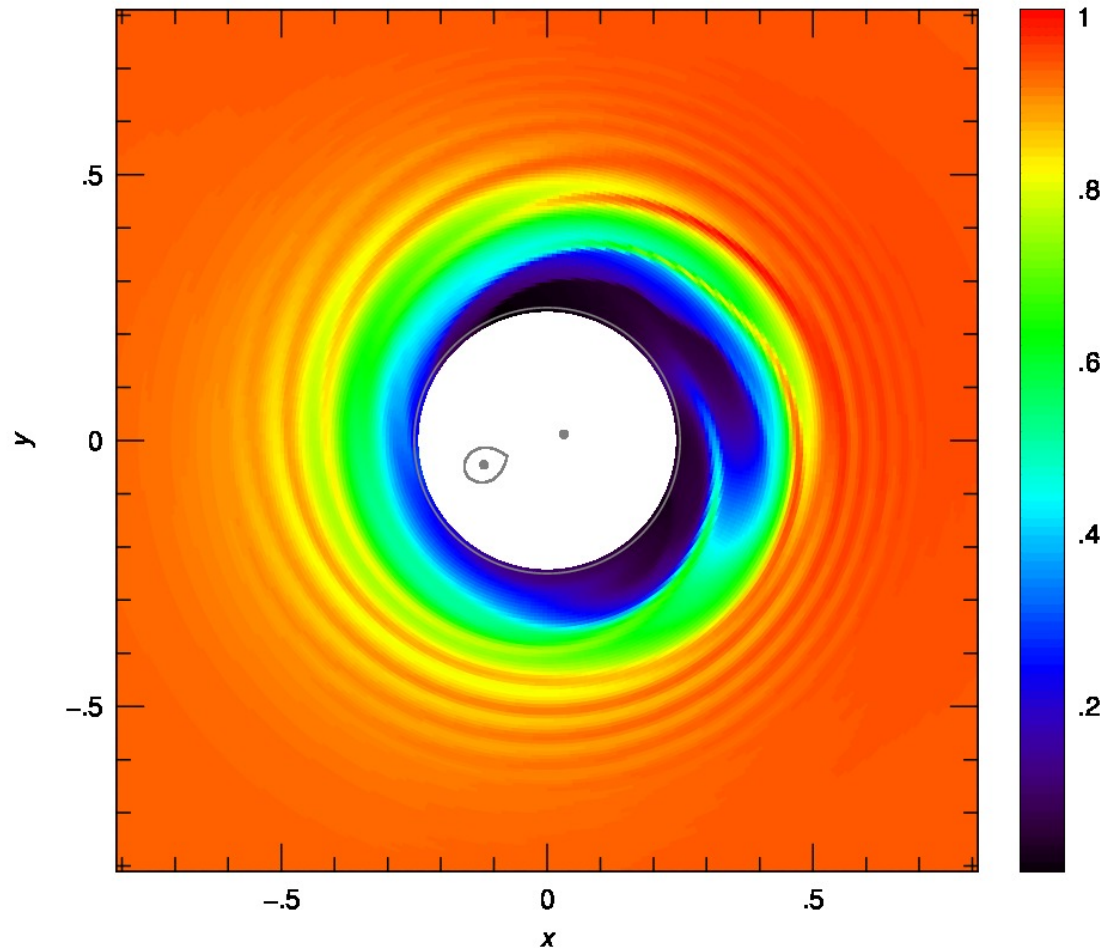


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- RV-Obs.: ≈ 50 multi-planet extrasolar planetary systems
 $\approx 1/4$ contain planets in a low-order **mean-motion resonance** (MMR)
In **Solar System**: 3:2 between Neptune and Pluto (plutinos)
 - Resonant capture through convergent migration process
dissipative forces due to disk-planet interaction
 - Existence of resonant systems
 - **Clear evidence for planetary migration** (next Talk: R.Nelson)
 - Hot Jupiters (Neptunes) & Kepler systems
 - **Clear evidence for planetary migration**



Animation of disk around Binary Star
(shown is the surface density)

k38a : ρ (0.25, 3.0546E-09, 1.0357E+00) N=3500000; t= 3057.829



Binary Parameter:

$$M_1 = 0.95 M_{\odot},$$

$$M_2 = 0.25 M_{\odot}$$

$$a_B = 0.15 \text{ AU}$$

$$e_B = 0.10$$

Planet Parameter:

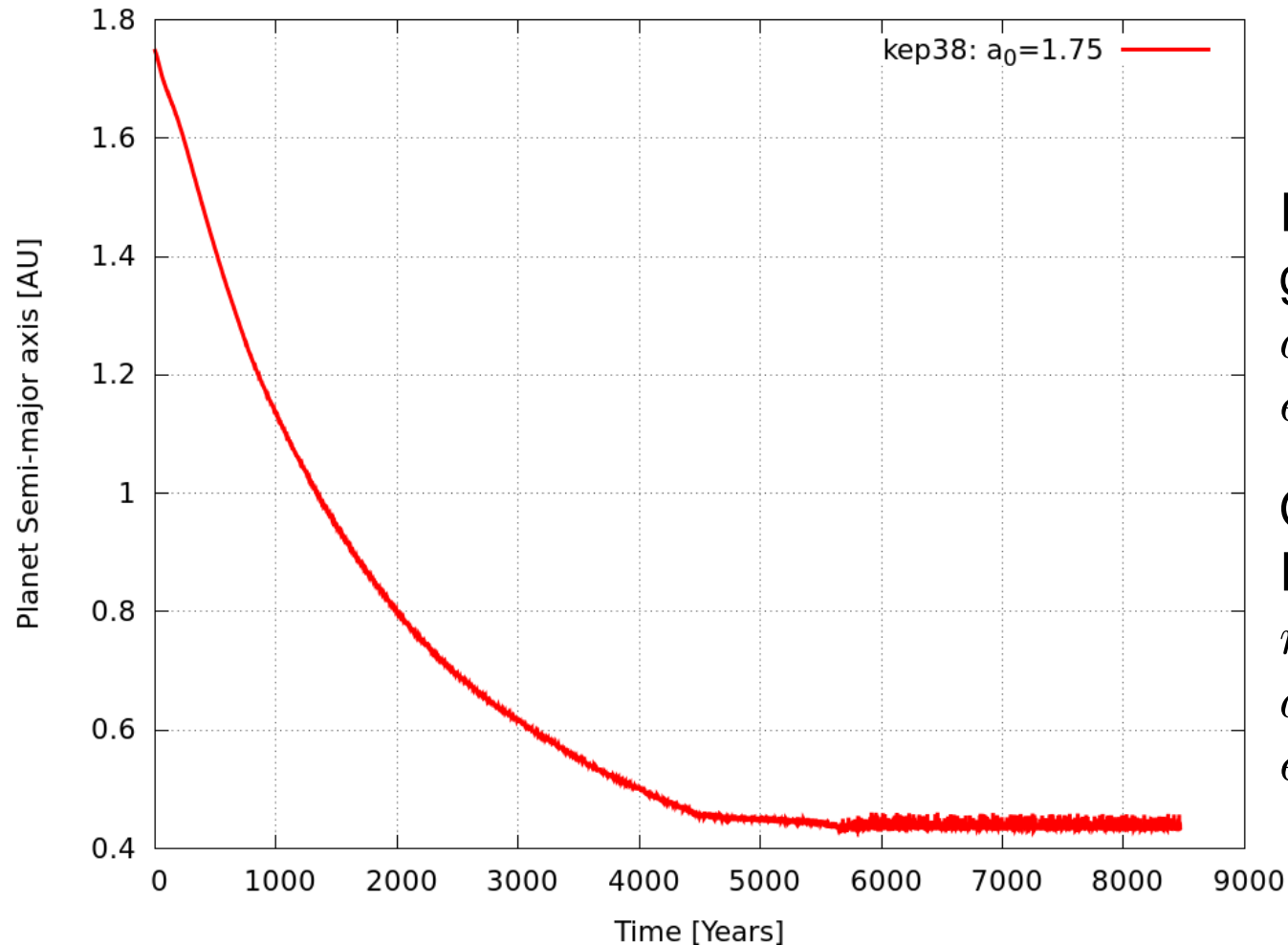
$$m_p = 0.36 M_{Jup}$$

$$a_p = 0.46 \text{ AU}$$

$$e_p = 0.03$$



Migration of planet in disk



Planet stops at
gap edge with:

$$a_p = 0.43 \text{ AU}$$

$$e_p = 0.15 \text{ AU}$$

Observed

Planet Parameter:

$$m_p = 0.36 M_{Jup}$$

$$a_p = 0.46 \text{ AU}$$

$$e_p = 0.03$$

(Kley & Haghighipour, in prep.)

(see also: Pierens & Nelson, 2013)



Planets form through bottom-up process

- Dust agglomeration, core formation, rapid gas accretion

Planets migrate in disks

- Lindblad and Corotation Torques
- Inward or outward, depending on local disk physics

Example: Circumbinary Planet

The Plato Connection:

Interpret Orbital and Physical Parameter through simultaneous modeling of Formation and Evolution

(very useful: multiple systems)

⇒ see the following talks !



Thank you for your attention !

(A. Crida)